

# INTERNATIONAL STANDARD

**ISO**  
**10767-2**

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## Hydraulic fluid power — Determination of pressure ripple levels generated in systems and components —

### Part 2: Simplified method for pumps

*Transmissions hydrauliques — Détermination des niveaux d'onde  
de pression engendrés dans les circuits et composants —*

*Partie 2: Méthode simplifiée pour les pompes*



Reference number  
ISO 10767-2:1999(E)

## Contents

<b>1 Scope</b> .....	<b>1</b>
<b>2 Normative references</b> .....	<b>1</b>
<b>3 Terms and definitions</b> .....	<b>1</b>
<b>4 Symbols and units</b> .....	<b>2</b>
<b>5 Instrumentation</b> .....	<b>3</b>
<b>6 General provisions</b> .....	<b>3</b>
<b>7 Determination of geometric parameters and speed of sound in the test fluid</b> .....	<b>3</b>
<b>8 Valid frequency and pressure range</b> .....	<b>4</b>
<b>9 Test circuit</b> .....	<b>4</b>
<b>10 Test procedure</b> .....	<b>6</b>
<b>11 Data presentation</b> .....	<b>6</b>
<b>12 Identification statement</b> (Reference to this part of ISO 10767) .....	<b>7</b>
<b>Annex A</b> (normative) <b>Test report forms</b> .....	<b>8</b>
<b>Annex B</b> (informative) <b>Tutorial explanation of the basis for the test procedure given in this part of ISO 10767 for measuring pump pressure ripple</b> .....	<b>10</b>
<b>Bibliography</b> .....	<b>20</b>

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## Foreword

ISO (the International Organization for Standardization) is a worldwide federation of national standards bodies (ISO member bodies). The work of preparing International Standards is normally carried out through ISO technical committees. Each member body interested in a subject for which a technical committee has been established has the right to be represented on that committee. International organizations, governmental and non-governmental, in liaison with ISO, also take part in the work. ISO collaborates closely with the International Electrotechnical Commission (IEC) on all matters of electrotechnical standardization.

International Standards are drafted in accordance with the rules given in the ISO/IEC Directives, Part 3.

Draft International Standards adopted by the technical committees are circulated to the member bodies for voting. Publication as an International Standard requires approval by at least 75 % of the member bodies casting a vote.

International Standard ISO 10767-2 was prepared by Technical Committee ISO/TC 131, *Fluid power systems*, Subcommittee SC 8, *Product testing*.

ISO 10767 consists of the following parts, under the general title *Hydraulic fluid power — Determination of pressure ripple levels generated in systems and components*:

- *Part 1: Precision method for pumps*
- *Part 2: Simplified method for pumps*
- *Part 3: Method for motors*

Annex A forms a normative part of this part of ISO 10767. Annexes B and C are for information only.

## Introduction

In hydraulic fluid power systems, power is transmitted and controlled through a liquid under pressure within an enclosed circuit. Hydraulic pumps are devices which convert rotary mechanical power into fluid power. Pump flow has a large, steady component and a smaller, cyclical component superimposed upon it. It is this smaller, cyclical component of the pump flow that reacts with the fluid system of the pump and its circuit, that results in pressure ripple or fluid-borne noise. This fluid-borne noise can be transmitted through the liquid under pressure to other attached components and structures, and can result in unwanted noise and vibrations.

While the flow ripple is the cause of the pressure ripple, it is more difficult to measure. Therefore pressure ripple will be used in this procedure to characterize the fluid-borne noise generation potential of hydraulic fluid power pumps. Pressure ripple is a function of the pump design and the circuit in which it is measured. It is important, therefore, that the test circuit be controlled so as to provide uniform results when comparing the fluid-borne noise generation potential of different types of pumps. Pressure ripple determined in accordance with this part of ISO 10767 may be different to that measured in fluid power systems because of the high impedance of the test line.

# Hydraulic fluid power — Determination of pressure ripple levels generated in systems and components —

## Part 2: Simplified method for pumps

### 1 Scope

This part of ISO 10767 specifies a procedure for measuring the fluid pressure ripple characteristics of hydraulic fluid power pumps with a maximum error of + 1 dB to – 3 B.

ISO 10767-1 can be used if pressure ripple measurements at lower pressure levels, lower frequencies, or at greater accuracy levels is required. This procedure covers a frequency and pressure range that has been found to excite many circuits to emit airborne noise that most concerns designers of hydraulic fluid power systems. It allows the pressure ripple data to be published with minimal calculations and processing of the measured data. This part of ISO 10767 promotes quieter fluid power systems by establishing a uniform procedure for measuring and reporting the fluid pressure ripple characteristics of hydraulic fluid power pumps. Annex B contains a tutorial explanation of the technical basis for this test procedure.

### 2 Normative references

The following normative documents contain provisions which, through reference in this text, constitute provisions of this part of ISO 10767. For dated references, subsequent amendments to, or revisions of, any of these publications do not apply. However, parties to agreements based on this part of ISO 10767 are encouraged to investigate the possibility of applying the most recent editions of the normative documents indicated below. For undated references, the latest edition of the normative document referred to applies. Members of ISO and IEC maintain registers of currently valid International Standards.

ISO 1000:1992, *SI units and recommendations for the use of their multiples and of certain other units*.

ISO 1219-1:1991, *Fluid power systems and components — Graphic symbols and circuit diagrams — Part 1: Graphic symbols*.

ISO 5598:1985, *Fluid power systems and components — Vocabulary*.

ISO 9110-1:1990, *Hydraulic fluid power — Measurement techniques — Part 1: General measurement principles*.

ISO 10767-1:1996, *Hydraulic fluid power — Determination of pressure ripple levels generated in systems and components — Part 1: Precision method for pumps*.

### 3 Terms and definitions

For the purposes of this part of ISO 10767, the fluid power terms and definitions given in ISO 5598, the acoustical terms and definitions given in ISO 10767-1 and the following apply.

### 3.1 pump outlet port passage length

$L_S$

average length from the volume exchange cavities of the pump to the entrance of the test line in normal operation at the test conditions specified

### 3.2 pump outlet port passage diameter

$D_S$

average diameter of the discharge cavity from the volume exchange cavities of the pump to the entrance of the test line in normal operation at the test conditions specified

## 4 Symbols and units

4.1 For the purposes of this part of ISO 10767, the symbols given in Table 1 apply.

Table 1 — Symbols

Symbol	Quantity
$B$	bulk modulus of elasticity of the test fluid
$c_0$	reference speed of sound in test fluid not corrected for test line elasticity
$D_L$	inside diameter of test line
$D_{O,min}$	minimum line termination orifice diameter
$D_{O,max}$	maximum line termination orifice diameter
$D_S$	pump outlet port passage diameter
$E$	modulus of elasticity of test line material
$f_1$	fundamental pumping frequency
$f_{max}$	maximum frequency limit of test procedure
$K$	orifice flow coefficient, $K = \frac{4q}{\pi D_O^2 \sqrt{\Delta p}}$ (1)
$L_L$	test line length
$L_S$	pump outlet port passage length
$Z$	number of pumping chambers per revolution
$n$	harmonic number $n = 1, 2, 3, \dots$
$N$	pump shaft speed
$P_n$	amplitude of $n$ -th harmonic of pressure ripple (i.e. $\frac{1}{2}$ of peak-to-peak)
$p_{RMS}$	the root mean square (RMS) average of the pressure ripple harmonics from $f_1$ to $f_{max}$
$p_{max}$	maximum pump outlet test pressure
$p_{min}$	minimum pump outlet test pressure
$\Delta p$	orifice pressure drop
$q$	average pump flow rate
$\rho$	mass density of test fluid
$t$	wall thickness of test line
$V_S$	pump outlet passage volume

4.2 Units used in this part of ISO 10767 are in accordance with ISO 1000.

4.3 Graphic symbols used in this part of ISO 10767 are in accordance with ISO 1219-1 unless otherwise stated.

## 5 Instrumentation

5.1 The instruments used to measure flow, pressure, drive speed, and oil temperature shall be in accordance with the recommendations in ISO 9110-1.

5.2 Pressure transducers for measuring pressure ripple shall be piezoelectric type transducers capable of accurate measurements from the pump drive shaft frequency up to 10 kHz minimum in accordance with ISO 9110-1.

5.3 The harmonic content of the pressure ripple shall be established as a function of frequency. This may be achieved using a Fast Fourier Transform (FFT) narrow-band spectrum analyzer. The analysis shall produce accurate measurements from drive shaft frequency up to 10 kHz minimum in accordance with ISO 9110-1.

## 6 General provisions

6.1 Control the average pressure, drive shaft speed, and fluid temperature to a class B accuracy level in accordance with ISO 9110-1.

6.2 Use the test fluid for which pressure ripple data is desired. Make sure that the test fluid is acceptable for use with the test pump.

6.3 Use extra care when installing pump inlet lines to maintain the inlet pressure within the manufacturer's rated conditions and to prevent air from leaking into the circuit.

6.4 "Run-in" the pump in accordance with the manufacturer's recommendations prior to running tests.

6.5 Run the pump to purge air from all lines and circuit components prior to running tests. All test conditions shall be stabilized within the limits specified in 6.1.

6.6 Use extra care to ensure that the operating pressure of the test lines, components, and the test pump does not exceed the manufacturer's ratings. Do not install any additional components to the test circuit because this can affect the accuracy of the measurements.

**WARNING — Line pressure is determined by pump flow and the orifice size selected for the test circuit. Incorrect orifice size can result in extreme line pressure. Take the necessary safety precautions to protect both test equipment and personnel from extreme line pressure.**

## 7 Determination of geometric parameters and speed of sound in the test fluid

7.1 Values for  $D_S$  and  $L_S$  can be obtained in any one of the following ways:

- a) using the diameter of the pump outlet port as an approximation of  $D_S$  and calculating  $L_S$  from titration measurements of the pump outlet port volume  $V_S$  using the following equation:

$$L_S \approx \frac{4 V_S}{\pi D_S^2} \quad (2)$$

NOTE  $V_S$  includes all fittings up to the entrance of the test line.

- b) from the manufacturer of the test pump;

- c) by estimation from the results of a test procedure that measures the internal impedance of the test pump (e.g. ISO 10767-1).

**7.2** Values for the speed of sound in the test fluid  $c_0$  and the test fluid mass density  $\rho$  can be obtained from the manufacturer of the fluid. The speed of sound in the test fluid can be corrected for the elasticity of the test line using the following equation:

$$c = \sqrt{\frac{1}{\frac{1}{c_0^2} + \frac{(D_L + t)\rho}{E_t}}} \quad (3)$$

**7.3** If a value for the speed of sound in the test fluid  $c_0$  is not available from the manufacturer of the fluid it may be estimated using the following equation:

$$c_0 = \sqrt{B/\rho} \quad (4)$$

## 8 Valid frequency and pressure range

**8.1** The fundamental pumping frequency is  $f_1$ . It is the lowest frequency of the pump pressure ripple that can be measured with this test procedure.

$$f_1 = \frac{ZN}{60} \quad (5)$$

where  $N$  is expressed in rotations per minute in order to give  $f_1$  in hertz.

**8.2** The minimum pump outlet pressure that can be measured with this test procedure is  $p_{\min}$ .

$$p_{\min} = \frac{2\rho c q}{\pi D_S^2 \tan\left(\frac{2\pi f_1 L S}{c}\right)} \quad (6)$$

**8.3** The highest frequency that can be measured with this test procedure is 2,5 kHz or  $f_{\max}$ , whichever is the lower limit. The following equation is used to calculate  $f_{\max}$ :

$$f_{\max} = \left(\frac{c}{2LS}\right) - f_1 \quad (7)$$

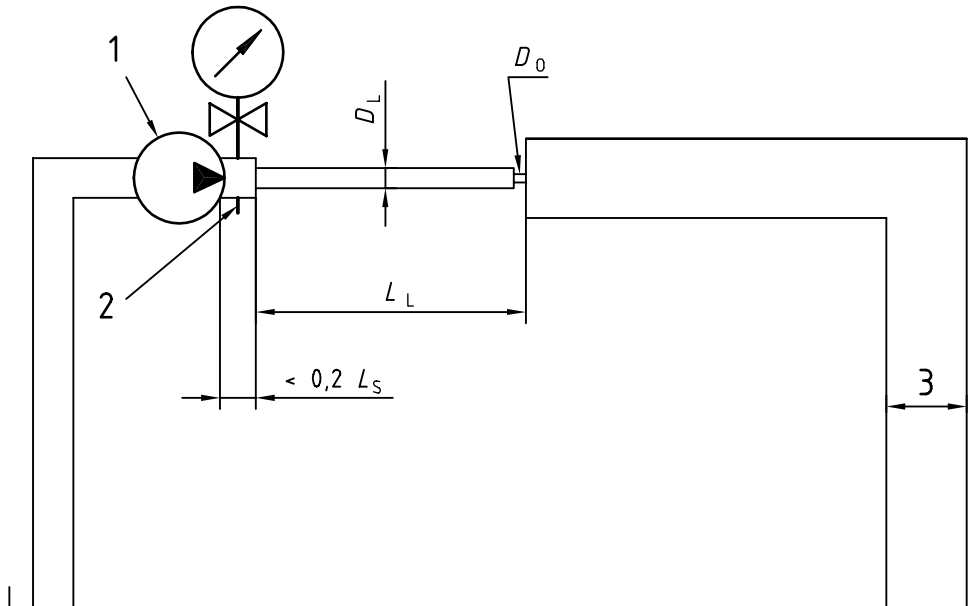
**8.4**  $p_{\max}$  is defined as the maximum pump outlet pressure where pressure ripple data is desired.  $p_{\max}$  shall be less than the maximum pump outlet pressure allowed by the pump manufacturer and shall comply with the requirements of 6.6.

**8.5** Acceptable pressure ripple measurements can be obtained with this test procedure at pump outlet pressures from  $p_{\min}$  to  $p_{\max}$  and over a frequency range from  $f_1$  to  $f_{\max}$  or 2,5 kHz whichever is the lower limit. If the value of  $p_{\min}$  calculated in 8.2 is greater than  $p_{\max}$ , valid pressure ripple measurements cannot be obtained using this test procedure.

## 9 Test circuit

**9.1** A test circuit shall be constructed as shown in Figure 1. The test pump can be a single pump, as shown in Figure 1, a multiple stage pump, or may include a boost pump or supercharge pump.



**Key**

- 1 Text pump
- 2 Piezoelectric pressure transducer
- 3 Inside diameter  $> 5D_L$

NOTE Pipeline and orifice symbols are for illustrative purposes only and are not in accordance with ISO 1219-1.

**Figure 1 — Schematic diagram of test circuit.**

**9.2** The transition from the pump outlet port to the entrance of the test line shall be completed within a distance of less than 20 % of the pump outlet port passage length  $L_S$ . Install the pressure transducer and pressure gauge between the pump outlet port and the entrance to the test line.

If the transition from outlet port to the entrance of the test line cannot be achieved within the distance specified, then this part of ISO 10767 does not apply. ISO 10767-1 may be a suitable alternative.

**9.3** Mount the pressure transducer so that its sensing surface faces upward and is essentially tangential to the flow stream.

**9.4** The outlet pressure gauge shall be shut off from the test circuit when making pressure ripple measurements. The gauge shut-off valve shall be located as close as possible to the test line to minimize branch circuit interactions.

**9.5** The test line between the pump and the termination orifice shall be steel tubing with an inside diameter estimated using the following equation:

$$D_L = \sqrt{\frac{4\rho c q}{\pi(p_{\max} + p_{\min})}} \quad (8)$$

A tubing inside diameter shall be chosen that is equal to  $D_L$  or the next smaller standard tubing size. The wall thickness of the tubing shall be chosen to comply with the operating pressure requirements given in 6.6.

**9.6** The test line length  $L_L$ , as shown in Figure 1, shall be within the following limits:

$$0,9L_S \leq L_L \leq 1,1L_S \quad (9)$$

9.7 Determine the maximum test line termination orifice diameter using the following equation:

$$D_{O,max} = \sqrt{\frac{4q}{\pi K \sqrt{p_{min}}}} \quad (10)$$

Testing with this orifice diameter will yield pump outlet pressure approximately equal to  $p_{min}$

9.8 Determine the minimum test line termination orifice diameter using the following equation:

$$D_{O,min} = \sqrt{\frac{4q}{\pi K \sqrt{p_{max}}}} \quad (11)$$

Testing with this orifice diameter will yield pump outlet pressures approximately equal to  $p_{max}$ .

9.9 The termination orifice shall be located at the entrance to the fitting at the downstream end of the test line. Care should be taken not to create any significant oil volume cavities between the end of the test line and the entrance to the termination orifice.

9.10 The line downstream of the termination orifice shall have an inside diameter greater than  $5D_L$ .

## 10 Test procedure

10.1 Install the test line termination orifice with diameter  $D_{O,max}$  as determined in 9.7.

10.2 With the pressure gauge shut-off valve opened, adjust the pump drive speed and inlet oil temperature to the desired test values.

10.3 Measure and record the actual average pump outlet port pressure.

10.4 Close the pressure gauge shut-off valve.

10.5 Measure the harmonic content of the pressure ripple. Record only the first 10 harmonics of pumping frequency. Establish the peak amplitude of each harmonic. Discard any harmonics above 2,5 kHz or  $f_{max}$ , whichever is the lower limit.

10.6 Shut down the test pump and install the test line termination orifice diameter  $D_{O,min}$  as determined in 9.9 and repeat 10.2 to 10.5.

10.7 If pressure ripple data at an average pump outlet pressure between  $p_{min}$  and  $p_{max}$  is desired, choose as many intermediate test line termination orifice diameters as desired between  $D_{O,max}$  and  $D_{O,min}$  and repeat 10.2 to 10.5 with each orifice.

10.8 If pressure ripple data at other test conditions (i.e. drive speeds, pump displacements, oil temperatures, etc.) is required, calculate a new test line diameter according to 9.5 and termination orifice diameters according to 9.7 and 9.8 and repeat 10.2 to 10.7. The requirements of 8.2, 8.3 and 8.4 shall be met with each corresponding test line diameter, termination orifice, and operating condition.

## 11 Data presentation

11.1 Report the harmonics of pumping frequency obtained in 10.5 for each pump operating condition. This data shall be reported as the amplitude (i.e. 1/2 of the peak-to-peak value) of the pressure ripple.

11.2 Calculate the overall RMS average pressure ripple amplitude for the integral harmonics of pumping frequency from  $f_1$  to  $f_{max}$  or 2,5 kHz (whichever is the lower) for each pump operating condition of 11.1. Do not include pressure ripple measurements above the tenth harmonic of pumping frequency. This can be calculated using the following equation:

$$p_{\text{RMS}} = \sqrt{\frac{P_1^2 + P_2^2 + P_3^2 + \dots + P_n^2}{2}} \quad (12)$$

**11.3** All pressure ripple measurements and test conditions shall be expressed in units in accordance with ISO 1000.

**11.4** The test information and conditions shall be reported using the forms given in annex A.

## **12 Identification statement** (Reference to this part of ISO 10767)

Use the following statement in test reports, catalogues and sales literature when electing to comply with this part of ISO 10767:

"Fluid borne noise characteristics of this pump were obtained and are presented in accordance with ISO 10767-2:1999, *Hydraulic fluid power — Determination of pressure ripple levels generated in systems and components — Part 2: Simplified method for pumps.*"

Annex A
(normative)

Test report forms

A.1 Pump pressure ripple test information form

Description of pump:
Model or identification number:
Serial number:
Part number:
Name of manufacturer:
Address of manufacturer:
Name of testing organization:
Address of testing organization:
Date of test:
Location of test:

A.2 Pump pressure ripple test conditions form

Test fluid description
Pump inlet oil temperature
Speed of sound in test fluid (corrected) c =
Reference speed of sound in test fluid (uncorrected)
c0 =
Density of test fluid
rho =
Drive shaft speed
N =
Pump outlet flow
q =
Pump outlet port passage diameter
DS =
Pump outlet port passage length
LS =
Method used to obtain DS and LS (see 7.1)
Number of pumping chambers
Z =
Test line internal diameter
DL =
Test line length
LL =
Test line wall thickness
t =

Test line material modulus of elasticity  $E =$  .....

Termination orifice diameters  $D_{O,max} =$  .....

$D_{O,min} =$  .....

Other: .....

Test pressures  $p_{min} =$  .....

$p_{max} =$  .....

Other: .....

Fundamental pumping frequency  $f_1 =$  .....

Maximum frequency  $f_{max} =$  .....

### A.3 Pump pressure ripple test results form

Drive shaft speed: .....

Test pressure: .....

Pump inlet oil temperature: .....

$P_1 =$  .....

$P_2 =$  .....

$P_3 =$  .....

$P_4 =$  .....

$P_5 =$  .....

$P_6 =$  .....

$P_7 =$  .....

$P_8 =$  .....

$P_9 =$  .....

$P_{10} =$  .....

$p_{RMS} =$  .....

## Annex B (informative)

### Tutorial explanation of the basis for the test procedure given in this part of ISO 10767 for measuring pump pressure ripple

#### Introduction

This part of ISO 10767 has been developed as a test method to provide an unbiased pump pressure ripple measurement directly from a simple test. This part of ISO 10767 is similar to ANSI/(NFPA) T 2.7.2:1995 [7] which is a method suitable for measuring the pressure ripple of many commonly used industrial hydraulic pumps. It does not cover as broad a frequency range and pressure range as this part of ISO 10767 but it will yield valid comparative data on which to make selections of pumps where fluid-borne noise is a concern. It is also possible for the method specified in this part of ISO 10767 to be conducted with the test pump operating in a modified version of its intended application for comparison with manufacturer's laboratory measurements.

ISO 10767-1 (the precision method) requires more specialized laboratory test equipment and an additional pump or pressure ripple source to provide measurements that allow the test pump pressure ripple, flow ripple, internal impedance, and the speed of sound in the test fluid to be calculated. Because of the nature of the required complex calculations, ISO 10767-1 is best suited for use in a laboratory with computer based data acquisition and analysis equipment.

#### B.1 Additional Symbols

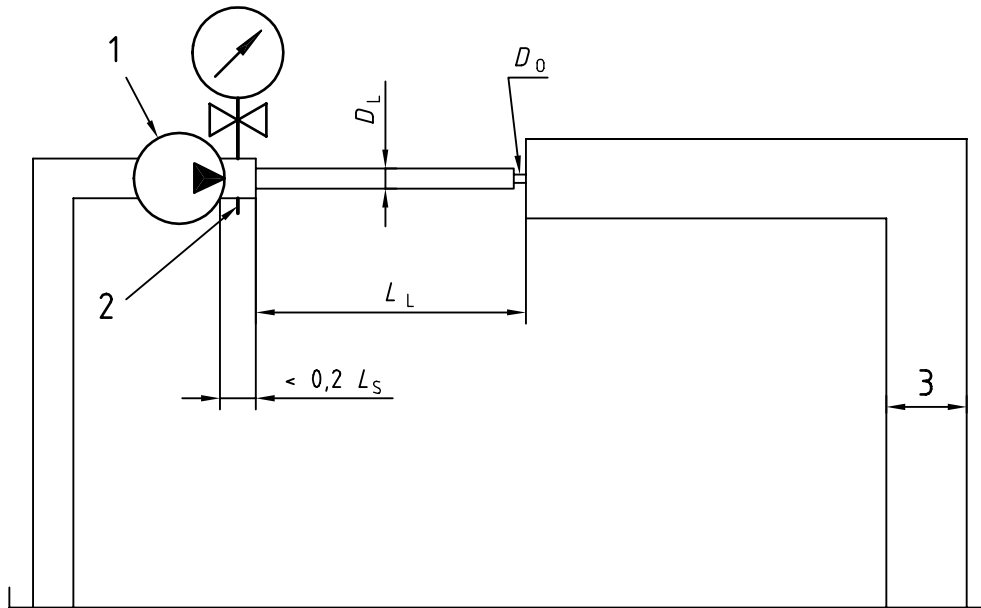
$f$	frequency, in hertz (Hz)
$j$	imaginary unit vector ( $\sqrt{-1}$ )
$P_B$	theoretical blocked pressure ripple amplitude
$P_E$	pressure ripple amplitude at the entrance to a test pipe
$p$	average pump outlet pressure
$p^*$	rated average pump outlet pressure
$Q_S$	pump flow ripple amplitude
$\Delta q(p^*)$	average pump flow loss at rated average outlet pressure
$\omega$	frequency, in radians per second (rad/s)
$x$	distance along a transmission line
$Z_E$	entry impedance of a transmission line with a termination impedance
$Z_0$	characteristic impedance of test pipe
$Z_{0S}$	characteristic impedance of pump outlet chamber
$Z_S$	pump internal impedance
$Z_T$	termination orifice impedance
$Z_{TS}$	termination leakage impedance of pump

NOTE See Table 1 for symbols not listed above.

### B.2 Description of the ISO 10767-2 test procedure

This part of ISO 10767 is based on the assumption that a short, small diameter (but standard size) steel tube and orifice can be connected to the pump outlet port that will allow the measured pressure ripple to be independent of the test circuit and only dependent upon the pressure ripple generation characteristics of the test pump. This will only be true when the combined impedance  $Z_E$  of the tube and orifice is large relative to the internal impedance  $Z_S$  of the test pump.

The recommended test circuit is shown schematically in Figure B.1.



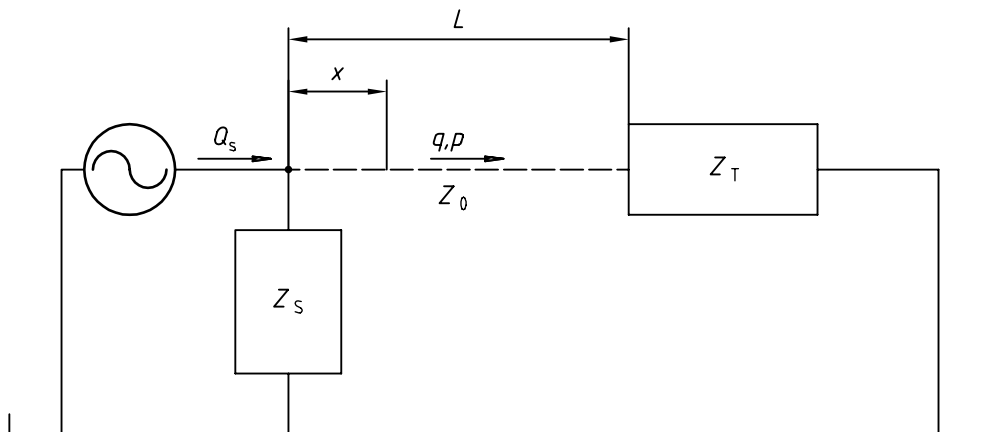
**Key**

- 1 Text pump
- 2 Piezoelectric pressure transducer
- 3 Inside diameter  $> 5D_L$

NOTE Pipe-line and orifice symbols are for illustrative purposes only and are not in accordance with ISO 1219-1.

**Figure B.1 — Schematic diagram of test circuit**

Figure B.2 shows the impedance representation proposed by Bowns, Edge and Tilley [1] of the hydraulic circuit shown in Figure B.1.



**Figure B.2 — Impedance representation of hydraulic circuit**

Distances  $x$  and  $L$  in Figure B.2 are intended to represent measurements along a transmission line with a characteristic impedance  $Z_0$  that is connected between the pump outlet port and a termination orifice  $Z_T$ . The internal impedance of the pump is represented by  $Z_S$ .

By differentiating the equation for pressure drop across an orifice it can be shown that the termination orifice impedance is given by equation (B.1):

$$Z_T = \frac{2p}{q} \quad (\text{B.1})$$

Equation (B.1) has been independently verified in tests performed by both Claar [2] and Theissen [3] on adjustable throttling valves at frequencies up to 450 Hz. McCandish, Edge and Tilley [4] have shown that the impedance of such a throttling valve can be lower than that described by equation (B.1) at high frequency, but it is felt that this effect was probably due to the volume chamber typically found at the entrance of such valves. Steps have been taken in this part of ISO 10767 to avoid such volume chambers at the entry to the termination orifice  $Z_T$ . With such precautions, equation (B.1) has been shown to be valid up to 4 kHz and suitable for pressure ripple measurements to that frequency.

Keller [5] defines the impedance of a hydraulic transmission line of length  $L_L$ , characteristic impedance  $Z_0$ , and termination impedance  $Z_T$  with equation (B.2):

$$Z_E = Z_0 \left[ \frac{Z_T \cos\left(\frac{\omega L_L}{c}\right) + j Z_0 \sin\left(\frac{\omega L_L}{c}\right)}{Z_0 \cos\left(\frac{\omega L_L}{c}\right) + j Z_T \sin\left(\frac{\omega L_L}{c}\right)} \right] \quad (\text{B.2})$$

If the pressure drop along the transmission line and the leakage from the line are assumed to be zero,  $Z_0$  can be calculated from equation (B.3):

$$Z_0 = \frac{4\rho c}{\pi D_L^2} \quad (\text{B.3})$$

Edge [6] has shown that the internal impedance of the pump  $Z_S$  behaves like a short transmission line and has the same form as equation (B.2). The pump internal impedance can be calculated using equation (B.4) if it is assumed that the pump characteristic impedance  $Z_{0S}$  is based on an apparent diameter  $D_S$  of the pump's discharge passageway, the transmission line length is based on the apparent length  $L_S$  of this passageway, and the termination impedance  $Z_{TS}$  is based on the ratio of the average pump outlet pressure to the average flow loss at that pressure (i.e. based on the pump's volumetric efficiency).

$$Z_S = Z_{0S} \left[ \frac{Z_{TS} \cos\left(\frac{\omega L_S}{c}\right) + j Z_{0S} \sin\left(\frac{\omega L_S}{c}\right)}{Z_{0S} \cos\left(\frac{\omega L_S}{c}\right) + j Z_{TS} \sin\left(\frac{\omega L_S}{c}\right)} \right] \quad (\text{B.4})$$

where

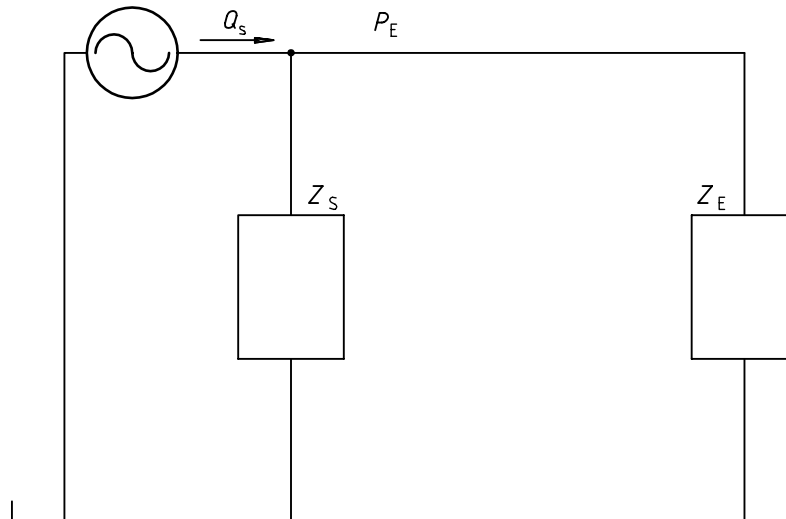
$$Z_{0S} = \frac{4\rho c}{\pi D_S^2} \quad (\text{B.5})$$

and

$$Z_{TS} = \frac{p^*}{\Delta q(p^*)} \quad (\text{B.6})$$

An impedance representation of this circuit that includes the transmission line effects can be drawn as shown in Figure B.3.





**Figure B.3 — Impedance representation of circuit including transmission line effects**

The pressure ripple at the outlet of the pump (i.e. at the entrance of the transmission line connected to the outlet) can be calculated using equation (B.7):

$$P_E = \frac{Q_S Z_S Z_E}{Z_S + Z_E} \quad (\text{B.7})$$

The product of  $Q_S Z_S$  is the pressure ripple that would be developed at the pump outlet port if  $Z_E$  was infinitely high (equivalent to blocking the outlet port). The ratio of the pressure ripple measured at the outlet of the pump  $P_E$  to the theoretical blocked pressure  $P_B$  can be obtained by rearranging equation (B.7):

$$\frac{P_E}{P_B} = \frac{Z_E}{Z_S + Z_E} \quad (\text{B.8})$$

where

$$P_B = Q_S Z_S \quad (\text{B.9})$$

The pressure ripple ratio  $P_E/P_B$  of equation (B.8) depends only on the relative complex values of the entry impedance of the transmission line connected to the pump outlet port  $Z_E$  and the pump internal impedance  $Z_S$ . If  $Z_E$  is much larger than  $Z_S$ , then the pressure ripple ratio is nearly equal to 1 (i.e. 0 dB) and the pressure ripple measured at the pump outlet port is nearly equal to the theoretical blocked pressure  $P_B$ . This condition where  $Z_E > Z_S$  will be subsequently referred to throughout the remainder of the annex as "low error". If we could obtain an independent measurement of  $Z_S$ , then the pump flow ripple  $Q_S$  could be calculated from equation (B.9).

These relationships in a typical pump circuit are shown graphically in Figure B.4.

In this circuit, the pipe inside diameter  $D_L$  is about 1,1 times the apparent diameter of the pump outlet port chamber  $D_S$  and the length  $L_L$  of this pipe is about 4,6 times the apparent length of the pump outlet chamber  $L_S$ . Such an outlet circuit would be common for typical customer installations of such a pump. There are two frequency ranges where the magnitude of the test circuit entry impedance  $Z_E$  is less than the pump impedance  $Z_S$ . These two ranges are from 0,02 kHz to 1,2 kHz and from 1,75 kHz to 2,25 kHz. In these ranges the measured pressure ripple error is very large. Even over the remainder of the frequency range where  $Z_E$  is larger than  $Z_S$ , it is not large enough to yield a low error.

If the outlet pipe is shortened to about  $2,7 L_S$  but with the same inside diameter, the critical frequency ranges are shifted to higher values, but the error remains high as shown in Figure B.5.

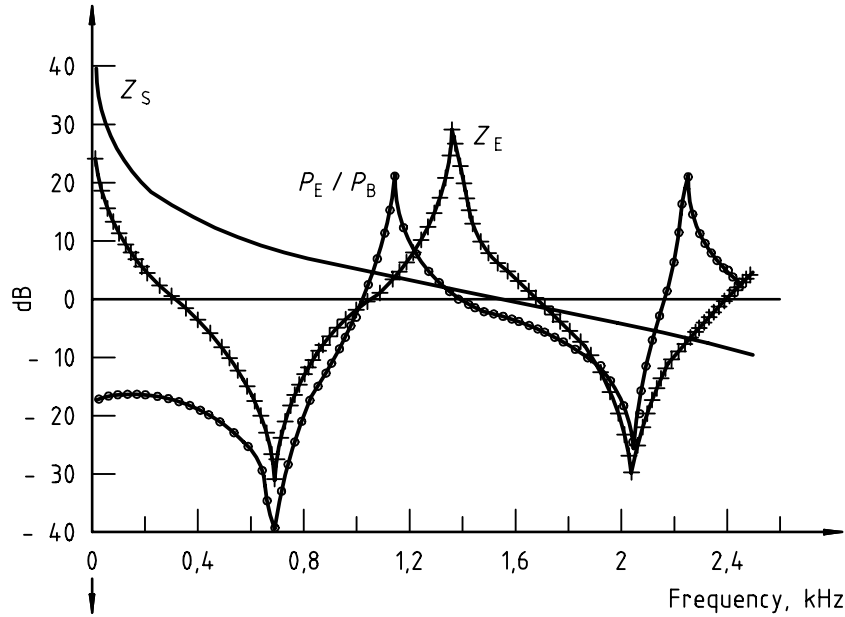


Figure B.4 — Effect of complex values of entry impedance on pressure ripple ratio

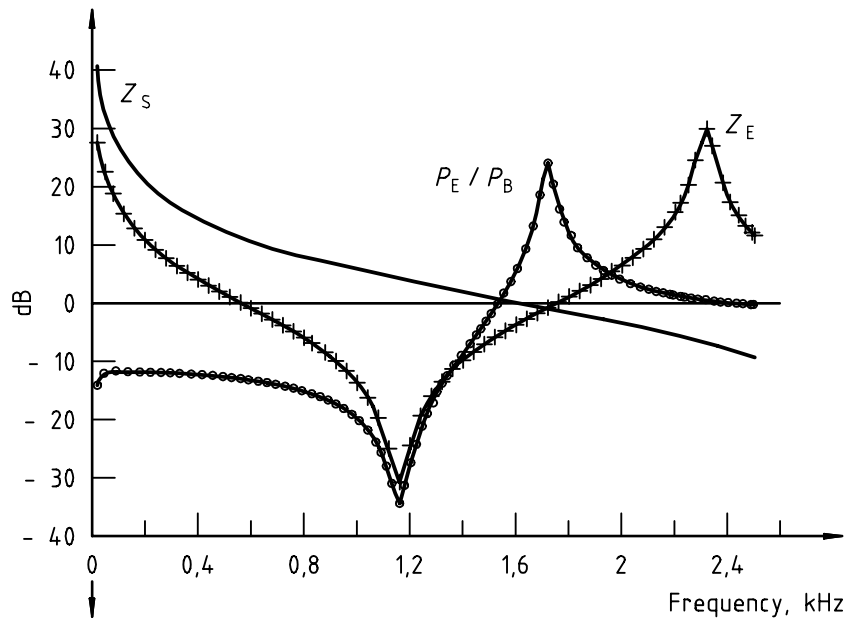
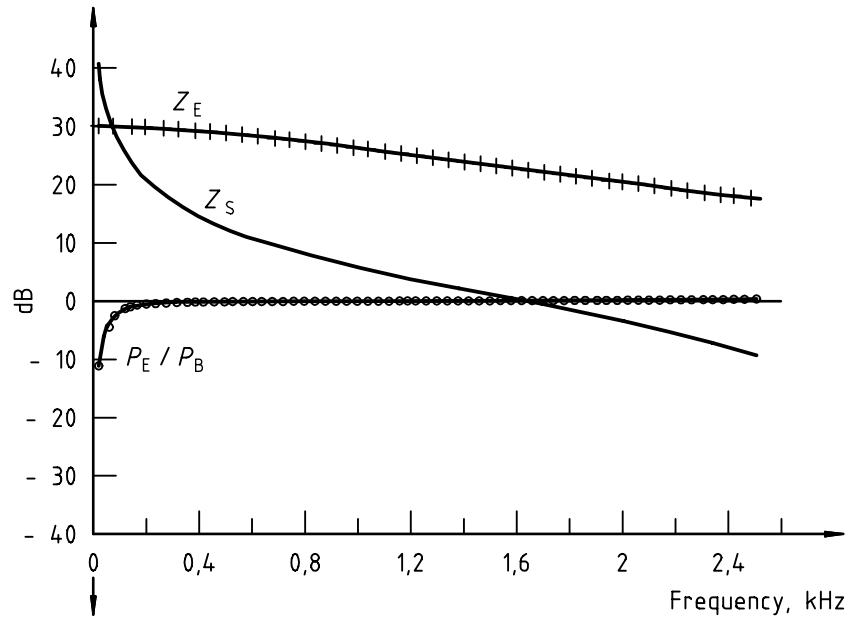


Figure B.5 — Effect of higher frequencies

By observing the trends in Figures B.4 and B.5, it is apparent that making the test pipe shorter makes the curves of  $Z_E$  and  $Z_S$  more nearly parallel. In fact, if  $L_L$  is made equal to  $L_S$ , the  $Z_E$  and  $Z_S$  curves will be nearly parallel with identical critical frequencies. Furthermore, if  $D_L = D_S$  and  $L_L = L_S$  then  $Z_E$  would have a similar shape and magnitude as  $Z_S$  at all frequencies. In this case, the shape of  $Z_E$  and  $Z_S$  would only differ by the magnitude of their respective termination impedances.

The form of equations (B.2) and (B.3) causes the magnitude of  $Z_E$  to be large relative to  $Z_S$  when the pipe inside diameter  $D_L$  is much smaller than  $D_S$ . Selecting a small diameter, short test pipe will therefore yield a test circuit with low error. Figure B.6 shows the effect of choosing a pipe of diameter where  $D_L = 0,28D_S$  and length  $L_L = 1,0L_S$ .

Figure B.6 shows that the difference between the pressure ripple measured at the pump outlet port and the theoretical blocked pressure ripple is very small from about 100 Hz up to the maximum value shown in the graph of 2,5 kHz.



**Figure B.6 — Comparison of measurements of pump outlet and blocked pressure ripple**

This is the principle used in this part of ISO 10767. The test pipe diameter is chosen in 9.5 so that its characteristic impedance  $Z_0$  is equal to the termination orifice impedance  $Z_T$  at the average pump outlet test pressure.

$$Z_0 = Z_T \quad (\text{B.10})$$

$$\frac{4\rho c}{\pi D_L^2} = \frac{2p}{q} \quad (\text{B.11})$$

$$D_L = \sqrt{\frac{2\rho c q}{\pi p}} \quad (\text{B.12})$$

The test procedure allows a range of pressures from  $p_{\min}$  to  $p_{\max}$  with a single pipe diameter. The equation in 9.5 uses  $(p_{\min} + p_{\max})/2$  as the pressure where  $Z_0 = Z_T$ . Substituting this average test pressure for  $p$  in equation (B.12) yields:

$$D_L = \sqrt{\frac{4\rho c q}{\pi (p_{\min} + p_{\max})}} \quad (\text{B.13})$$

Choosing the pipe diameter in this way has the effect of increasing the magnitude of  $Z_E$  relative to  $Z_S$  and keeping the variations of  $Z_E$  as a function of frequency relatively small. Figure B.7 is a graph of equation (B.13) for a range of pipe diameters  $D_L$  from 2 mm to 32 mm. The values used in Figure B.7 for the speed of sound  $c$  and fluid mass density  $\rho$  were 1 302 m/s and 908 kg/m<sup>3</sup> respectively.

The test pipe length is chosen in 9.6 so that the first anti-resonance of the test pipe coincides with the first anti-resonance of the pump internal impedance; that is where  $L_L = L_S$ . This makes the critical frequencies of  $Z_E$  and  $Z_S$  equal, reducing the number of times that these two curves can intersect and thereby reducing measurement error.

The minimum pressure  $p_{\min}$  of paragraph 8.2 is the pump outlet pressure below which the magnitude of the pressure ripple ratio of equation (B.8) is greater than  $-3$  dB at the fundamental pumping frequency  $f_1$ . Similarly, the upper frequency limit of  $f_{\max}$  in 8.3 is the frequency above which the magnitude of the pressure ripple ratio is greater than  $-3$  dB at a pump outlet pressure of  $p_{\min}$ . The derivations of the minimum pressure and maximum frequency equations are described in clause B.3.

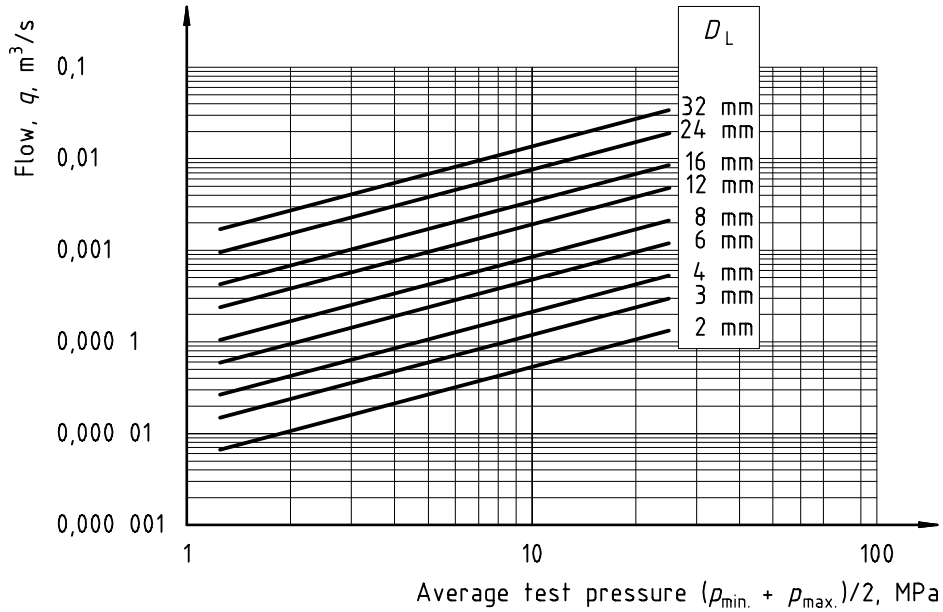


Figure B.7 — Flow vs. average test pressure for a range of pipe diameters

The root mean square (RMS) average pressure ripple as a function of the average pump outlet pressure for an axial piston pump tested according to an early version of this part of ISO 10767 is shown in Figure B.8. It displays the overall RMS average value of all of the harmonics of the measured pump pressure ripple from the fundamental frequency to 4 kHz. The two lines on this graph are for data taken at drive shaft speeds of 1 500 r/min and 1 800 r/min.

The spectral distribution of this pressure ripple data and knowledge of the pump internal impedance are theoretically all that is necessary to predict the pump pressure ripple in other defined impedance circuits.

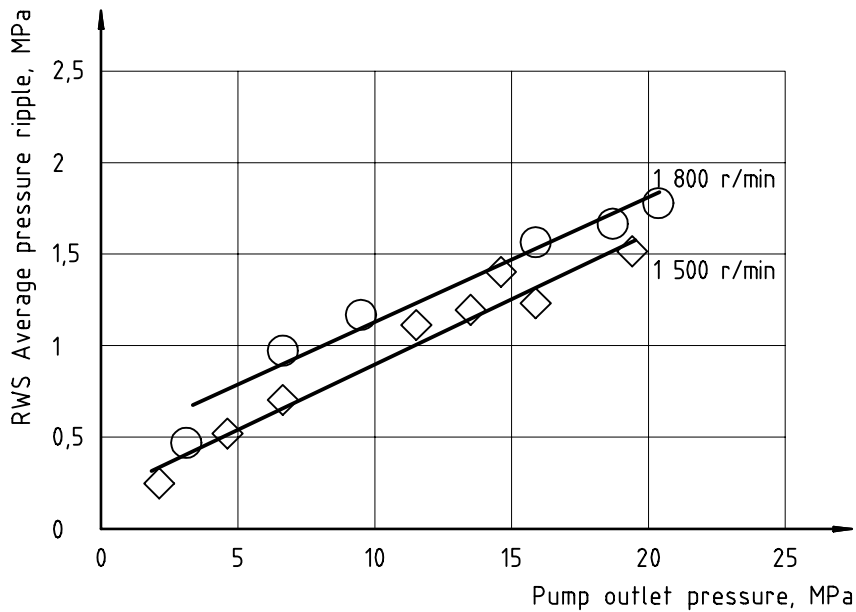


Figure B.8 — RMS average pressure ripple vs. pump outlet pressure

### B.3 Valid measurement range

The ratio of the pressure ripple measured at the outlet of the pump to the theoretical blocked pressure ripple from equation (B.8) is:

$$\left| \frac{P_E}{P_B} \right| = \frac{Z_E}{Z_E + Z_S} \quad (\text{B.14})$$

Allowing for a maximum – 3 dB error between the measured pressure ripple  $P_E$  and the blocked pressure ripple  $P_B$  yields:

$$\left| \frac{P_E}{P_B} \right| = \frac{1}{\sqrt{2}} \quad (\text{B.15})$$

Combining equations (B.14) and (B.15) yields:

$$\left| \frac{Z_E}{Z_E + Z_S} \right| = \frac{1}{\sqrt{2}} \quad (\text{B.16})$$

The entry impedance  $Z_E$  of a line terminated by an orifice is approximately equal to its termination impedance  $Z_T$  at frequencies near the line resonant frequency, when the line termination impedance  $Z_T$  is nearly equal to the transmission line characteristic impedance  $Z_0$ .

$$Z_E \approx \frac{2p}{q} \quad (\text{B.17})$$

The general equation for the pump internal impedance  $Z_S$  from equation (B.4) is:

$$Z_S = Z_{0S} \left[ \frac{Z_{TS} \cos\left(\frac{\omega LS}{c}\right) + j Z_{0S} \sin\left(\frac{\omega LS}{c}\right)}{Z_{0S} \cos\left(\frac{\omega LS}{c}\right) + j Z_{TS} \sin\left(\frac{\omega LS}{c}\right)} \right] \quad (\text{B.18})$$

If the volumetric efficiency of the pump is high (i.e. when  $Z_{TS} \gg Z_{0S}$ ). The pump impedance  $Z_S$  can then be simplified as follows:

$$Z_S = Z_{0S} \left[ \frac{\cos\left(\frac{\omega LS}{c}\right) + j \frac{Z_{0S}}{Z_{TS}} \sin\left(\frac{\omega LS}{c}\right)}{\frac{Z_{0S}}{Z_{TS}} \cos\left(\frac{\omega LS}{c}\right) + j \sin\left(\frac{\omega LS}{c}\right)} \right] \quad (\text{B.19})$$

$$Z_S = Z_{0S} \left[ \frac{\cos\left(\frac{\omega LS}{c}\right)}{j \sin\left(\frac{\omega LS}{c}\right)} \right] \quad (\text{B.20})$$

$$Z_S = \frac{4\rho c}{\pi D_S^2 j \tan\left(\frac{\omega LS}{c}\right)} \quad (\text{B.21})$$

Equation (B.21) for  $Z_S$  is a periodic function of frequency that reaches a maximum when:

$$\frac{\omega_{n,\max} LS}{c} = n\pi \quad (\text{B.22})$$

where

$$n = 0, 1, 2, 3, \dots, \infty$$

Solving equation (B.22) for frequency yields:

$$\omega_{n,\max} = \frac{n \pi c}{L_S} \tag{B.23}$$

It is slightly above and below these maximum value frequencies  $\omega_{n,\max}$  where the error is equal to  $-3$  dB. In order to calculate the pump outlet pressure where the error is equal to  $-3$  dB, equations (B.17) and (B.21) are substituted into equation (B.16).

$$\left| \frac{\frac{2p}{q}}{2p + \frac{4\rho c}{q} + \frac{\pi D_S^2 j \tan\left(\frac{\omega L_S}{c}\right)}{q}} \right| = \frac{1}{\sqrt{2}} \tag{B.24}$$

$$\frac{\sqrt{\left(\frac{2p}{q}\right)^2}}{\sqrt{\left(\frac{2p}{q}\right)^2 + \left(\frac{4\rho c}{\pi D_S^2 \tan\left(\frac{\omega L_S}{c}\right)}\right)^2}} = \frac{1}{\sqrt{2}} \tag{B.25}$$

$$\frac{\left(\frac{2p}{q}\right)^2}{\left(\frac{2p}{q}\right)^2 + \left(\frac{4\rho c}{\pi D_S^2 \tan\left(\frac{\omega L_S}{c}\right)}\right)^2} = \frac{1}{2} \tag{B.26}$$

$$\left(\frac{2p}{q}\right)^2 = \left(\frac{4\rho c}{\pi D_S^2 \tan\left(\frac{\omega L_S}{c}\right)}\right)^2 \tag{B.27}$$

$$\frac{2p}{q} = \frac{4\rho c}{\pi D_S^2 \tan\left(\frac{\omega L_S}{c}\right)} \tag{B.28}$$

$$p = \frac{2\rho c q}{\pi D_S^2 \tan\left(\frac{\omega L_S}{c}\right)} \tag{B.29}$$

At the fundamental pumping frequency  $f_1$ , the minimum pump outlet test pressure for a  $-3$  dB difference between the measured pressure ripple and the blocked pressure ripple is:

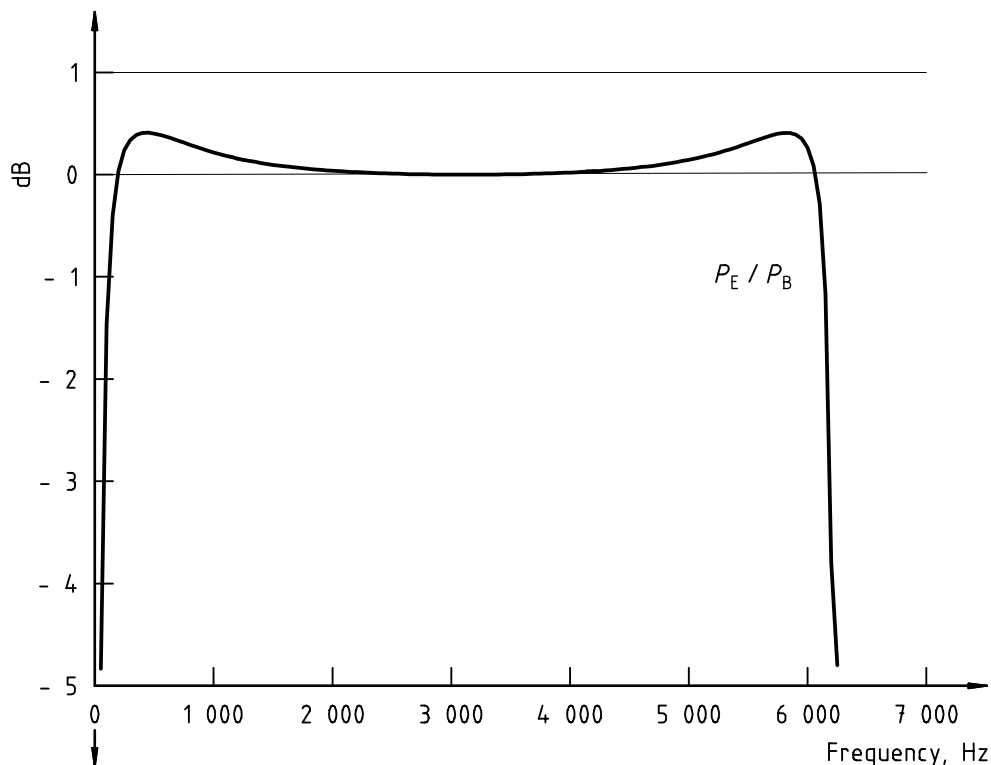
$$p_{\min} = \frac{2\rho c q}{\pi D_S^2 \tan\left(\frac{2\pi f_1 L_S}{c}\right)} \tag{B.30}$$

At any pump outlet pressure greater than or equal to  $p_{\min}$ , the error remains less than  $-3$  dB from  $f_1$  up to a frequency slightly below the second resonant frequency of the pump internal impedance. This is the next higher frequency above  $f_1$  where the difference between the measured pressure ripple again differs from the blocked pressure ripple by more than  $-3$  dB. This maximum frequency  $f_{\max}$  is below the second resonant frequency of the pump internal impedance by an amount equal to  $f_1$  and can be calculated with equation (B.31).

$$f_{\max} = \left( \frac{c}{2L_S} \right) - f_1 \quad (\text{B.31})$$

Pressure ripple measurements over the pump outlet pressure range from  $p_{\min}$  to  $p_{\max}$  and over the frequency range from  $f_1$  to  $f_{\max}$  will yield values that are equal to the theoretical blocked pressure ripple with a maximum negative error of  $-3$  dB. A small positive error is also possible at pump outlet pressures below  $p_{\max}/2$ . Based on numerical simulations of the test procedure, the positive error is limited to about  $+1$  dB. The general form of the ratio of the measured pressure ripple to the theoretical blocked pressure ripple for this part of ISO 10767 is shown as a function of frequency in Figure B.9.

The maximum positive error is reduced to  $0$  dB when the test pressure is equal to or greater than  $p_{\max}/2$ . The maximum total error is therefore, between  $0$  dB to  $-3$  dB at test pressures equal to or greater than  $p_{\max}/2$  and between  $+1$  dB to  $-3$  dB at pressures less than  $p_{\max}/2$ .



**Figure B.9 — Form of ratio of measured pressure ripple to blocked pressure ripple**

## Bibliography

- [1] BOWNS, D.E., EDGE, K.A. and TILLEY, D.G. *The Assessment of Pump Fluid Borne Noise*. The Institution of Mechanical Engineers Conference: "Quiet Oil Hydraulic Systems — Where are we now?" London, England, November 1997.
- [2] CLAAR, L.M. Vickers Development Laboratory Report C-3907: *The Impedance of a Throttling Valve to High Frequency, Pump Generated, Flow Ripple*. Troy, Michigan, 16 April 1982.
- [3] THEISSEN, H. and RISKEN, W. *Messung der Volumenstrompulsation von Hydraulikpumpen*. o+p ölhydraulik und pneumatik #27 (1983) Nr.5, pp. 387-392.
- [4] McCANDISH, D., EDGE, K.A. and TILLEY, D.G. *Fluid Noise Generated by Positive Displacement Pumps*. Institute of Mechanical Engineers Research Project Seminar on Quiet Oil Hydraulic Systems Paper C265/77. London, England, 1977.
- [5] KELLER, GEORGE R. *Hydraulic Systems Analysis*, Chapter 5: Transmission Lines — Unsteady Flow. Industrial Publishing Company, Cleveland Ohio, 1969.
- [6] EDGE, K.A. *The Theoretical Prediction of the Impedance of Positive Displacement Pumps*. The Institution of Mechanical Engineers, Seminar on Quieter Oil Hydraulics. London, England, 1980.
- [7] ANSI/NFPA T 2.7.2:1995, *Hydraulic fluid power — Pumps — Determination of fluid pressure fluctuation characteristics*.





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