# INTERNATIONAL **STANDARD**

First edition 2006-10-01

## **Road vehicles — Road load —**

Part 1: **Determination under reference atmospheric conditions** 

*Véhicules routiers — Résistance sur route —* 

*Partie 1: Détermination dans les conditions atmosphériques de référence* 



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## **Foreword**

ISO (the International Organization for Standardization) is a worldwide federation of national standards bodies (ISO member bodies). The work of preparing International Standards is normally carried out through ISO technical committees. Each member body interested in a subject for which a technical committee has been established has the right to be represented on that committee. International organizations, governmental and non-governmental, in liaison with ISO, also take part in the work. ISO collaborates closely with the International Electrotechnical Commission (IEC) on all matters of electrotechnical standardization.

International Standards are drafted in accordance with the rules given in the ISO/IEC Directives, Part 2.

The main task of technical committees is to prepare International Standards. Draft International Standards adopted by the technical committees are circulated to the member bodies for voting. Publication as an International Standard requires approval by at least 75 % of the member bodies casting a vote.

Attention is drawn to the possibility that some of the elements of this document may be the subject of patent rights. ISO shall not be held responsible for identifying any or all such patent rights.

ISO 10521-1 was prepared by Technical Committee ISO/TC 22, *Road vehicles*, Subcommittee SC 5, *Engine tests*.

This first edition, together with ISO 10521-2, cancels and replaces ISO 10521:1992, which has been technically revised.

ISO 10521 consists of the following parts, under the general title *Road vehicles — Road load*:

⎯ *Part 1: Determination under reference atmospheric conditions* 

⎯ *Part 2: Reproduction on chassis dynamometer* 

## **Introduction**

It is known that wind gives much influence to vehicle road-load measurement on test roads. Therefore, no international standards or national standards/regulations allowed conducting on-road tests under windy (e.g. 3 m/s or more) conditions in terms of measurement accuracy. In this standard, wind effect correction methodology is newly introduced into the conventional coastdown method and torquemeter method, and it offers wider (up to wind speed of 10 m/s) opportunity of on-road tests. In addition, more realistic road load can be simulated even under lower wind conditions.

This part of ISO 10521 also adopts the off-road road-load measurement method as the comparable alternative. The method is based on the separation of the total road load into two components, aerodynamic drag and rolling resistance, where the former is measured in a wind tunnel and the latter with a chassis dynamometer. This alternative enables the standard users to carry out road-load measurement regardless of atmospheric conditions or other requirements necessary for the on-road test. It is not the scope of this standard to define all requirements of wind-tunnel design or test practice. Nevertheless, the standard users are encouraged to conduct the measurement with state-of-the-art wind-tunnel technologies and to respect the highest quality management standards such as ISO 17025, so as to secure the measurement reliability and repeatability.

In view of accessibility of the standard, International Standard ISO 10521 is divided into two parts in this second edition in order to provide two separate standards for the two different technical aspects, determination of road load and reproduction of road load on chassis dynamometer.

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## **Road vehicles — Road load —**

## Part 1: **Determination under reference atmospheric conditions**

## **1 Scope**

This part of ISO 10521 specifies methods of determining the road load of road vehicles for subsequent test purposes, for example, fuel consumption tests or exhaust emission measurements. This determines the road load of a vehicle running on a level road under reference atmospheric conditions. It is achieved by either the coastdown method, the torquemeter method or the wind-tunnel/chassis-dynamometer method.

This part of ISO 10521 is applicable to motor vehicles, as defined in ISO 3833, up to a gross vehicle mass of 3 500 kg.

## **2 Normative references**

The following referenced documents are indispensable for the application of this document. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies.

ISO 3833, *Road vehicles — Types — Terms and definitions*

## **3 Terms and definitions**

For the purposes of this document, the terms and definitions given in ISO 3833 and the following apply.

#### **3.1**

#### **total resistance**

total force-resisting movement of a vehicle, measured either by the coastdown method or by the windtunnel/chassis-dynamometer method, including the friction forces in the drive-train

## **3.2**

#### **running resistance**

torque-resisting movement of a vehicle, measured by the torquemeter installed in the drive-train of a vehicle, including the friction torque in the drive-train downstream of the torquemeter

#### **3.3**

#### **road load**

general meaning of the force or torque which opposes the movement of a vehicle, including total resistance and/or running resistance

#### **3.4**

#### **aerodynamic drag**

resistance of the air to the motion of a vehicle

## **3.5**

#### **rolling resistance**

opposing force in the drive-train, axles and tyres to the motion of a vehicle

## **3.6**

### **reference speed**

a vehicle speed at which a chassis-dynamometer load is verified

### **3.7**

### **reference atmospheric conditions**

atmospheric conditions of the following values, to which the road-load measurement results are corrected:

- a) atmospheric pressure: *p0* = 100 kPa, unless otherwise specified by regulations;
- b) atmospheric temperature: *t <sup>0</sup>* = 293 K, unless otherwise specified by regulations;
- c) dry air density:  $\rho_0$  = 1,189 kg/m<sup>3</sup>, unless otherwise specified by regulations;
- d) wind speed: 0 m/s.

## **3.8**

## **stationary anemometry**

measurement of wind speed and direction with an anemometer at a location and height above road level alongside the test road where the most representative wind conditions will be experienced

## **3.9**

## **onboard anemometry**

measurement of wind speed and direction with an anemometer appropriately installed to the test vehicle

## **3.10**

## **wind correction**

correction of the effect of wind on road load, which is achieved either by stationary or by onboard anemometry

## **3.11**

## **aerodynamic stagnation point**

point on the surface of a vehicle where the wind velocity is equal to zero

## **4 Required overall measurement accuracy**

The required overall measurement accuracy shall be as follows:

- a) vehicle speed:  $\pm$  0,5 km/h or  $\pm$  1 %, whichever is greater;
- b) time:  $\pm$  50 ms or  $\pm$  0,1 %, whichever is greater;
- c) wheel torque:  $\pm 3$  N·m or  $\pm 0.5$  %, whichever is greater;
- d) wind speed:  $\pm$  0,3 m/s;
- e) wind direction:  $\pm 3^{\circ}$ ;
- f) atmospheric temperature:  $\pm$  1 K;
- g) atmospheric pressure:  $\pm$  0,3 kPa;
- h) vehicle mass:  $\pm$  10 kg;
- i) tyre pressure:  $\pm$  5 kPa;
- j) product of aerodynamic coefficient and frontal projected area  $(SCd): \pm 2\%$ ;
- k) chassis-dynamometer roller speed:  $\pm$  0,5 km/h or  $\pm$  1 %, whichever is greater;
- l) chassis-dynamometer force:

Category 1 chassis dynamometer:  $\pm$  6 N, or

Category 2 chassis dynamometer:  $\pm$  10 N or  $\pm$  0,1 % of full scale, whichever is greater.

NOTE The Category 2 chassis dynamometer usually has a greater load capacity, e.g. 130 kW or more.

## **5 Road-load measurement on road**

#### **5.1 Requirements for road test**

#### **5.1.1 Atmospheric conditions for road test**

#### **5.1.1.1 Wind**

The average wind speed over the test road shall not exceed 10 m/s, nor wind gusts exceed 14 m/s. Relevant wind correction shall be conducted according to the applicable type of anemometry specified in Table 1. In order to decide the applicability of each anemometry type, the average wind speed shall be determined by continuous wind speed measurement, using a recognized meteorological instrument, at a location and height above the road level alongside the test road where the most representative wind conditions will be experienced. --`,,```,,,,````-`-`,,`,,`,`,,`---

NOTE Wind correction may be waived when the average wind speed is 3 m/s or less.

#### **Table 1 — Applicable anemometry depending on average wind speed and cross-wind component**

Wind speed in metres per second (m/s)



#### **5.1.1.2 Atmospheric temperature**

The atmospheric temperature shall be within the range of 274 to 308 K, inclusive.

#### **5.1.2 Test road**

The road surface shall be flat, dry and hard, and its texture and composition shall be representative of current urban and highway road surfaces. The test-road longitudinal slope shall not exceed  $\pm$  1 %. The local

inclination between any points 3 m apart shall not deviate more than  $\pm$  0,5 % from this longitudinal slope. The maximum cross-sectional camber of the test road shall be 1,5 %.

## **5.2 Preparation for road test**

## **5.2.1 Vehicle preparation**

## **5.2.1.1 Vehicle condition**

The test vehicle shall be suitably run-in for the purpose of the subsequent test. The tyres shall be suitably broken-in for the purpose of the subsequent test, while still having a tread depth of not less than 50 % of the initial tread depth.

Unless any particular purpose is intended, the vehicle shall be in normal vehicle conditions, as specified by the manufacturer. That is, tyre pressure (see 5.2.1.2), wheel alignment, vehicle height, lubricants in the drivetrain and wheel-bearings, and brake adjustment to avoid unrepresentative parasitic drag.

During the road test, the engine bonnet/hood and all windows shall be closed so that they will not influence the road-load measurement. Any covers of the air ventilation system, headlamps, etc., shall be closed, and the air-conditioning switched off.

The vehicle mass shall be adjusted to meet the requirement of the intended subsequent test, including the mass of the driver and instruments.

## **5.2.1.2 Tyre-pressure adjustment**

If the difference between the ambient and soak temperature is more than 5 K, the tyre pressure shall be adjusted as follows.

Soak the tyres for more than 4 h at 10 % above the target pressure. Just before testing, reduce the pressure down to the manufacturer's recommended inflation pressure, adjusted for difference between the soakingenvironment temperature and the ambient test temperature at a rate of 0,8 kPa per 1 K using the following formula:

$$
\Delta P_t = 0.8 \times (T_{\text{soak}} - T_{\text{amb}})
$$

where

 $Δ$   $P_t$ is the tyre pressure adjustment, in kilopascals (kPa);

0.8 is the pressure adjustment factor, in kilopascals per kelvin (kPa/K);

 $T_{\text{soak}}$  is the tyre-soaking temperature, in kelvins (K);

 $T_{amb}$  is the test ambient temperature, in kelvins (K).

## **5.2.2 Installation of instruments**

Any instruments, especially for those installed outside the vehicle, shall be installed on the vehicle in such a manner as to minimize effects on the operating characteristics of the vehicle.

## **5.2.3 Vehicle preconditioning**

Prior to the test, the vehicle shall be preconditioned appropriately, until stabilized and normal vehicle operating temperatures have been reached. It is recommended that the vehicle should be driven at the most appropriate reference speed for a period of 30 min. During this preconditioning period, the vehicle speed shall not exceed the highest reference speed.

## **5.3 Measurement of total resistance by coastdown method**

The total resistance shall be determined by either the multi-segment method (5.3.1), the average deceleration method (5.3.2) or the direct regression method (5.3.3).

#### **5.3.1 Multi-segment method**

#### **5.3.1.1 Selection of speed points for road-load curve determination**

In order to obtain a road-load curve as a function of vehicle speed, a minimum of four speed points,  $V_j$  ( $j$  = 1, 2, etc.) shall be selected. The highest speed point shall not be lower than the highest reference speed, and the lowest speed point shall not be higher than the lowest reference speed. The interval between each speed point shall not be greater than 20 km/h.

#### **5.3.1.2 Data collection**

During the test, a) and b) shall be measured and recorded at a maximum of 0,2 s intervals, and c) and d) at a maximum of 1,0 s intervals.

- a) elapsed time;
- b) vehicle speed;
- c) wind speed;
- d) wind direction.

NOTE The wind speed and the wind direction are measured by the stationary anemometry.

#### **5.3.1.3 Vehicle coastdown**

**5.3.1.3.1** Following preconditioning, and immediately prior to each test measurement, drive the vehicle at the highest reference speed for, at most, 1 min, if necessary. Then accelerate the vehicle to 5 km/h more than the speed at which the coastdown time measurement begins  $(V_i + \Delta V)$  and begin the coastdown immediately.

**5.3.1.3.2** During coastdown, the transmission shall be in neutral, and the engine shall run at idle. In the case of vehicles with manual transmission, the clutch shall be engaged. Movement of steering-wheel shall be avoided as much as possible, and the vehicle brakes shall not be operated until the end of the coastdown.

**5.3.1.3.3** Repeat the test, taking care to begin the coastdown at the same speed and preconditions.

**5.3.1.3.4** Although it is recommended that each coastdown run be performed without interruption, split runs are permitted if data cannot be collected in a continuous fashion for the entire speed range. For split runs, care shall be taken so that the vehicle condition be constant as much as possible at each split point.

#### **5.3.1.4 Determination of total resistance by coastdown time measurement**

**5.3.1.4.1** Measure the coastdown time corresponding to the speed  $V_j$  as the elapsed time from the vehicle speed  $(V_i + \Delta V)$  to  $(V_i - \Delta V)$ . It is recommended that  $\Delta V$  be 10 km/h when the vehicle speed is more than 60 km/h, and 5 km/h when the vehicle speed is 60 km/h or less.

**5.3.1.4.2** Carry out these measurements in both directions until a minimum of three consecutive pairs of figures have been obtained which satisfy the statistical accuracy *p*, in percent, defined below.

$$
p = \frac{ts}{\sqrt{n}} \times \frac{100}{\Delta T_j} \le 3\%
$$

where

- *n* is the number of pairs of measurements;
- ∆ $T_j$  is the mean coastdown time at speed  $V_j$ , in seconds (s), given by the formula:

$$
\Delta T_j = \frac{1}{n} \sum_{i=1}^n \Delta T_{ji}
$$

in which

∆*Tji* is the harmonized average coastdown time of the *i*th pair of measurements at speed *Vj* , in seconds (s) given by the formula:

$$
\Delta T_{ji} = \frac{2}{\left(\sqrt[4]{\Delta T_{jai}}\right) + \left(\sqrt[4]{\Delta T_{jbi}}\right)}
$$

and in which

∆*T<sub>jai</sub>* and ∆*T<sub>jbi</sub>* are the coastdown times of the *i*<sup>th</sup> measurement at speed *V<sub>j</sub>* in each direction, respectively, in seconds (s);

*s* is the standard deviation, in seconds (s), defined by the formula:

$$
s = \sqrt{\frac{1}{n-1} \sum_{i=1}^{n} (\Delta T_{ji} - \Delta T_j)^2}
$$



is the coefficient given in Table 2.





**5.3.1.4.3** If, during a measurement in one direction, the driver is forced to change the vehicle direction sharply, this measurement and the paired measurement in the opposite direction shall be rejected.

**5.3.1.4.4** The total resistances,  $F_{j\mathbf{a}}$  and  $F_{j\mathbf{b}}$  at speed  $V_j$  in each direction, in newtons, are determined by the formulae:

$$
F_{j\text{a}} = -\frac{1}{3.6} \times (m + m_{\text{r}}) \times \frac{2 \times \Delta V}{\Delta T_{j\text{a}}}
$$

$$
F_{j\text{b}} = -\frac{1}{3.6} \times (m + m_{\text{r}}) \times \frac{2 \times \Delta V}{\Delta T_{j\text{b}}}
$$

where

- *m* is the test vehicle mass including the driver and instruments, in kilograms (kg);
- $m_r$  is the equivalent effective mass of all the wheels and vehicle components rotating with the wheels during coastdown on the road, in kilograms (kg); *m*<sup>r</sup> should be measured or calculated by an appropriate technique. As an alternative, *m*<sup>r</sup> may be estimated as 3 % of the unladen vehicle mass;
- ∆*T<sub>ja</sub>* and ∆*T<sub>jb</sub>* are the mean coastdown times in each direction, respectively, corresponding to speed *V<sub>j</sub>*, in seconds (s), given by the formulae:

$$
\Delta T_{j\mathbf{a}} = \frac{1}{n} \sum_{i=1}^{n} \Delta T_{j\mathbf{a}i}
$$

$$
\Delta T_{j\mathbf{b}} = \frac{1}{n} \sum_{i=1}^{n} \Delta T_{j\mathbf{b}i}
$$

1

*i*

**5.3.1.4.5** The total-resistance curve shall be determined as follows. Fit the following regression curve to the data sets  $(V_j, F_{j\mathbf{a}})$  and  $(V_j, F_{j\mathbf{b}})$  corresponding to all the speed points  $V_j$  (*j* = 1, 2, etc.) and direction (a, b) to determine  $f'_0$ ,  $f'_1$  and  $f_2$ :

$$
F_{a} = f_{0a} + f_{1a}V + f_{2a}V^{2}
$$

$$
F_{b} = f_{0b} + f_{1b}V + f_{2b}V^{2}
$$

where

- $F_a$  and  $F_b$  are the total resistances in each direction, in newtons (N);
- $f_{0a}$  and  $f_{0b}$  are the constant terms in each direction, in newtons (N);
- $f_{1a}$  and  $f_{1b}$  are the coefficients of the first-order term of the vehicle speed in each direction, in newtons hour per kilometre (N·h/km); *f* 1 may be assumed to be zero, if the value of *f <sup>1</sup>V* is no greater than 3 % of *F* at the reference speed(s); in this case, the coefficients  $f_0$  and  $f_2$  shall be recalculated;
- $f_{2a}$  and  $f_{2b}$  are the coefficients of the second-order term of the vehicle speed in each direction, in newtons hour squared per kilometre squared [(N⋅(h/km)2];
- $V$  is the vehicle speed, in kilometres per hour  $(km/h)$ .

Then calculate the coefficients  $f_0, f_1$  and  $f_2$  in the total-resistance equation using the following formulae:

$$
f_0 = \frac{f_{0a} + f_{0b}}{2}
$$

$$
f_1 = \frac{f_{1a} + f_{1b}}{2}
$$

$$
f_2 = \frac{f_{2a} + f_{2b}}{2}
$$

where  $f_0, f_1$  and  $f_2$  are the average coefficients in the following average total-resistance equation:

$$
F_{\text{avg}} = f_0 + f_1 V + f_2 V^2
$$

and in which  $F_{avg}$  is the average total resistance, in newtons (N).

NOTE As a simple alternative to the above calculation, the following formula may be applied to compute the average total resistance, where the harmonized average of the alternate coastdown time is used instead of the average of alternate total resistance.

$$
F_j = -\frac{1}{3.6} \times (m + m_r) \times \frac{2 \times \Delta V}{\Delta T_j}
$$

where ∆*Tj* is the harmonized average of alternate coastdown time measurements at speed *Vj* , in seconds (s), given by the formula:

$$
\Delta T_j = \frac{2}{\left(\sqrt[4]{\Delta T_{j\mathbf{a}}}\right) + \left(\sqrt[4]{\Delta T_{j\mathbf{b}}}\right)}
$$

and in which ∆ $T_{j{\sf a}}$  and ∆ $T_{j{\sf b}}$  are the coastdown time at speed  $V_j$  in each direction, respectively, in seconds (s).

Then, calculate the coefficients  $f_0$ ,  $f_1$  and  $f_2$  in the total-resistance equation with the regression analysis.

## **5.3.2 Average deceleration method**

As an alternative to the determination in 5.3.1, the total resistance may also be determined by the procedures described in 5.3.2.1 to 5.3.2.4.

#### **5.3.2.1 Selection of speed points for road-load curve determination**

Speed points shall be selected as specified in 5.3.1.1.

#### **5.3.2.2 Data collection**

Data shall be measured and recorded as specified in 5.3.1.2.

## **5.3.2.3 Vehicle coastdown**

Vehicle coastdown shall be conducted as specified in 5.3.1.3.

#### **5.3.2.4 Determination of total resistance by coastdown measurement**

**5.3.2.4.1** • Record the speed-versus-time data during coastdown from vehicle speed  $(V_j + \Delta V)$  to  $(V_j - \Delta V)$ , where ∆*V* is more than 10 km/h.

**5.3.2.4.2** Fit the following function to the group of data by polynomial regression to determine the coefficients  $A_0$ ,  $A_1$ ,  $A_2$  and  $A_3$ :

$$
V_{a}(t) = A_{0a} + A_{1a}t + A_{2a}t^{2} + A_{3a}t^{3}
$$

$$
V_{b}(t) = A_{0b} + A_{1b}t + A_{2b}t^{2} + A_{3b}t^{3}
$$

where

 $V_a(t)$ ,  $V_b(t)$  is the vehicle speed, in kilometres per hour (km/h);

*t* is the time, in seconds (s);

 $A_{0a}$ ,  $A_{1a}$ ,  $A_{2a}$ ,  $A_{3a}$ ,  $A_{0b}$ ,  $A_{1b}$ ,  $A_{2b}$  and  $A_{3b}$  are the coefficients.

**5.3.2.4.3** Determine the deceleration,  $\gamma_j$ , in metres per second squared, at the speed  $V_j$  as follows:

$$
\gamma_j = \frac{1}{3,6} \times \left( A_1 + 2 \times A_2 t_j + 3 \times A_3 t_j^2 \right)
$$

where  $t_j$  is the time at which the vehicle speed given by the function in 5.3.2.4.2 is equal to  $V_j^{\cdot}$ .

**5.3.2.4.4** Repeat the measurements in both directions, until a minimum of four consecutive pairs of the data have been obtained which satisfy the statistical accuracy *p*, in percent, below. The validity of the data shall be decided in accordance with 5.3.1.4.3.

$$
p = \frac{ts}{\sqrt{n}} \times \frac{100}{\Gamma_j} \le 3\%
$$

where

- *n* is the number of pairs of measurements;
- $\Gamma_j$  is the mean average deceleration at the speed  $V_j$ , in metres per second squared (m/s<sup>2</sup>), given by the formula:

$$
\Gamma_j = \frac{1}{n} \sum_{i=1}^n \Gamma_{ji}
$$

in which

$$
\Gamma_j = \frac{1}{2} \times (\gamma_{jai} + \gamma_{jbi})
$$

and in which

$$
\gamma_{jai} \text{ and } \gamma_{jbi}
$$

are the decelerations of the *i*th measurement at the speed  $V_j$  defined in 5.3.2.4.3 for each direction, respectively, in metres per second squared  $(m/s<sup>2</sup>)$ ;

*s* is the standard deviation, in metres per second squared (m/s<sup>2</sup>), defined by the formula:

$$
s = \sqrt{\frac{1}{n-1} \sum_{i=1}^{n} (F_{ji} - F_j)^2}
$$

*t* is the coefficient given in Table 2.

**5.3.2.4.5** Determine the total resistance  $F_j$  at the speed  $V_j$  by the following formula, using m and  $m_r$  as defined in 5.3.1.4.4.

 $F_j = (m+m_\text{r})\Gamma_j$ 

#### **5.3.2.4.6 Total-resistance curve determination**

Determine the total-resistance curve as specified in 5.3.1.4.5.

#### **5.3.3 Direct regression method**

As an alternative to the determination in 5.3.1.4.5, the total resistance may also be determined by the following mathematical approach.

#### **5.3.3.1 Selection of speed range for road-load curve determination**

The test speed range (i.e. the maximum speed and the minimum speed) shall be so determined that it covers the range of the reference speeds, over which total resistance is measured. If the test is carried out in a manner of split runs, each split speed range shall be determined accordingly.

## **5.3.3.2 Data collection**

Data shall be measured and recorded as specified 5.3.1.2.

#### **5.3.3.3 Vehicle coastdown**

Vehicle coastdown shall be conducted as specified in 5.3.1.3.

## **5.3.3.4 Determination of total resistance by coastdown measurement**

The coefficients  $f_0, f_1$  and  $f_2$  shall be calculated by approximating the relation between *V* and *t* to tangent with Equation (4), of which the mathematical process is as follows.

**5.3.3.4.1** Express *F* using Formulae (1) and (2):

$$
F = f_0 + f_1 V + f_2 V^2 \tag{1}
$$

$$
F = -\frac{1}{3.6} \times (m + m_{\rm r}) \times \frac{\mathrm{d}V}{\mathrm{d}t} \tag{2}
$$

where

- *F* is the total resistance, in newtons (N);
- *f* is the constant term, in newtons  $(N)$ ;
- *f* is the coefficient of the first-order term, in newtons hour per kilometre [N⋅(h/km)];
- *f* is the coefficient of the second-order term, in newtons hour squared per kilometre squared  $[N-(h/km)^2]$ ;
- *m* is the test vehicle mass including the driver and instruments, in kilograms (kg);
- $m_r$  is the equivalent effective mass of all the wheels and vehicle components rotating with the wheels during coastdown on the road, in kilograms (kg); *m<sup>r</sup>* should be measured or calculated by an appropriate technique; as an alternative,  $m_{\text{r}}$  may be estimated as 3 % of the unladen vehicle mass;
- $V$  is the vehicle speed, in kilometres per hour (km/h).

**5.3.3.4.2** Equation (3) is derived from Equations (1) and (2).

$$
-\frac{3.6 \times dt}{m + m_{\rm r}} = \frac{dV}{f_0 + f_1 V + f_2 V^2}
$$
(3)

**5.3.3.4.3** Yield Equation (4) from Equation (3).

$$
V = \frac{\sqrt{4 \times f_0 f_2 - f_1^2}}{2 \times f_2} \tan \left( -\frac{3.6 \times \sqrt{4 \times f_0 f_2 - f_1^2}}{2 \times (m + m_r)} \times t - C_0 \right) - \frac{f_1}{2 \times f_2}
$$
(4)

where

- *t* is the time, in seconds (s);
- $C_0$  is the integration constant.

**5.3.3.4.4** Replace Equation (4) with (5).

$$
V = A \tan(Bt + C) + D \tag{5}
$$

**5.3.3.4.5** Calculate *A*, *B*, *C* and *D* in the approximate Equation (5) by the least-squares method, and then determine the coefficients  $f_0, f_1$  and  $f_2$  by the following formulae:

$$
f_0 = -\frac{1}{3.6} \times (m + m_r) \times \frac{B}{A} \times (A^2 + D^2)
$$
  

$$
f_1 = \frac{1}{3.6} \times (m + m_r) \times \frac{2 \times BD}{A}
$$
  

$$
f_2 = -\frac{1}{3.6} \times (m + m_r) \times \frac{B}{A}
$$

NOTE If coastdowns are carried out in the manner of split runs, the total resistance, *F*, can be calculated as follows. Calculate the road-load force for each reference speed included in the actual coastdown speed range. Then put each split data into one set, and calculate one road-load force equation for respective directions.

#### **5.3.3.4.6 Total-resistance curve determination**

Determine the total-resistance curve as specified in 5.3.1.4.5.

#### **5.4 Onboard-anemometer based coastdown method**

As an alternative to the determination in 5.3.1, 5.3.2 or 5.3.3, the total resistance may also be determined by the procedure described in 5.4.1 to 5.4.5. This method is applicable to a wind speed range up to 10 m/s on a test road as given in Table 1.

## **5.4.1 Selection of speed range for road-load curve determination**

Select the test speed range as specified in 5.3.3.1.

## **5.4.2 Data collection**

The following data shall be measured and recorded at a maximum of 0,2 s intervals during the test.

- a) elapsed time;
- b) vehicle speed;
- c) wind speed and direction.
- NOTE The wind speed and the wind direction are measured by the onboard anemometry.

#### **5.4.3 Vehicle coastdown**

Vehicle coastdown shall be conducted as specified in 5.3.1.3.1 to 5.3.1.3.4 with an onboard anemometer installed on the vehicle. The anemometer shall be installed in a position such that the effect on the operating characteristics of the vehicle is minimized. It is recommended to install the anemometer at the aerodynamic stagnation point of the vehicle's front and approximately 2 m in front of it. Before the coastdown, the anemometer shall be installed on the vehicle and calibrated appropriately, as specified by the manufacturer. An example of the anemometer calibration procedure is given in Annex A.

## **5.4.4 Determination of coefficients**

Calculate each coefficient by the following equation with multi-regression analysis, using coastdown time and wind data.

$$
-\frac{1}{3,6} \times (m+m_{\rm r}) \times \frac{\mathrm{d}V}{\mathrm{d}t} = a_{\rm mech} + b_{\rm mech}V + c_{\rm mech}V^2 + \frac{1}{2} \times \rho SV_r^2 \times \left(a_0 + a_1\theta + a_2\theta^2 + a_3\theta^3 + a_4\theta^4\right)
$$

where



*S* is the projected frontal area of the vehicle, in square metres  $(m^2)$ ;

*a<sub>n</sub>* (*n* = 0 to 4) is the coefficient for aerodynamic drag as a function of yaw angle, in degrees<sup>-n</sup>;

 $\theta$  is the yaw-angle apparent wind relative to the direction of vehicle travel, in degrees.

NOTE If the wind speed is close to 0, the equation theoretically cannot separate  $c_{\text{mech}}$  and (1/2) ×  $a_0 \rho S$ appropriately. Therefore, a contrained analysis, where  $a_0$  is fixed if it is previously determined, for example in a wind tunnel, or  $c_{\text{mech}}$  is assumed to be zero, may be employed.

#### **5.4.5 Determination of total resistance**

Calculate the total resistance, *F*, where all the wind effects are eliminated, by the following equation with the coefficients obtained in 5.4.4.

$$
F = a_{\text{mech}} + b_{\text{mech}}V + \left(c_{\text{mech}} + \frac{1}{2} \times a_0 \rho S\right) V^2
$$

#### **5.5 Measurement of running resistance by torquemeter method**

As an alternative to the coastdown methods, the torquemeter method may also be used, in which the running resistance is determined by measuring the torque as described in 5.5.1 to 5.5.3.

#### **5.5.1 Installation of torquemeter**

The torquemeter(s) shall be installed on the drive-train of the test vehicle. It is preferable to have wheel torquemeters on each driven wheel.

#### **5.5.2 Vehicle running and data sampling**

#### **5.5.2.1 Start of data collection**

The data collection may be started following preconditioning and stabilization of the vehicle at the speed  $V_j$ , where the running resistance is to be measured.

#### **5.5.2.2 Data collection**

Record at least 10 data sets of speed, torque and time over a period of at least 5 s.

#### **5.5.2.3 Speed deviation**

The speed deviation from the mean speed shall be within the values in Table 3.



**Table 3** 

#### **5.5.3 Calculation of mean speed and mean torque**

#### **5.5.3.1 Calculation process**

Calculate the mean speed *Vj*m*,* in kilometres per hour (km/h), and mean torque *Cj*<sup>m</sup> in newton metres (N·m), over a time period, as follows:

$$
V_{j\mathsf{m}} = \frac{1}{k} \sum_{i=1}^{k} V_{ji}
$$

and

$$
C_{j\mathsf{m}} = \frac{1}{k} \sum_{i=1}^{k} C_{ji} - C_{j\mathsf{s}}
$$

where

 $V_{ji}$  is the vehicle speed of the  $i<sup>th</sup>$  data set, in kilometres per hour (km/h);

*k* is the number of data sets;

and

- $C_{ji}$  is the torque of the *i*<sup>th</sup> data set, in newton metres (N·m);
- $C_{j\text{s}}$  is the compensation term for the speed drift, in newton metres (N·m), which is given by the following formula; *Cj*<sup>s</sup> shall be not greater than 5 % of the mean torque before compensation, and may be neglected if  $\alpha_j$  is no greater than  $\pm$  0,005 m/s<sup>2</sup>:

$$
C_{j\mathbf{S}} = (m + m_{\mathbf{r}}) \times \alpha_j r_j
$$

in which

 $m$  and  $m_r$ 

*rj*

 are the test vehicle mass and the equivalent effective mass, respectively, both in kilograms (kg), defined in 5.3.1.4.4;

is the dynamic radius of the tyre, in metres (m), given by the formula:

$$
r_j = \frac{1}{3.6} \times \frac{v_{jm}}{2 \times \pi N}
$$

and in which

- *N* is the rotational frequency of the driven tyre, in revolutions per second (s<sup>-1</sup>);
- *αj* is the mean acceleration, in metres per second squared  $(m/s<sup>2</sup>)$ , which shall be calculated by the formula:

$$
\alpha_{j} = \frac{1}{3.6} \times \frac{k \sum_{i=1}^{k} t_{i} V_{ji} - \sum_{i=1}^{k} t_{i} \sum_{i=1}^{k} V_{ji}}{k \sum_{i=1}^{k} t_{i}^{2} - (\sum_{i=1}^{k} t_{i})^{2}}
$$

and in which  $t_i$  is the time at which the  $i^{\text{th}}$  data set was sampled, in seconds (s).

#### **5.5.3.2 Accuracy of measurement**

Carry out these measurements in both directions until a minimum of four consecutive figures have been obtained which satisfy accuracy *p*, in percent (%), below. Calculate the mean speed *Vj*m, in kilometres per hour (km/h), and mean torque *Cj*<sup>m</sup> in newton metres, over a time period as follows. The validity of the data shall be decided in accordance with 5.3.1.4.3.

$$
p = \frac{ts}{\sqrt{k}} \times \frac{100}{C_j} \le 3\%
$$

where

*k* is the number of data sets;

 $C_j$  is the running resistance at the speed  $V_j$ , in newton metres (N·m), given by the formula:

$$
\overline{C}_j = \frac{1}{k} \sum_{i=1}^k C_{jmi}
$$

in which  $C_{jmi}$  is the average torque of the *i*<sup>th</sup> pair of data sets at the speed  $V_j$ , in newton metres (N⋅m), given by the formula:

$$
C_{jmi} = \frac{1}{2} \times \left( C_{jmai} + C_{jmbi} \right)
$$

and in which

 $C_{j_{\text{max}}}$  and  $C_{j_{\text{min}}}$  are the mean torques of the *i*<sup>th</sup> data sets at the speed  $V_j$  determined in 5.5.3.1 for each direction respectively, in newton metres (N⋅m);

$$
\overline{s}
$$

*is the standard deviation, in newton metres (N⋅m), defined by the formula:* 

$$
s = \sqrt{\frac{1}{k-1} \sum_{i=1}^{k} \left( C_{jmi} - \overline{C_j} \right)^2}
$$

*t* is the coefficient given by replacing *n* in Table 2 with *k*.

#### **5.5.3.3 Validity of the measured average speed**

The average speed  $V_{jmi}$ , shall not deviate by more than  $\pm$  2 km/h from its mean,  $V_j$ ,  $V_{jmi}$  and  $V_j$  shall be calculated as follows:

$$
\overline{V_j} = \frac{1}{k} \sum_{i=1}^{k} V_{jmi}
$$

and

$$
V_{jmi} = \frac{1}{2} \times \left( V_{jmai} + V_{jmbi} \right)
$$

where  $V_{j\text{maj}}$  and  $V_{j\text{mb}i}$  are the mean speeds of the *i*<sup>th</sup> pair of data sets at the speed  $V_j$  determined in 5.5.3.1 for each direction respectively, in kilometres per hour (km/h).

#### **5.5.4 Running resistance curve determination**

The following regression curve shall be fitted to all the data pairs  $(V_{jm}, C_{jma})$  and  $(V_{jm}, C_{jmb})$  for both directions at all speed points  $V_j$  (j = 1, 2, etc.) described in 5.3.1.1, to determine  $c_{0a}$ ,  $c_{0b}$ ,  $c_{1a}$ ,  $c_{1b}$ ,  $c_{2a}$  and  $c_{2b}$ :

$$
C_{a} = c_{0a} + c_{1a}V + c_{2a}V^{2}
$$

 $C_{\bf h} = c_{0{\bf h}} + c_{1{\bf h}} V + c_{2{\bf h}} V^2$ 

where

- $C_{\mathbf{a}}$  and  $C_{\mathbf{b}}$  are the running resistances in each direction, in newton metres (N·m);
- $c_{0a}$  and  $c_{0b}$  are the constant terms in each direction, in newton metres (N·m);
- $c_{1a}$  are  $c_{1b}$  are the coefficients of the first-order term in each direction, in newton metres hour per kilometre [N⋅m(h/km)];  $c_1$  may be assumed to be zero, if the value of  $c_1V$  is no greater than 3 % of *C* at the reference speed(s); In this case, the coefficients  $c_0$  and  $c_2$  shall be recalculated;
- $c_{2a}$  and  $c_{2b}$  are the coefficients of the second-order term in each direction, in newton metres hour squared per kilometre squared [N⋅m(h/km)<sup>2</sup>];

*V* is the vehicle speed, in kilometres per hour (km/h).

Then calculate the coefficients  $c_0$ ,  $c_1$  and  $c_2$  in the total torque equation using the following formulae:

$$
c_0 = \frac{c_{0a} + c_{0b}}{2}
$$

$$
c_1 = \frac{c_{1a} + c_{1b}}{2}
$$

$$
c_2 = \frac{c_{2a} + c_{2b}}{2}
$$

where

 $c_0$ ,  $c_1$  and  $c_2$  are the average coefficients in the following average total torque equation:

$$
C_{\text{avg}} = c_0 + c_1 V + c_2 V^2
$$

and in which  $C_{\text{av}q}$  is the average running resistance, in newton metres (N⋅m).

## **5.6 Correction to standard atmospheric conditions**

## **5.6.1 Correction factors**

## **5.6.1.1 Determination of correction factor for air resistance**

Determine the correction factor for air resistance  $K_2$  as follows:

$$
K_2 = \frac{T}{293} \times \frac{100}{\rho}
$$

where

- *T* is the mean atmospheric temperature, in kelvins (K);
- $\rho$  is the mean atmospheric pressure, in kilopascals (kPa).

#### **5.6.1.2 Determination of correction factor for rolling resistance**

The correction factor,  $K_0$ , for rolling resistance, in reciprocal kelvins, may be determined, based on the empirical data for the particular vehicle and tyre test, or may be assumed as follows:

 $K_0 = 8.1 \times 10^{-3} \times K^{-1}$ 

#### **5.6.1.3 Wind correction**

Wind correction, for absolute wind speed alongside the test road, shall be made by subtracting the difference that cannot be cancelled by alternate runs from the constant term  $f_0$  given in 5.3.1.4.5, or from  $c_0$  given in 5.5.4. This wind correction shall not apply in the onboard-anemometer-based coastdown method (5.4) as the wind correction is made during the series of data sampling and subsequent analysis. The wind correction resistance  $w_1$  for the coastdown method (5.3) or  $w_2$  for the torquemeter method shall be calculated by the formulae:

$$
w_1 = 3.6^2 \times f_2 v_w^2
$$

or

$$
w_2 = 3.6^2 \times c_2 v_w^2
$$

where

 $w_1$  is the wind correction resistance, in newtons (N):

- *f* is the coefficient of the aerodynamic term determined in 5.3.1.4.5;
- $v_w$  is the average wind speed alongside the test road during the test, in metres per second (m/s);

or

- $w_2$  is the wind correction resistance, in newtons (N);
- $c<sub>2</sub>$  is the coefficient of the aerodynamic term determined in 5.5.4.

#### **5.6.2 Road-load curve correction**

**5.6.2.1** The fitting curve determined in 5.3.1.4.5, 5.3.2.4.6 or 5.3.3.4.6 shall be corrected to reference conditions as follows:

$$
F^* = \{(f_0 - w_1) + f_1 V\} \times \{(1 + K_0 (T - 293)\} + K_2 f_2 V^2)
$$

where

- $F^*$  is the corrected total resistance in newtons (N);
- *f* is the constant term, in newtons  $(N)$ ;
- *f* is the coefficient of the first-order term, in newtons hour per kilometre [N⋅(h/km)];
- *f* 2 is the coefficient of the second-order term, in newtons hour squared per kilometre squared  $[N·(h/km)<sup>2</sup>]$ ;
- $K<sub>0</sub>$  is the correction factor for rolling resistance, as defined in 5.6.1.2;
- $K<sub>2</sub>$  is the correction factor for air resistance, as defined in 5.6.1.1;
- $V$  is the vehicle speed, in kilometres per hour (km/h);
- $w_1$  is the wind correction resistance, as defined in 5.6.1.3.
- **5.6.2.2** The fitting curve determined in 5.4.5 shall be corrected to reference conditions as follows:

$$
F^* = (a_{\text{mech}} + b_{\text{mech}}V + c_{\text{mech}}V^2) \times (1 + K_0 \times (T - 293)) + \frac{1}{2} \times K_2 a_0 \rho S V^2
$$

#### where

*F*\* is the corrected total resistance, in newtons (N);

 $a_{\text{mech}}$  is the coefficient of mechanical drag, in newtons (N); --`,,```,,,,````-`-`,,`,,`,`,,`---

 $b<sub>mech</sub>$  is the coefficient of mechanical drag, in newtons per kilometre per hour [N/(km/h)];

- *c*mech is the coefficient of mechanical drag, in newtons per kilometre squared per hour squared [N/(km/h)2];
- $\rho$  is the air density, in kilograms per cubic metre (kg/m<sup>3</sup>);
- *S* is the projected frontal area of the vehicle, in square metres  $(m^2)$ ;
- $a_0$  is the coefficient for aerodynamic drag, as a function of yaw angle;
- $K<sub>0</sub>$  is the correction factor for rolling resistance, as defined in 5.6.1.2;

 $K<sub>2</sub>$  is the correction factor for air resistance as defined in 5.6.1.1;

*V* is the vehicle speed, in kilometres per hour (km/h).

**5.6.2.3** The fitting curve determined as decribed in 5.5.4 shall be corrected to reference conditions as follows:

$$
C^* = \{(c_0 - w_2) + c_1 V\} \times \{(1 + K_0 \times (T - 293)\} + K_2 c_2 V^2)
$$

#### where

- $C^*$  is the corrected total running resistance, in newton metres (N·m);
- $c_0$  is the constant term, in newton metres (N·m);
- $c_1$  is the coefficient of the first-order term, in newton metres hour per kilometre [N·m (h/km)];
- $c_2$  is the coefficient of the second-order term, in newton metres hour squared per kilometre squared  $[N·m·(h/km)<sup>2</sup>]$ ;
- $K<sub>0</sub>$  is the correction factor for rolling resistance as defined in 5.6.1.2;
- $K<sub>2</sub>$  is the correction factor for air resistance as defined in 5.6.1.1;
- $V$  is the vehicle speed, in kilometres per hour (km/h);
- $w_2$  is the wind correction resistance as defined in 5.6.1.3.

## **6 Road-load measurement by wind tunnel/chassis dynamometer**

## **6.1 Aerodynamic drag measurement in wind tunnel**

#### **6.1.1 Requirements for wind tunnel**

The wind-tunnel design, the test methods and the corrections shall be sufficient to provide a *SCd* [(see 4j)] representative of the on-road *SCd* value.

#### **6.1.2 Testing procedure**

**6.1.2.1** The test vehicle shall be positioned according to the specifications of the wind-tunnel laboratory, so as to ensure that the air stream is parallel to the longitudinal axis of the test vehicle. The test-vehicle ground clearance shall be checked according to the vehicle manufacturer's specification, and shall be adjusted if required. The engine bonnet/hood, all windows, any covers of the air ventilation system, headlamps, etc., shall be closed. The test vehicle shall be immobilized in a way that minimizes the effect on the airflow.

**6.1.2.2** The measurement shall be conducted according to the specification of the wind-tunnel laboratory. It is recommended to use the test section wind speed of 140 km/h, but the lowest wind speed shall be 80 km/h.

Two measurements shall be conducted. If the difference in the resultant *SCd* values is greater than 1 %, the test vehicle set-up and the wind-tunnel set-up shall be checked and corrected if necessary. Two further tests shall then be performed. This procedure shall be repeated until a difference of no more than 1 % between two values is obtained.

#### **6.1.3 Test result**

Determine the test result (*SCd*), in square metres, by averaging a pair of the measurement values.

## **6.2 Rolling resistance determination with chassis dynamometer**

#### **6.2.1 Testing device**

The chassis dynamometer shall have the following characteristics:

- $-$  single roller (double single rollers for permanent four-wheel-drive vehicles);
- roller diameter: no less than 1.2 m;
- ⎯ roller surface: smooth steel, or other equivalent materials, or textured and shall be kept clean. In cases where a textured surface is used, this fact shall be noted in the test report, and the surface texture shall be 180  $\mu$ m deep (80 grit).

The external vehicle-cooling fan shall have the following characteristics:

- blower nozzle area: surface: greater than  $0,4$  m<sup>2</sup>;
- cooling wind speed:  $\pm$  2 km/h of roller speed.

#### **6.2.2 Testing procedure**

The rolling resistance of the front and rear wheels shall be measured separately. When a double-single-axistype chassis dynamometer is used for a permanent four-wheel-drive vehicle, the resistance of both axles may be measured simultaneously. During the test, the vehicle shall be cooled with an external cooling fan.

NOTE This procedure is based on force measurement at several steady speed points and not under deceleration.

**6.2.2.1** Adjust the vehicle conditions as specified in 5.2.1.1.

**6.2.2.2** Adjust the test room temperature to 293 K  $^{+6}_{-2}$  K. Warm up the chassis dynamometer according to the chassis-dynamometer specification. Measure the chassis-dynamometer running losses.

**6.2.2.3** Place the non-driving wheels in the normal front-driving direction on the chassis dynamometer first;

- a) restrain the vehicle, taking care not to apply an abnormal load on the measured axle;
- b) warm up the axle until the chassis-dynamometer force is stabilized, or up to a maximum of 30 min at the highest reference speed;
- c) measure the axle rolling resistance for this speed;
- d) decrease the speed to the immediate lower reference speed;
- e) measure the axle rolling resistance for this new speed;
- f) repeat c) to e) for each reference speed;
- g) once the loads have been measured for each reference speed, repeat the entire measurement procedure from c) to f);
- h) if the difference is greater than 4 % at any reference speed, the test vehicle set-up and the chassisdynamometer set-up shall be checked and corrected, if necessary. Two further tests shall then be performed. This procedure shall be repeated until a difference of no more than 4 % between two values, at any reference speed, is obtained;
- i) once two satisfactory measurements have been obtained, the final result shall be the average of the two measurements for each reference speed.
- **6.2.2.4** Place the driving axle on the chassis dynamometer;
- a) restrain the vehicle, taking care not to apply an abnormal load on the measured axle;
- b) adjust the chassis-dynamometer load to an appropriate value;
- c) warm up the axle until the chassis-dynamometer force is stabilized, or up to a maximum of 30 min at the highest reference speed, running the engine on the appropriate gear;
- d) return the engine to idle, shift the transmission into neutral, and re-engage the clutch in the case of a manual transmission vehicle;
- e) stabilise the speed at the highest reference speed;
- f) measure the axle rolling resistance for this speed;
- g) decrease the speed to the immediate lower reference speed;
- h) measure the axle rolling resistance for this new speed;
- i) repeat e) to h) for each reference speed;
- j) once the loads have been measured for each reference speed, repeat the entire measurement procedure from e) to i);
- k) if the difference is greater than 4 % at any reference speed, the test vehicle set-up and the chassisdynamometer set-up shall be checked and corrected, if necessary. Two further tests shall then be performed. This procedure shall be repeated until a difference of no more than 4 % between two values at any reference speed is obtained;
- l) once two satisfactory measurements have been obtained, the final result shall be the average of the two measurements for each reference speed.

#### **6.2.3 Test results**

For each reference speed  $V_j$ , calculate the total rolling resistance using the following formula:

$$
Rr_{t,j} = Rr_{f,j} + Rr_{r,j} - 2 \times Rr_{loss,j}
$$

where

 $Rr_{t,i}$  is the total rolling resistance, in newtons (N);

*Rr*<sub>f</sub>*i* is the rolling resistance of the front wheel, in newtons (N);

*Rr*r*,j* is the rolling resistance of the rear wheel, in newtons (N);

 $Rr_{\text{loss},i}$  is the loss of the chassis dynamometer, in newtons (N).

The *Rr*t*,j* result should be corrected. Examples of the correction procedures are given in Annex B.

#### **6.3 Total-resistance calculation**

The total road-load resistance is calculated for each reference speed  $V_j$  by the following formula, using  $SCd$ obtained in 6.1 and *Rr*t, *<sup>j</sup>* in 6.2:

$$
F_j = \frac{1}{3.6^2} \times \frac{\rho SCdV_j^2}{2} + Rr_{t,j}
$$

where

- $F_i$  is the total road-load resistance, in newtons (N);
- $\rho$  is the air density, in kilograms per cubic metre (kg/m<sup>3</sup>);
- *S* is the projected frontal area of the vehicle, in square metres  $(m^2)$ ;
- *Cd* is the aerodynamic coefficient;

 $V_i$  is the vehicle speed, in kilometres per hour (km/h).

## **6.4 Total-resistance curve determination**

If necessary, the total-resistance curve shall be determined by fitting the following regression curve with the least-squares method:

$$
F = f_0 + f_1 V + f_2 V^2
$$

where

- *F* is the total resistance, in newtons (N);
- $f_{0}$ is the constant term, in newtons (N);
- *f* is the coefficient of the first-order term, in newtons hour per kilometre (N⋅h/km);
- *f* is the coefficient of the second-order term, in newtons hour squared per kilometre squared  $[(N·(h/km)<sup>2</sup>]$ ;
- $V$  is the vehicle speed, in kilometres per hour (km/h).

## **Annex A**

## (informative)

## **Examples of onboard-anemometer calibration procedure**

## **A.1 Introduction**

This annex gives an example of a calibration procedure for a type of onboard-anemometer to be used in 5.4. The onboard-anemometer-based coastdown method requires instrumentation that measures the apparent relative air speed and apparent yaw angle encountered by the vehicle during a coastdown test. The method described below requires that the calibration data collection assume a minimum variation in the true wind speed and true wind attack angle, during each pair of opposite direction drives.

## **A.2 Instrumentation and theory**

A meteorological anemometer is installed on a mast, approximately 2 m in front of the vehicle at the approximately aerodynamic stagnation height, level with the vehicle front bumper. Typically, this device produces an anemometer-propeller rotational signal which is proportional to the apparent relative air speed, as well as a static signal that indicates the angular direction of the anemometer vane with respect to some reference position. These signals are assumed to correlate with the observed changes in vehicle deceleration, such that the coefficients *S*,  $a_0$ ,  $a_1$ ,  $a_2$ ,  $a_3$  and  $a_4$  can be determined in the following aerodynamic drag ( $F_{\text{aero}}$ ) equation, which is consistent with that described in 5.4.4.

$$
F_{\text{aero}} = \frac{1}{2} \times \rho S V_{\text{r}}^2 \times \left( a_0 + a_1 \theta + a_2 \theta^2 + a_3 \theta^3 + a_4 \theta^4 \right)
$$

A "zero yaw offset" must be calculated by a method described in this Annex, because the aerodynamic centreline of the anemometer may not be assumed to coincide exactly with the aerodynamic centre-line of the vehicle.

The following procedure outlines a method by which the anemometer signals can be correlated to vehicle deceleration.

## **A.3 Assumptions and procedural suggestions**

## **A.3.1 Symbols**

Symbols and the meanings in A.3 are as follows:

- *V* is the vehicle speed, in kilometres per hour (km/h);
- *Va* is the apparent air speed, in the direction of the vehicle movement without respect to wind, in

kilometres per hour (km/h);

- *Vw* is the true wind speed, in kilometres per hour (km/h);
- $\alpha$  is the true direction of the wind, with respect to the direction of the track, in degrees;
- $\theta_0$  is the zero yaw offset angle, in degrees;

## **ISO 10521-1:2006(E)**

 $\theta_{\text{true}}$  is the true yaw angle, in degrees;

 $\theta_{\text{apparent}}$  is the apparent yaw angle, in degrees;

 $Vr_{true}$  is the true relative air speed, in kilometres per hour (km/h);

*Vr*<sub>apparent</sub> is the apparent relative air speed, in kilometres per hour (km/h);

*ky* is the yaw correction coefficient;

 $ka$  is the coefficient relating  $Vr_{\text{true}}$  to  $Vr_{\text{anparent}}$ ;

*ka\** is the coefficient relating *V* to *Va*;

- *kr* is the minimum velocity at which the anemometer will respond, in kilometres per hour (km/h);
- *ku* is a unitless coefficient relating yaw angle to relative air speed.

## **A.3.2 Graphical description of the pertinent parameters**

The apparent air speed (*Va*) is lower than the vehicle speed (*V*) due to the presence of the vehicle. Because of this retardative effect, the measured relative air speed ( $Vr_{\text{anparent}}$ ) and the true relative air speed ( $Vr_{\text{true}}$ ) are shown graphically in Figures A.1 and A.2.







## **A.3.3 Equation assumption**

When it is assumed that the variation in the true wind attack angle during each pair of opposite direction drives is a minimum, *Va* can be calculated with  $V_{\text{apparent}}$  and  $\theta_{\text{apparent}}$  as follows.

$$
Va = \frac{Vr_{1,\text{apparent}}\cos\theta_{1,\text{apparent}} + \left(Vr_{1,\text{apparent}}\sin\theta_{1,\text{apparent}}/Vr_{2,\text{apparent}}\sin\theta_{2,\text{apparent}}\right) \times Vr_{2,\text{apparent}}\cos\theta_{2,\text{apparent}}
$$
  

$$
1 + \left(Vr_{1,\text{apparent}}\sin\theta_{1,\text{apparent}}/Vr_{2,\text{apparent}}\sin\theta_{2,\text{apparent}}\right)
$$

The relationship between *V* and *Va* is shown in Figure A.2.



**Figure A.3 — Relationship between** *V* **and**  $V_a$ 

Graphically, the relationship between *Vr*true and *Vr*apparent can be also described similarly. Taking the effect of  $ku$  and  $\theta_{\text{true}}$  into consideration, however, the relationships and operating equations used in Figure A.1 are assumed as follows;

$$
\theta_{true} = ky \times (\theta_{apparent} - \theta_0), \text{ in a direction against the wind} \tag{A.1}
$$

$$
\theta_{\text{true}} = ky \times (\theta_{\text{apparent}} + \theta_0), \text{ in a direction with the wind} \tag{A.2}
$$

$$
Vr_{\text{true}} = \left(ka \times Vr_{\text{apparent}} + kr\right) \times \left(1 - ku \times \theta_{\text{true}}^2\right)
$$
\n(A.3)

As the errors in these equations become larger in proportion with the increase of  $\theta$  apparent, it is recommended to eliminate data at  $\theta_{\text{aoparent}}$  of 20° or more.

## **A.3.4 Calibration procedure**

The vehicle is driven at a constant speed over a fixed length of track, calibration data is recorded, and then the vehicle is driven in the opposite direction over the same section of track at the same speed (*V*). Repeat the same procedure at (a) different constant speed(s) at least once. It is recommended that 80 km/h should be included in the speed selection.

If *kr* is known previously by an appropriate technique, the calibration data collection may be done with a run at a constant speed. In this case, 80 km/h is recommended as the vehicle speed. --`,,```,,,,````-`-`,,`,,`,`,,`---

At least 3 pairs of passes at each speed are recommended for the calibration data collection.

The average values of  $\theta$  <sub>apparent</sub> and  $Vr$ <sub>apparent</sub> are calculated for each direction. Then, solve *ky*, *ka*, *ku* and  $\theta$ <sub>0</sub> in Equations (A.1), (A.2) and (A.3) by the least-squares or iteration technique, while the value of *kr* is assumed from the relationship between *V* and *Va* as described in Figure A.2.

During the subsequent coastdown test, the  $ky$ ,  $ka$  and  $ku$  values are introduced to compute  $Vr_{\text{true}}^2$  and  $\theta_{\text{true}}$  of the aerodynamic term,

$$
\frac{1}{2} \times \rho SVr_{\text{true}}^2 \times \left( a_0 + a_1 \theta_{\text{true}} + a_2 \theta_{\text{true}}^2 + a_3 \theta_{\text{true}}^3 + a_4 \theta_{\text{true}}^4 \right)
$$

## **Annex B**

(informative)

## **Examples of dynamometer-measured rolling-resistance correction method**

## **B.1 Introduction**

It is recommended that the value of the total rolling resistance measured with chassis dynamometers should be corrected. This annex describes three correction methods as examples.

## **B.2 Method 1**

In this method, tyre rolling resistance is separated from other mechanical losses, and the correction factor for only the tyre rolling resistance is determined. Also, in this method, the correction factor for the tyre rolling resistance is determined by comparing the change of rolling resistance value on the road and the change of the tyre rolling resistance value on the chassis dynamometer, under two different test conditions. For the comparison test, the factor that affects only the tyre rolling resistance, for example the tyre inflation pressure or the axle load, shall be altered.

NOTE The loss of the wheel bearing is included in the tyre rolling resistance in this method. However, generally it is sufficiently small in comparison with the other mechanical losses, and may be neglected.

**B.2.1** Under the two conditions, determine the total-resistance curve from road data to calculate the following equation coefficients:

$$
F_1 = f_{0,1} + f_{1,1}V + f_{2,1}V^2
$$

$$
F_2 = f_{0,2} + f_{1,2}V + f_{2,2}V^2
$$

where

 $F_1, F_2$  are the total resistances under the first and second conditions, in newtons (N);

 $f_{0,1}$ ,  $f_{0,2}$  are the constant terms under the first and second conditions, in newtons (N);

 $f_{1,1}, f_{1,2}$  are the coefficients of the first-order term under the first and second conditions, in newtons hour per kilometre [N·(h/km)];

 $f_{2,1}$ ,  $f_{2,2}$  are the coefficients of the second-order term of vehicle speed under the first and second conditions, in newtons hour squared per kilometre squared  $[(N·(h/km)^2];$ --`,,```,,,,````-`-`,,`,,`,`,,`---

 $V_i$  is the vehicle speed, in kilometres per hour (km/h).

Notice that the rolling resistance consists of only the constant and the first-order terms. This simplification presumes that the contribution from the rolling resistance to *f* 2 is negligible. The following equations express the simplified result.

$$
F_{\text{roll1},j} = f_{0,1} + f_{1,1}V_j
$$

$$
F_{\text{roll2},j} = f_{0,2} + f_{1,2}V_j
$$

where  $F_{\mathsf{roll1},j}$  and  $F_{\mathsf{roll2},j}$  are the rolling resistances measured on the road under the first and second conditions, in newtons (N).

**B.2.2** Substitute the formula specified in 6.2.3 with the following formulae:

$$
R{r_{t,j}}^* = K_{3,j} \times (R{r_{t,j}} + R{r_{t,j}}) + R{r_{tm,j}} + R{r_{tm,j}}
$$
  

$$
R{r_{t,j}}^* = K_{3,j} \times (R{r_{t,j}} + R{r_{r,j}} - R{r_{tm,j}} - 2 \times R{r_{loss,j}}) + R{r_{tm,j}} + R{r_{rm,j}}
$$

where

 $Rr_{t,i}$ <sup>\*</sup> is the corrected total rolling resistance, in newtons (N);

 $K_{3,i}$  is the correction factor for the tyre rolling resistance;

*Rr<sub>fti</sub>* is the front-tyre rolling resistance measured on a chassis dynamometer, in newtons (N);

 $Rr_{rt,i}$  is the rear-tyre rolling resistance measured on a chassis dynamometer, in newtons (N);

*Rr<sub>fm</sub>*, is the front mechanical loss, except for the tyre rolling resistance, in newtons (N);

*Rr*rm, *j* is the rear mechanical loss, except for the tyre rolling resistance, in newtons (N);

 $Rr_{f,i}$  is the front total rolling resistance, including the loss of the chassis dynamometer, in newtons (N);

*Rr*r, *j* is the rear total rolling resistance, including the loss of the chassis dynamometer, in newtons (N);

 $Rr_{\text{loss}, i}$  is the loss of the chassis dynamometer, in newtons (N).

**B.2.3** Set the front axle of the vehicle on the chassis dynamometer, and measure the front rolling resistances under the two different conditions, which are expressed by the following equations:

 $Rr_{\text{f1},j} = Rr_{\text{f1},j} + Rr_{\text{fml},j} + Rr_{\text{loss},j}$ 

for the first condition

$$
Rr_{f2,j} = Rr_{\text{ft2},j} + Rr_{\text{fm2},j} + Rr_{\text{loss},j}
$$

for the second condition

where

*Rr*<sub>ft1</sub>, and *Rr*<sub>ft2, *j* are the front-tyre rolling resistances, measured on a chassis dynamometer including</sub> the loss of the chassis dynamometer, in newtons (N);

*Rr*fm1, *j* and *Rr*fm2 *j* are the front mechanical losses, except for the tyre rolling resistance, in newtons (N).

**B.2.4** Disconnect the front joint between the wheel and axle shaft or driveshaft, and then measure the tyre rolling resistances, including the loss of chassis dynamometer,  $Rr_{\text{ft1},j} + Rr_{\text{loss},j}$  and  $Rr_{\text{ft2},j} + Rr_{\text{loss},j}$ ,on the chassis dynamometer.

**B.2.5** Calculate the mechanical losses, except for tyre,  $Rr_{\text{fm1},j}$  and  $Rr_{\text{fm2},j}$ , as the difference of B.2.3 and B.2.4.

**B.2.6** Remove the vehicle from the chassis dynamometer, and then measure the loss of the chassis dynamometer, *Rr*loss,*<sup>j</sup>* .

**B.2.7** Calculate the front-tyre rolling resistances,  $Rr_{\text{ft1},j}$  and  $Rr_{\text{ft2},j}$ , from B.2.3, B.2.5 and B.2.6.

**B.2.8** Set the rear axle of the vehicle on the chassis dynamometer, and measure the rolling resistances under the two different conditions, which are expressed by the following equations

 $Rr_{r1,i} = Rr_{rt1,i} + Rr_{rm1,i} + Rr_{loss,i}$ 

for the first condition

 $Rr_{r2,i} = Rr_{rt2,i} + Rr_{rm2,i} + Rr_{loss,j}$ 

for the second condition

where

 $Rr_{rt1,j}$  and  $Rr_{rt2,j}$  are the rear-tyre rolling resistances, measured on a chassis dynamometer including the loss of the chassis dynamometer, in newtons (N);

*Rr<sub>rm1</sub>*, and *Rr<sub>rm2</sub>*, are the rear mechanical losses, except for the tyre rolling resistance, in newtons (N).

**B.2.9** Disconnect the rear joint between wheel and axle shaft or driveshaft, and then measure the rolling resistances including the loss of chassis dynamometer,  $Rr_{rt1j} + Rr_{loss}$  and  $Rr_{rt2j} + Rr_{loss}$ , on the chassis dynamometer.

**B.2.10** Calculate the mechanical losses except for tyre,  $Rr_{rm}$ <sub>*rm1 j*</sub> and  $Rr_{rm}$ <sub>*i*</sub>, as the difference of B.2.8 and B.2.9.

**B.2.11** Calculate the rear-tyre rolling resistances,  $Rr_{rt1j}$  and  $Rr_{rt2j}$ , from B.2.6, B.2.8 and B.2.10.

**B.2.12** Determine the correction factor for each reference speed,  $V_j$ , by the following equation:

 $K_{3,j} = \left\{ (f_{0,1} + f_{1,1}V_j) - (f_{0,2} + f_{1,2}V_j) \right\} / \left\{ (Rr_{\text{ft1},j} + Rr_{\text{rt1},j}) - (Rr_{\text{ft2},j} + Rr_{\text{rt2},j}) \right\}$ 

The correction factor may be applied to future measurements of similar sized vehicles and tyres on the same chassis dynamometer.

NOTE If a dual-axis chassis dynamometer is used for Method 1, the front and the rear resistances can be measured at the same time.

## **B.3 Method 2**

In this method, the total rolling resistance values measured on the chassis dynamometer are compared to the total-resistance values obtained on the road using, in this example, the coastdown method described in 5.3.

**B.3.1** Determine the total-resistance curve from road data to estimate the following equation coefficients:

$$
F = f_0 + f_1 V + f_2 V^2
$$

where

- *F* is the total resistance, in newtons (N);
- *f* is the constant term, in newtons  $(N)$ ;
- *f* is the coefficient of the first-order term, in newtons hour per kilometre [N⋅(h/km)];
- *f* is the coefficient of the second-order term of vehicle speed, in newtons hour squared per kilometre squared [N⋅(h/km)<sup>2</sup>];
- $V$  is the vehicle speed, in kilometres per hour (km/h).

Assume the following equation, on the presumption that the contribution to *f* 2 which comes from the rolling resistance is negligible:

 $F_{\text{roll } i} = f_0 + f_1 V_i$ 

where  $F_{roll, i}$  is the rolling resistance measured on the road, in newtons (N).

**B.3.2** The corrected total rolling resistance is expressed by the following formula using the chassisdynamometer measurement data as specified in 6.2.

$$
Rr_{t,j}^* = K_{4,j} \times \left(Rr_{t,j} + Rr_{t,j} - 2 \times Rr_{\text{loss},j}\right)
$$

where

- $Rr_{t,j}^{\dagger}$ is the corrected total rolling resistance, in newtons (N);
- *K*4,*<sup>j</sup>* is the correction factor for the tyre rolling resistance;
- $Rr_f$ , is the rolling resistance of the front-wheel dynamometer, including the loss of the chassis dynamometer, in newtons (N);
- *Rr*r,*<sup>j</sup>* is the rolling resistance of the rear-wheel dynamometer, including the loss of the chassis dynamometer, in newtons (N);

 $Rr_{\text{loss}}$ *;* is the loss of the chassis dynamometer, in newtons (N).

**B.3.3** Determine the correction factor for each reference speed,  $V_j$ , using the following equation, because  $F_{\mathsf{roll},j}$  is equal to  $Rr_{\mathsf{t},j}$ :

$$
K_{4,j} = (f_0 + f_1 V_1) / (R r_{f,j} + R r_{f,j} - 2 \times R r_{loss,j})
$$

The correction factor may be applied to future measurements of similar sized vehicles and tyres on the same chassis dynamometer.

## **B.4 Method 3**

The total rolling resistance values measured on the dynamometer shall be compared to the total-resistance values obtained on the road using, in this example, the coastdown method described in 5.3. The *SCd* value is measured in a wind tunnel to separate the on-road rolling resistance from the total on-road resistance.

**B.4.1** Determine the total-resistance curve from road data to estimate the following equation coefficients:

$$
F = f_0 + f_1 V_j + f_2 V^2
$$

where

- *F* is the total resistance, in newtons (N);
- $f<sub>0</sub>$  is the constant term, in newtons (N);
- $f_1$  is the coefficient of the first-order term, in newtons hour per kilometre (N·h/km);
- $f<sub>2</sub>$  is the coefficient of the second-order term of vehicle speed, in newtons hour squared per kilometre squared [N⋅(h/km)2];
- $V$  is the vehicle speed, in kilometres per hour (km/h).

**B.4.2** Measure *SCd* of the vehicle using the method described in 6.1, in order to calculate the values of the on-road rolling resistance at each reference speed. Then, assume the following equation:

$$
F_{\text{roll},j} = f_0 + f_1 V_1 + f_2 V_j^2 - \frac{1}{2} \times \rho SCdV_j^2
$$

where  $F_{\mathsf{roll},j}$  is the value of the calculated on-road rolling resistance, for each reference speed,  $V_j$ .

**B.4.3** The corrected total rolling resistance is expressed by the following formula, using the chassisdynamometer measurement data as specified in 6.2.

$$
Rr_{t,j}^* = K_{5,j} \times \left(Rr_{t,j} + Rr_{t,j} - 2 \times Rr_{\text{loss},j}\right)
$$

where

- $Rr_{t,j}$ is the corrected total rolling resistance, in newtons  $(N)$ ;
- *K*5,*<sup>j</sup>* is the correction factor for the tyre rolling resistance;
- $R_{f,i}$  is the rolling resistance of the front-wheel dynamometer, including the loss of the chassis dynamometer, in newtons (N);
- *Rr*r,*<sup>j</sup>* is the rolling resistance of the rear-wheel dynamometer, including the loss of the chassis dynamometer, in newtons (N);
- $Rr_{\text{loss},i}$  is the loss of the chassis dynamometer, in newtons (N).

**B.4.4** Determine the correction factor for each reference speed  $V_j$  by the following equation, because  $F_{\text{roll},j}$ is equal to  $Rr_{\mathfrak{t},j}$ :

$$
K_{5,j} = \left(f_0 + f_1 V_1 + f_2 V_j^2 - \frac{1}{2} \times \rho SCdV_j^2\right) / \left(Rr_{f,j} - Rr_{f,j} - Rr_{\text{loss},j}\right)
$$

The correction factor may be applied to future measurements of similar sized vehicles and tyres on the same chassis dynamometer.

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