INTERNATIONAL STANDARD

ISO 10303-105

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Industrial automation systems and integration — Product data representation and exchange —

Part 105:

Integrated application resource: Kinematics

Systèmes d'automatisation industrielle et intégration — Représentation et échange de données de produits —

Partie 105: Ressource d'application intégrée: Cinématique

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Foreword

The International Organization for Standardization (ISO) is a worldwide federation of national standards bodies (ISO member bodies). The work of preparing International Standards is normally carried out through ISO technical committees. Each member body interested in a subject for which a technical committee has been established has the right to be represented on that committee. International organizations, governmental and non-governmental, in liaison with ISO, also take part in the work. ISO collaborates closely with the International Electrotechnical Commission (IEC) on all matters of electrotechnical standardization.

Draft International Standards adopted by technical committees are circulated to the member bodies for voting. Publication as an International Standard requires approval by at least 75% of the member bodies casting a vote.

International Standard ISO 10303-105 was prepared by Technical Committee ISO/TC 184, Industrial automation systems and integration, Subcommittee SC4, Industrial data.

ISO 10303 consists of the following parts under the general title Industrial automation systems and integration – Product data representation and exchange:

- Part 1, Overview and fundamental principles;
- Part 11, Description methods: The EXPRESS language reference manual;
- Part 12, Description method: The EXPRESS-I language reference manual;
- Part 21, Implementation methods: Clear text encoding of the exchange structure;
- Part 22, Implementation method: Standard data access interface specification;
- Part 23, Implementation method: C++ language binding to the standard data access interface;
- Part 24, Implementation method: C language binding to the standard data access interface:
- Part 26, Implementation method: Interface definition language binding to the standard data access interface;
 - Part 31, Conformance testing methodology and framework: General concepts;
- Part 32, Conformance testing methodology and framework: Requirements on testing laboratories and clients;
- Part 33, Conformance testing methodology and framework: Structure and use of abstract test suites;
 - Part 34, Conformance testing methodology and framework: Abstract test methods;

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- Part 35, Conformance testing methodology and framework: Abstract test methods for SDAI implementations;
 - Part 41, Integrated generic resources: Fundamentals of product description and support;
 - Part 42, Integrated generic resources: Geometric and topological representation;
- Part 43, Integrated generic resources: Representation structures;
- Part 44, Integrated generic resources: Product structure configuration;
- Part 45, Integrated generic resource: Materials;
- Part 46, Integrated generic resource: Visual presentation;
- Part 47, Integrated generic resource: Shape variation tolerances;
- Part 49, Integrated generic resource: Process structure and properties;
- Part 101, Integrated application resource: Draughting;
- Part 104, Integrated application resource: Finite element analysis;
- Part 105, Integrated application resource: Kinematics;
- Part 106, Integrated application resource: Building construction core model;
- Part 201, Application protocol: Explicit draughting;
- Part 202, Application protocol: Associative draughting;
- Part 203, Application protocol: Configuration controlled design;
- Part 204, Application protocol: Mechanical design using boundary representation;
- Part 205, Application protocol: Mechanical design using surface representation;
- Part 207, Application protocol: Sheet metal die planning and design;
- Part 208, Application protocol: Life cycle management Change process;
- Part 209, Application protocol: Composite and metallic structural analysis and related design;
- Part 210, Application protocol: Design of layered electronic products;

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- Part 211, Application protocol: Electronics test diagnostics and remanufacture;
- Part 212, Application protocol: Electrotechnical design and installation;
- Part 213. Application protocol: Numerical control process plans for machined parts;
- Part 214, Application protocol: Core data for automotive mechanical design;
- Part 215, Application protocol: Ship arrangement;
- Part 216, Application protocol: Ship moulded forms;
- Part 217, Application protocol: Ship piping;
- Part 218, Application protocol: Ship structures;
- Part 220, Application protocol: Process planning, manufacture, and assembly of layered electronic products;
- Part 221, Application protocol: Functional data and their schematic representation for process plant;
- Part 222, Application protocol: Exchange of product data for composite structures;
- Part 223, Application protocol: Exchange of design and manufacturing product information for cast parts;
- Part 224, Application protocol: Mechanical product definition for process plans using mechanical feature;
- Part 225, Application protocol: Building elements using explicit shape representation;
- Part 226, Application protocol: Ship mechanical systems;
- Part 227, Application protocol: Plant spatial configuration;
- Part 228, Application protocol: Building services: Heating, ventilation, and air conditioning;
- Part 229, Application protocol: Exchange of design and manufacturing product information for forged parts;
- Part 230, Application protocol: Building structural frame: Steelwork;
- Part 231, Application protocol: Process engineering data: Process design and process specification of major equipment;

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- Part 232, Application protocol: Technical data package;
- Part 301, Abstract test suite: Explicit draughting;
- Part 302, Abstract test suite: Associative draughting;
- Part 303, Abstract test suite: Configuration controlled design;
- Part 304, Abstract test suite: Mechanical design using boundary representation;
- Part 305, Abstract test suite: Mechanical design using surface representation;
- Part 307, Abstract test suite: Sheet metal die planning and design;
- Part 308, Abstract test suite: Life cycle management Change process;
- Part 309, Abstract test suite: Composite and metallic structural analysis and related design;
- Part 310, Abstract test suite: Design of layered electronic products;
- Part 311, Abstract test suite: Electronics test diagnostics and remanufacture;
- Part 312, Abstract test suite: Electrotechnical design and installation;
- Part 313, Abstract test suite: Numerical control process plans for machined parts;
- Part 314, Abstract test suite: Core data for automotive mechanical design;
- Part 315, Abstract test suite: Ship arrangement;
- Part 316, Abstract test suite: Ship moulded forms;
- Part 317, Abstract test suite: Ship piping;
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- Part 322, Abstract test suite: Exchange of product data for composite structures;
- Part 323, Abstract test suite: Exchange of design and manufacturing product information for cast parts;

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- Part 324, Abstract test suite: Mechanical product definition for process plans using mechanical features;
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- Part 330, Abstract test suite: Building structural frame: Steelwork;
- Part 331, Abstract test suite: Process engineering data: Process design and process specification of major equipment;
 - Part 332, Abstract test suite: Technical data package;
- Part 501, Application interpreted construct: Edge-based wireframe;
- Part 502, Application interpreted construct: Shell-based wireframe;
- Part 503, Application interpreted construct: Geometrically bounded 2D wireframe;
- Part 504, Application interpreted construct: Draughting annotation;
- Part 505, Application interpreted construct: Drawing structure and administration;
- Part 506, Application interpreted construct: Draughting elements;
- Part 507, Application interpreted construct: Geometrically bounded surface;
- Part 508, Application interpreted construct: Non-manifold surface;
- Part 509, Application interpreted construct: Manifold surface;
- Part 510, Application interpreted construct: Geometrically bounded wireframe;
- Part 511, Application interpreted construct: Topologically bounded surface;
- Part 512, Application interpreted construct: Faceted boundary representation;
- Part 513, Application interpreted construct: Elementary boundary representation;

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- Part 514, Application interpreted construct: Advanced boundary representation;
- Part 515, Application interpreted construct: Constructive solid geometry;
- Part 517, Application interpreted construct: Mechanical design geometric presentation;
- Part 518, Application interpreted construct: Mechanical design shaded representation.

The structure of this International Standard is described in ISO 10303-1. The numbering of the parts of this International Standard reflects its structure:

- Parts 11 to 13 specify the description methods,
- Parts 21 to 26 specify the implementation methods,
- Parts 31 to 35 specify the conformance testing methodology and framework,
- Parts 41 to 49 specify the integrated generic resources,
- Parts 101 to 106 specify the integrated application resources,
- Parts 201 to 232 specify the application protocols,
- Parts 301 to 332 specify the abstract test suites, and
- Parts 501 to 518 specify the application interpreted constructs.

Should further parts be published, they will follow the same numbering pattern.

Annexes A and B are an integral part of this part of ISO 10303. Annexes C, D, E, F, and G are for information only.

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Introduction

ISO 10303 is an International Standard for the computer-interpretable representation and exchange of product data. The objective is to provide a neutral mechanism capable of describing product data throughout the life cycle of a product independent from any particular system. The nature of this description makes it suitable not only for neutral file exchange, but also as a basis for implementing and sharing product databases and archiving.

This International Standard is organized as a series of parts, each published separately. The parts of ISO 10303 fall into one of the following series: description methods, integrated resources, application interpreted constructs, application protocols, abstract test suites, implementation methods, and conformance testing. The series are described in ISO 10303–1. This part of ISO 10303 is a member of the integrated resources series. Major subdivisions of this International Standard are:

- kinematic structure;
- kinematic motion representation;
- kinematic analysis control and results.

This part of ISO 10303 specifies an information model for the kinematic aspects of a mechanical product as required for the communication between CAD systems and kinematic analysis systems, and among dissimilar kinematic analysis systems. Kinematic information in the context of this part of ISO 10303 may be used in:

- early design stages, where detailed component shape is yet undetermined. The purpose of the kinematic description in these stages is to develop the conceptual model of the mechanical product to understand its motion characteristics;
- detail design stage where detailed shapes of components are determined. The purpose of the kinematic description in that stage is to verify the performance of the kinematic characteristics of a mechanical product using the final shape of its components, e.g., by means of collision checking.

The kinematic structure in this part of ISO 10303 is composed of rigid components related by kinematic pairs along a surface, on a curve, or at a point.

The kinematic structure schema defines the kinematic structure of rigid objects in terms of links, pairs, and joints. A link is the rigid part of a kinematic object. A pair represents the geometric aspects of the kinematic constraints of motion of these objects, and a joint represents the topological aspects of these constraints. The kinematic structures are represented by graphs in which the vertices of the graph correspond to the links, and the edges of the graph correspond to the joints.

The kinematic motion representation schema specifies the motion of a mechanical product by using a parametric path definition.

The kinematic analysis control and result schema specifies configurations of kinematic structures and the interpolation between configurations. This schema describes prescribed paths for a kinematic analysis and paths resulting from such a kinematic analysis.

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Figure 1 illustrates these three schemas and the types and entities that are defined in one schema and referenced by another.

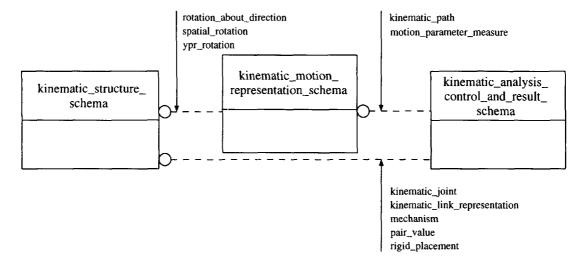


Figure 1 - The relationships between the three schemas of ISO 10303-105: Kinematics

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Industrial automation systems and integration — Product data representation and exchange — Part 105: Integrated application resource: Kinematics

1 Scope

This part of ISO 10303 specifies the resource constructs for the representation of the kinematic aspects of a mechanical product.

The following are within the scope of this part of ISO 10303:

- definition of kinematic relationships between rigid objects called links;
- representation of the topology for a kinematic structure;
- definition of a kinematic motion as a sequence of discretised positions and orientations;
- representation of the input to and the result of a kinematic analysis.

The following are outside the scope of this part of ISO 10303:

- description of tolerances and clearances in kinematic structures;
- description of motion parameters in terms of a continuous time variable;
- representation of intermittent joints with variable constraints on motion;
- representation of dynamic mechanical assemblies;
- representation of force, mass, and friction.

2 Normative references

The following standards contain provisions which, through reference in this text, constitute provisions of this part of ISO 10303. At the time of publication, the editions indicated were valid. All standards are subject to revision, and parties to agreements based on this part of ISO 10303 are encouraged to investigate the possibility of applying the most recent editions of the standards indicated below. Members of IEC and ISO maintain registers of currently valid International Standards.

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ISO/IEC 8824-1:1995, Information technology - Abstract Syntax Notation One (ASN.1): Specification of basic notation.

ISO 8855:1991, Road vehicles - Vehicle dynamics and road-holding ability - Vocabulary.

ISO 10303-1:1994, Industrial automation systems and integration - Product data representation and exchange - Part 1: Overview and fundamental principles.

ISO 10303-11:1994, Industrial automation systems and integration - Product data representation and exchange - Part 11: Description methods: The EXPRESS language reference manual.

ISO 10303-21:1994, Industrial automation systems and integration - Product data representation and exchange - Part 21: Implementation methods: Clear text encoding of the exchange structure.

ISO 10303-41:1994, Industrial automation systems and integration - Product data representation and exchange - Part 41: Integrated generic resources: Fundamentals of product description and support.

ISO 10303-42:1994, Industrial automation systems and integration - Product data representation and exchange - Part 42: Integrated generic resources: Geometric and topological representation.

ISO 10303-43:1994, Industrial automation systems and integration - Product data representation and exchange - Part 43: Integrated generic resources: Representation structures.

3 Definitions

3.1 Terms defined in ISO 10303-1

This part of ISO 10303 makes use of the following terms defined in ISO 10303-1:

- application resource;
- data;
- generic resource;
- information;
- integrated resource;
- product.

3.2 Terms defined in ISO 10303-42

This part of ISO 10303 makes use of the following terms defined in ISO 10303-42:

geometric coordinate system;

2

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- geometrically founded;
- graph.

3.3 Terms defined in ISO 8855

This part of ISO 10303 makes use of the following terms defined in ISO 8855:

- pitch angle;
- roll angle;
- yaw angle.

3.4 Other definitions

For the purposes of this part of ISO 10303, the following definitions apply.

- **3.4.1** base: a link which is fixed to the ground or whose motion is prescribed along a defined path.
- **3.4.2 frame:** a coordinate system used in kinematic representations.
- 3.4.3 ground: the immobile part of a mechanical product in the world coordinate system.
- **3.4.4 joint:** the topological aspect of an ordered connection or motion constraint between two and only two links.
- **3.4.5** kinematics: the description of movable mechanical structures consisting of joints and links including the number, location, and orientation of the joints.
- 3.4.6 kinematic chain: a sequence of kinematic links connected by joints.
- 3.4.7 link: a rigid kinematic object whose motion is constrained by one or more joints.
- 3.4.8 link frame: the local coordinate system of a link, implicitly defined as the geometric context of the link, with respect to which all geometric definitions of the link are defined.
- **3.4.9 loop:** a part of a mechanical structure whose joints and links together form a closed kinematic chain.
- 3.4.10 mechanism: a mechanical product whose motion is constrained by joints.
- **3.4.11 motion:** change of position and orientation of a rigid body.
- **3.4.12 pair:** the geometric aspect of either an ordered connection or motion constraint between two and only two links.

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- 3.4.13 pair actuation: the assignment of a pair value to a kinematic pair by an application.
- 3.4.14 placement: the location and orientation of a frame.
- **3.4.15 transform:** a representation of a placement that is specified with respect to an independent reference frame.
- 3.4.16 SU-parameters: the parameters that specify the placement between a pair of frames.
- 3.4.17 world coordinate system: the initial coordinate system from which all other frames are defined.

4 Symbols and abbreviations

For the purposes of this part of ISO 10303, the following symbols and abbreviations apply.

4.1 Mathematical symbols

The mathematical symbol convention used in this part of ISO 10303 is given in table 1.

4.2 Graphic convention for matrix representation

In mathematical formulas, a transform representation (three position values and three rotation values) is written as BOLD capital letters.

4.3 Abbreviations

SU

Sheth-Uicker

ypr

rotation angles called yaw, pitch, and roll.

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Table 1 - Mathematical symbology

Symbol	Definition
a	Scalar quantity a
\overline{a}	Vector quantity \overline{a}
x,y,z	Coordinate axes
$\overline{x},\overline{y},\overline{z}$	Unit vectors along coordinate axes
F	Matrix F
F^{-1}	The inverse of the matrix F
×	Vector (cross) product
•	Scalar product
f(u)	Parametric curve f
$\left f(u) \right _{u=u_p} = f(u_p)$	Value of $f(u)$ at the point denoted by p
$rac{df(u)}{du}$	Derivative of $f(u)$ with respect to u
f(u,v)	Parametric surface f
$\left f(u,v) \right _{u=u_p,v=v_p}$	Value of $f(u, v)$ at the point denoted by p
$rac{\partial f(u,v)}{\partial u}$	Partial differential of f with respect to u
$x \in \left]a,b ight]$	x is element of the range between a (excluded) and b (included)
sign(x)	Function returns the sign of the argument x
11	Absolute value, or magnitude, or determinant
R^m	m-dimensional real space

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5 Kinematic structure

The following EXPRESS declaration begins the kinematic_structure_schema and identifies the necessary references.

```
EXPRESS specification:
```

```
*)
SCHEMA kinematic_structure_schema;
REFERENCE FROM geometry_schema
    (axis2_placement_3d,
     cartesian_transformation_operator_3d,
     curve,
     direction,
     geometric_representation_context,
     normalise,
     point,
     point_on_curve,
     point_on_surface,
     surface,
     rectangular_trimmed_surface,
     trimmed_curve);
REFERENCE FROM measure_schema
    (conversion_based_unit,
     global_unit_assigned_context,
     length_measure,
     plane_angle_measure,
     si_prefix,
     si_unit,
     si_unit_name,
     unit);
REFERENCE FROM product_property_definition_schema
    (characterized_definition,
     property_definition);
REFERENCE FROM product_property_representation_schema
    (property_definition_representation);
REFERENCE FROM representation_schema
    (functionally_defined_transformation,
     item_defined_transformation,
     representation,
     representation_context,
     representation_item,
     representation_relationship,
     representation_relationship_with_transformation);
REFERENCE FROM support_resource_schema
    (bag_to_set,
```

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label);

(*

NOTES

1 - The schemas referenced above can be found in the following parts of ISO 10303:

geometry_schema	ISO 10303-42
measure_schema	ISO 10303-41
product_property_definition_schema	ISO 10303-41
$product_property_representation_schema$	ISO 10303-41
representation_schema	ISO 10303-43
support_resource_schema	ISO 10303-41

2 – See annex D for a graphical representation of this schema using the EXPRESS-G notation.

5.1 Introduction

The subject of the kinematic_structure_schema is the description of the kinematic information of a mechanical product defining its motion capabilities.

Motion in this part of ISO 10303 comprises both free, unconstrained motion of objects in a Cartesian coordinate system and motion constrained by kinematic joints and pairs.

This part of ISO 10303 covers the following types of pairs.

- 1) revolute pair;
- 2) prismatic pair;
- 3) screw pair;
- 4) cylindrical pair;
- 5) spherical pair;
- 6) universal pair;
- 7) planar pair;
- 8) gear pair;
- 9) rack and pinion pair;
- 10) unconstrained pair;
- 11) fully constrained pair;
- 12) point on surface pair;

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- 13) sliding surface pair;
- 14) rolling surface pair;
- point on planar curve pair; 15)
- sliding curve pair; 16)
- rolling curve pair.

Pair types 1 through 11 are called low order pairs and the remaining pair types are called high order pairs.

NOTE - Pair types 1 through 11 do not require explicit geometric information to describe their kinematic behaviour. Pair types 12 through 17 require a reference to a surface or to a curve in order to be defined kinematically.

For surface pairs and curve pairs, two specialisations are distinguished: the sliding and rolling subtypes. A rolling pair is constrained in the relative motion of the two surfaces or curves such that they cannot slide on each other.

EXAMPLE 1 - High levels of friction between two surfaces or curves may be the cause for relative motion to be constrained to rolling.

For sliding pairs such a constraint does not exist.

Low order pairs can be represented as sliding high order pairs. If a pair can be represented as a low order pair, it should be so represented and not as a high order pair.

5.2 Fundamental concepts and assumptions

5.2.1 Kinematic model structure

Mechanical products with kinematic representations may have arbitrary topological structures. The topological structures are not constrained to simple chains (i.e., open kinematic chains without branches) or to tree-type structures; they may include loops or a network structure.

NOTE - Every kinematic structure can be described in terms of its joints and links. Joints constrain the motion between two rigid objects called links. Joints and links are sufficient to describe the topology of kinematic structures, but for computation it is meaningful to introduce additional levels of structure based on graph theory. Information related to the graph representation of a kinematic structure is given in 5.4.70.

EXAMPLES

- 2 Simple chains are suitable kinematic structures for many industrial robots or cranes. Tree-type structures are used to represent multi-arm manipulators.
- 3 Network structures occur in industrial products. One example is the mechanism used for windscreen wipers.

In this part of ISO 10303, kinematic structures are represented by graphs where the links represent the vertices of the graph, and the joints represent the edges. The rigid objects with kinematic representations are defined kinematically in terms of links and geometrically in terms of their associated shape representation. All coordinate systems related to a kinematic link are founded in the link frame, which is the geometric context of the related link representation. These coordinate systems are called frames in this part of ISO 10303. For the purpose of representing the kinematic aspect of a mechanism, the shape of the link is represented by the relative location and orientation of all its pair frames with respect to its link frame.

5.2.2 Positioning and placement

Whenever constraints are imposed on the relative motion of two kinematic links, this fact is topologically represented by a joint. The geometric aspect of this motion constraint is represented by the corresponding pair.

A placement describes a relative position and orientation of a frame with respect to another frame. There are different ways of representing a placement. Eight different representations of placement are used in this part of ISO 10303:

- rigid homogenous matrix;
- axis2_placement_3d;
- **transform** (see 6.4.2);
- su_parameters;
- point_on_curve;
- point_on_surface;
- a pair type with its initial_state;
- cartesian_transformation_operator_3d.

The rigid homogeneous matrix is used only as a notation in mathematical formulas. It defines the relative position and orientation of one frame with respect to another. The terms of this matrix are as follows:

$$^{k}m{P}_{i}=egin{bmatrix} 3 imes3 & \delta x\ rotational & \delta y\ matrix & \delta z\ 0 & 0 & 0 & 1 \end{bmatrix}$$

where the notation used for a frame **P** shall be kP_i with:

k = identification of the reference frame in which the position of frame i is described; i = identification of the frame whose position is described with respect to frame k; δx , δy , $\delta z = \text{the components of the translation vector.}$

 ${}^{0}P_{i}$ represents the placement relative to the world coordinate system.

The transform includes three rotational and three translational components. The transform is the only form of placement representation which is suitable for interpolation or approximation via weighting functions.

The remaining representations are described in the schema.

5.2.3 Positive sense of rotations

For any rotation defined in the **kinematic_structure_schema**, a positive value of the rotation angle indicates a counter-clockwise rotation when looking in the negative direction with respect to the axis of that rotation.

5.2.4 Shape representations

Kinematic structure representations are frequently associated with shape representations for single parts of the structure at various levels of detail. In this part of ISO 10303, three kinds of shape representations are distinguished:

- shape representations of parts that belong to the immobile environment of a kinematic structure, referred to as the *ground shape*;
- shape representations describing the shape of a link of a kinematic structure, referred to as the *link shape*;
- shape representations describing specific aspects of the shape of a kinematic pair, referred to as the pair shape.

The geometric_representation_items which contribute to the ground shape representation may be in the items set either of the kinematic_ground_representation of the kinematic structure which, in this case, should be simultaneously a shape_representation, or of a shape_representation which is related to the kinematic_ground_representation of the kinematic structure by any means. This part of ISO 10303 does not specify any specific constraints on the representation of ground shape.

The **geometric_representation_items** contributing to a link shape representation shall not be in the **items** set of the corresponding **kinematic_link_representation**; rather they shall be in the **items** set of a **shape_representation** which is related to this **kinematic_link_representation** by means of a **kinematic_link_representation_association**. Any number of **shape_representations** may be related in this way to a specific **kinematic_link_representation**.

For the purpose of a pair shape representation, only geometric_representation_items of type kinematic_frame_background, i.e., point, curve, or surface are allowed. They shall be in the items set of a kinematic_frame_background_representation which, in turn, is related to one of the kinematic_link_representations of the pair by means of a kinematic_frame_background_representation_association. The items set of a kinematic_frame_background_representation may contain more than one item, and in general any number of

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kinematic_frame_background_representations may be related to a kinematic_link_representation and to any frame in its items set. In the case of the higher pair types, however, which need explicit geometric information to describe their kinematic behaviour, at least one kinematic_frame_background_representation is required for each curve or surface that is referenced in its specification.

5.2.5 Consistent use of units

It is required that units are used consistently throughout a kinematic structure, although such a kinematic structure will include a variety of representations and related representation_contexts. To ensure this consistency, it is further required that all units which are to be used in a kinematic structure are assigned globally to the items of the respective representations by means of the global_unit_assigned_context subtype of the representation_context (see ISO 10303-41). Units for measure_values of the same kind shall be identical throughout all the representations in a kinematic structure.

EXAMPLE 4 - The pair placements of a kinematic_pair are founded in two different kinematic_link_representations. Consistent use of units requires that these two kinematic_link_representations share the same units via their global_unit_assigned_contexts.

5.3 kinematic_structure_schema type definitions

5.3.1 rigid_placement

The **rigid_placement** type is a means for referencing either an **axis2_placement_3d** or **su_parameters**.

EXPRESS specification:

```
*)
TYPE rigid_placement = SELECT
  (axis2_placement_3d,
    su_parameters);
END_TYPE;
(*
```

5.3.2 rotational_range_measure

The rotational_range_measure type is a means for referencing either a plane_angle_measure or an unlimited_range.

EXPRESS specification:

```
*)
TYPE rotational_range_measure = SELECT
  (plane_angle_measure,
    unlimited_range);
END_TYPE;
```

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5.3.3 translational_range_measure

The translational_range_measure type is a means for referencing either a length_measure or an unlimited_range.

EXPRESS specification:

```
*)
TYPE translational_range_measure = SELECT
  (length_measure,
    unlimited_range);
END_TYPE;
(*
```

5.3.4 unlimited_range

The unlimited_range type is a means by which an unlimited value can be assigned to a range bound of a pair.

$\it EXPRESS$ specification:

```
*)
TYPE unlimited_range = ENUMERATION OF
  (unlimited);
END_TYPE;
(*
```

Enumerated item definitions:

unlimited: an indication that the range bound is unlimited.

5.3.5 spatial_rotation

The spatial_rotation type enables an arbitrary rotation in 3D space (R^3) to be specified either as a ypr_rotation or as a rotation_about_direction.

EXPRESS specification:

```
*)
TYPE spatial_rotation = SELECT
  (ypr_rotation,
    rotation_about_direction);
END_TYPE;
(*
```

5.3.6 ypr_enumeration

The **ypr_enumeration** is a means by which the angles of rotation about the origin in Cartesian coordinate space \mathbb{R}^3 are distinguished. Yaw represents the angle by which the original frame (x_0, y_0, z_0) is rotated first about the z-axis to yield an intermediate (x', y', z') frame. Pitch represents the angle by which the intermediate frame (x', y', z') then is rotated about the y'-axis to yield another intermediate (x'', y'', z'') frame. Roll represents the angle by which the (x'', y'', z'') frame is rotated about the x''-axis to yield the desired final (x, y, z) frame.

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NOTE – For more detailed information on yaw, pitch, and roll convention see ISO 8855:1991 (clause 2.2).

EXPRESS specification:

```
*)
TYPE ypr_enumeration = ENUMERATION OF
  (yaw,
  pitch,
  roll);
END_TYPE;
(*
```

Enumerated item definitions:

yaw: the angle of rotation about the z-axis.

pitch: the angle of rotation about the y'-axis.

roll: the angle of rotation about the x"-axis.

5.3.7 ypr_rotation

The **ypr_rotation** type is a means for specifying an ordered sequence of the angles of rotation. The **yaw** value is the first, the **pitch** value the second, and the **roll** value the last element in the array. The yaw rotation shall be performed first, followed by the pitch rotation. The roll rotation shall be performed as the last action of a **ypr_rotation**.

NOTE – An *EXPRESS* function which returns the rotation matrix corresponding to an input **ypr_rotation** is given in annex E. This function has been provided for applications that use this part of ISO 10303, but need the rotational transformation to be expressed in terms of a rotation matrix rather than in terms of a sequence of rotation angles.

EXPRESS specification:

```
*)

TYPE ypr_rotation = ARRAY [ypr_index(yaw) : ypr_index(roll)]

OF plane_angle_measure;

END_TYPE;

(*
```

Informal propositions:

angle bounds: The values of the yaw, pitch, and roll angle shall be in the ranges equivalent to the following ranges, where the angles are measured in radians:

```
yaw \ angle \in ]-\pi,\pi]

pitch \ angle \in [-\pi/2,\pi/2]

roll \ angle \in ]-\pi,\pi]
```

rectangular pitch angle: If the absolute value of the pitch angle is equal to the equivalent value of $\pi/2$, the roll angle shall be zero.

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kinematic_frame_background 5.3.8

The kinematic_frame_background type is a means for referencing either a point, a curve, or a surface.

EXPRESS specification:

```
*)
TYPE kinematic_frame_background = SELECT
  (point,
   curve,
   surface);
END_TYPE;
(*
```

kinematic_structure_schema entity definitions

rotation_about_direction 5.4.1

A rotation_about_direction specifies a rotation in Cartesian coordinate space R^3 . The axis of rotation passes the origin of the related coordinate system; its direction is given explicitly as direction_of_axis. Furthermore, the amount of rotation is specified by rotation_angle which may have any finite value; i.e., its absolute value in radians is not restricted to be less than π . A positive value of rotation_angle indicates a counter-clockwise rotation when looking in the negative direction with respect to the direction_of_axis.

EXPRESS specification:

```
*)
ENTITY rotation_about_direction;
  direction_of_axis : direction;
                    : plane_angle_measure;
  rotation_angle
  WR1: SIZEOF (direction_of_axis.direction_ratios) = 3;
END_ENTITY;
```

Attribute definitions:

direction_of_axis: the three-dimensional direction of the axis of rotation.

rotation_angle: the angle of rotation about the axis of rotation.

Formal propositions:

WR1: The direction_of_axis shall be a three-dimensional direction.

5.4.2kinematic_property_definition

The kinematic_property_definition specifies the kinematic property of a product.

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EXPRESS specification:

```
*)
ENTITY kinematic_property_definition
  SUBTYPE OF (property_definition);
  ground_definition : characterized_definition;
END_ENTITY;
(*
```

Attribute definitions:

ground_definition: the characterized_object, characterized_product_definition, or shape_definition related to the kinematic_ground_representation which is associated with the kinematic_property_definition.

NOTE – The **ground_definition** may be a **characterized_object** if it does not need to be associated with a product definition.

5.4.3 kinematic_property_representation_relation

A kinematic_property_representation_relation is a property_definition_representation that relates a kinematic_ground_representation to a kinematic_property_definition.

EXPRESS specification:

```
*)
ENTITY kinematic_property_representation_relation
   SUBTYPE OF (property_definition_representation);
UNIQUE
   UR1: SELF\property_definition_representation.definition;
WHERE
   WR1: 'KINEMATIC_STRUCTURE_SCHEMA.KINEMATIC_PROPERTY_DEFINITION'
        IN TYPEOF (SELF\property_definition_representation.definition);
WR2: 'KINEMATIC_STRUCTURE_SCHEMA.KINEMATIC_GROUND_REPRESENTATION'
        IN TYPEOF (SELF\property_definition_representation.used_representation);
END_ENTITY;
(*
```

Formal propositions:

UR1: A kinematic_property_definition shall be related to a kinematic_ground_representation by at most one kinematic_property_representation_relation.

WR1: The definition of a kinematic_property_representation_relation shall be a kinematic_property_definition.

WR2: The used_representation of a kinematic_property_representation_relation shall be a kinematic_ground_representation.

5.4.4 kinematic_ground_representation

A kinematic_ground_representation specifies the world coordinate system.

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NOTE - A shape_representation may be given together with a kinematic_ground_representation to specify the shape of those parts of a kinematic_property_definition that are immobile.

EXPRESS specification:

```
*)
ENTITY kinematic_ground_representation
   SUBTYPE OF (representation);
INVERSE
   property : kinematic_property_representation_relation FOR used_representation;
WHERE
   WR1: 'GEOMETRY_SCHEMA.GEOMETRIC_REPRESENTATION_CONTEXT' IN
        TYPEOF (SELF\representation.context_of_items);
END_ENTITY;
(*
```

Attribute definitions:

SELF\representation.items: a set of representation_items that are related in the context_of_items.

ground_context: the identification of a world coordinate system against which all placements in the kinematic_property_definition are measured, either directly or indirectly.

property: the kinematic_property_representation_relation that relates the kinematic_ground_representation to the kinematic_property_definition to which it belongs.

Formal propositions:

WR1: The context_of_items of a kinematic_ground_representation shall always be a geometric_representation_context.

Informal propositions:

ground definition: The kinematic_ground_representation shall be associated to property_property_definition_representation.definition.ground_definition.

5.4.5 mechanism

A mechanism specifies the capabilities of relative motion of its links under the constraints imposed by its joints. It is a kinematic structure with a single link fixed to the ground or to some other mechanism. The entire mechanism may be subject to the rigid body motion imposed to its base.

NOTE – A mechanism may have different bases at different times. In space applications, worm-like mechanisms have been designed which grab to a space-structure with one end, move on with the other end, fix themselves with an end-effector establishing a new base, and then loosen the original grip.

EXPRESS specification:

```
*)
ENTITY mechanism;
structure_definition : kinematic_structure;
base : kinematic_link;
```

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Attribute definitions:

structure_definition: the topological structure of the mechanism.

base: the initial link of the mechanism.

containing_property: the kinematic_property_definition to which the mechanism belongs.

Formal propositions:

WR1: The base shall be either the first link or the second link in at least one joint in the set structure_definition.joints. This ensures that the base is within the kinematic structure.

5.4.6 mechanism_base_placement

A mechanism_base_placement is a means to define the placement of the link frame of the base of a mechanism either relative to the world coordinate system or relative to the local coordinate system of a link that belongs to another mechanism.

NOTE 1 – If the placement is defined relative to the link of another **mechanism**, the **mechanism** whose **base** is being placed is said to be mounted on the other **mechanism**.

If the placement is defined relative to the world coordinate system, mechanism_base_placement relates the link frame of the base in the context_of_items of a kinematic_ground_representation. If the placement is defined relative to the local coordinate system of another link, mechanism_base_placement relates the link frame of the base in the link_frame of the kinematic_link_representation which is associated with this other link.

EXPRESS specification:

```
*)
ENTITY mechanism_base_placement
  SUBTYPE OF (representation_relationship_with_transformation);
  base_of_mechanism
                            : mechanism;
  SELF\representation_relationship_with_transformation.
   transformation_operator : cartesian_transformation_operator_3d;
DERIVE
  SELF\representation_relationship.rep_2
                            : kinematic_link_representation
                            := representation_of_link (base_of_mechanism.base);
UNIQUE
  UR1: base_of_mechanism;
WHERE
  WR1: ('KINEMATIC_STRUCTURE_SCHEMA.KINEMATIC_GROUND_REPRESENTATION' IN
         TYPEOF (SELF\representation_relationship.rep_1))
```

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Attribute definitions:

base_of_mechanism: the mechanism whose base is being placed.

SELF\representation_relationship_with_transformation.transformation_operator: the transformation between the context of rep_1 and the context of rep_2.

NOTE 2 - Legal values for the attributes of the cartesian_transformation_operator_3d that is used as the transformation_operator, are specified in application protocols which use this entity.

SELF\representation_relationship.rep_2: the kinematic_link_representation that is related to the base of base_of_mechanism. This is derived from base_of_mechanism.base by the function representation_of_link.

Formal propositions:

UR1: A mechanism shall be the base_of_mechanism for at most one mechanism_base_placement.

WR1: The rep_1 of a mechanism_base_placement shall be a kinematic_ground_representation or a kinematic_link_representation.

WR2: The mechanism_base_placement shall place the base of base_of_mechanism either with respect to the kinematic_ground_representation which is associated with its containing_property, or with respect to a kinematic_link_representation that belongs to another mechanism. This other mechanism shall also be in the mechanisms set of containing_property. In this way, the base of base_of_mechanism shall be placed with respect to the kinematic_ground_representation, directly or indirectly. If the placement is done indirectly, a mechanism shall not participate in the placement of its own base. These conditions are checked by the function suitably_based_mechanism.

WR3: The cartesian_transformation_operator_3d that is used as the transformation_operator in a mechanism_base_placement shall be in the items set of rep_1.

5.4.7 initial_state

The initial_state specifies initial values of the pair parameters of a mechanism.

NOTE - Some types of kinematic structures, such as four bar linkages, can only be assembled uniquely if configuration information is provided in addition to shape parameters, such as link

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lengths. In those cases the **initial_state** provides enough pair parameter information to make the configuration unique.

EXPRESS specification:

Attribute definitions:

applies_to_mechanism: the mechanism to which the initial_state applies.

pair_values: the pair parameter values of each pair in the mechanism.

Formal propositions:

WR1: An initial_state shall provide in its set of pair_values exactly one pair_value for each kinematic_pair in the mechanism to which it applies.

5.4.8 kinematic structure

The kinematic_structure specifies the topological aspects of a kinematic representation. The topology of the kinematic_structure is represented by means of kinematic_joints which, in turn, establish a relationship between pairs of kinematic_links.

NOTE – Every kinematic structure can be described in terms of its joints and links. Joints constrain the motion between two rigid objects called links. Joints and links are sufficient to describe the topology of kinematic structures, but for computation it is meaningful to introduce additional levels of structure based on graph theory. Information related to the graph representation of a kinematic structure is given in 5.4.70.

EXPRESS specification:

```
*)
ENTITY kinematic_structure;
  joints : SET [1 : ?] OF kinematic_joint;
END_ENTITY;
(*
```

Attribute definitions:

joints: the set of kinematic_joints that compose the kinematic_structure of a mechanism.

5.4.9 kinematic_joint

The **kinematic_joint** specifies the topological aspect of an ordered connection between two and only two links.

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A topological orientation is always implicitly associated with a joint. This orientation is defined as being from the first link to the second link.

For a kinematic_pair referencing a kinematic_joint, the pair_placement_in_first_link_context shall be an item of the kinematic_link_representation of the first_link of the kinematic_joint.

Similarly, the pair_placement_in_second_context shall be an item of the kinematic_link_representation of the second_link of the kinematic_joint.

NOTES

- 1 The type of constraint on the relative motion is defined by the **kinematic_pair** that has the joint as its **joint** attribute. In a graph representation of the topology, the **kinematic_joint** represents an oriented edge connecting two vertices in the graph. The orientation of the **kinematic_joint** reflects an implicit orientation which is arbitrary, except for the rack-and-pinion pair, the point-on-surface pair, and the point-on-planar-curve pair.
- 2 If the sequence of **first_link** and **second_link** is interchanged, both, pair values and pair range values, have to be used with the opposite signs, and in the subtypes of **simple_pair_range** additionally the attributes giving a lower limit are to be interchanged with those giving the corresponding upper limit.

EXPRESS specification:

```
*)
ENTITY kinematic_joint;
  first_link : kinematic_link;
  second_link : kinematic_link;
INVERSE
   structure : kinematic_structure FOR joints;
WHERE
  WR1: first_link :<>: second_link;
END_ENTITY;
(*
```

Attribute definitions:

first_link: the link through which the joint is entered.

second_link: the link through which the joint is left.

structure: the kinematic_structure containing the kinematic_joint in its set of joints.

Formal propositions:

WR1: first_link and second_link shall not be identical.

5.4.10 kinematic_link

A kinematic_link represents the topological aspects associated with a rigid part of a mechanism.

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EXPRESS specification:

Formal propositions:

WR1: A kinematic_link shall be the first_link or the second_link of at least one kinematic_joint.

WR2: A kinematic_link shall be a constituent of one mechanism only and shall occur only once in the kinematic structure of that mechanism.

5.4.11 kinematic_link_representation_relation

A kinematic_link_representation_relation relates the geometric aspects of a kinematic_link with its topological aspects.

EXPRESS specification:

```
*)
ENTITY kinematic_link_representation_relation;
  topological_aspects : kinematic_link;
  geometric_aspects : kinematic_link_representation;
UNIQUE
  UR1: topological_aspects;
END_ENTITY;
(*
```

Attribute definitions:

topological_aspects: the kinematic_link whose geometric aspects are represented by the kinematic_link_representation.

geometric_aspects: the representation of the context of the rigid part of a mechanical product and of the frames related to it for a **kinematic_link**.

Formal propositions:

UR1: A kinematic_link shall be related to a kinematic_link_representation by at most one kinematic_link_representation_relation.

5.4.12 kinematic_link_representation

A kinematic_link_representation specifies the geometric aspects of a kinematic_link. The context of the representation is established by the link_frame attribute.

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EXPRESS specification:

```
*)
ENTITY kinematic_link_representation
 SUBTYPE OF (representation);
  SELF\representation.context_of_items : geometric_representation_context;
DERIVE
  link_frame
                               : geometric_representation_context
                               := SELF\representation.context_of_items;
INVERSE
  link_representation_relation : kinematic_link_representation_relation FOR
                                 geometric_aspects;
WHERE
  WR1: SIZEOF (QUERY (item <* SELF\representation.items |
               NOT (('KINEMATIC_STRUCTURE_SCHEMA.RIGID_PLACEMENT' IN
                      TYPEOF (item))
                    ΛR
                    ('GEOMETRY_SCHEMA.CARTESIAN_TRANSFORMATION_OPERATOR_3D' IN
                      TYPEOF (item)))) = 0;
END_ENTITY;
```

Attribute definitions:

SELF\representation.items: a set of representation_items that are related in the link_frame. It contains at least one pair frame that is used by a kinematic_pair as pair_placement_in_first_link_context or as pair_placement_in_second_link_context. It may contain any number of cartesian_transformation_operator_3ds which serve as the transformation_operator of a mechanism_base_placement. Furthermore, it may contain additional frames that are attached to the link.

NOTE – The items set of a kinematic_link_representation does not contain geometric_representation_items that define the shape of the link.

SELF\representation.context_of_items: the **geometric_representation_context** providing the context for the **items**.

link_frame: the link frame of the related kinematic_link.

link_representation_relation: the kinematic_link_representation_relation that relates a kinematic_link to the kinematic_link_representation.

Formal propositions:

WR1: All elements in the items set of a kinematic_link_representation shall be of type rigid_placement or of type cartesian_transformation_operator_3d.

5.4.13 kinematic_link_representation_association

A kinematic_link_representation_association is a representation_relationship that associates a representation with a kinematic_link_representation.

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NOTE - A kinematic_link_representation_association is used to define the shape of a link by associating a shape_representation to the corresponding kinematic_link_representation.

EXPRESS specification:

Attribute definitions:

SELF\representation_relationship.rep_1: the kinematic_link_representation with which rep_2 is associated.

Formal propositions:

WR1: The context_of_items of rep_2 shall be identical to the link_frame of the kinematic_link_representation with which rep_2 is associated.

WR2: Neither a kinematic_ground_representation nor a kinematic_link_representation shall be associated with a kinematic_link_representation by this entity.

5.4.14 kinematic_frame_background_representation

A kinematic_frame_background_representation specifies the shape aspects which are associated with a kinematic_pair.

EXPRESS specification:

```
*)

ENTITY kinematic_frame_background_representation

SUBTYPE OF (representation);

SELF\representation.items : SET [1 : ?] OF

kinematic_frame_background;

SELF\representation.context_of_items : geometric_representation_context;

WHERE

WR1: SELF\representation.context_of_items\

geometric_representation_context.coordinate_space_dimension = 3;

END_ENTITY;

(*
```

Attribute definitions:

SELF\representation.items: a set of instances of kinematic_frame_background which specify shapes that are to be associated with a kinematic_pair.

SELF\representation.context_of_items: the context in which the items are founded.

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Formal propositions:

WR1: The context_of_items of a kinematic_frame_background_representation shall be three-dimensional.

5.4.15 kinematic_frame_based_transformation

The kinematic_frame_based_transformation is a functionally_defined_transformation which uses a rigid_placement as the transformation function.

EXPRESS specification:

```
*)
ENTITY kinematic_frame_based_transformation
SUBTYPE OF (functionally_defined_transformation);
transformer_frame : rigid_placement;
END_ENTITY;
(*
```

Attribute definitions:

transformer_frame: the rigid_placement which is used as the transformation function for the kinematic_frame_based_transformation.

5.4.16 kinematic_frame_background_representation_association

A kinematic_frame_background_representation_association is a representation_relationship_with_transformation which uses a kinematic_frame_based_transformation as the transformation_operator. The transformer_frame of this operator is founded in the kinematic_link_representation used as rep_1; the representation being transformed is a kinematic_frame_background_representation which is referenced by rep_2.

EXPRESS specification:

```
*)
ENTITY kinematic_frame_background_representation_association
  SUBTYPE OF (representation_relationship_with_transformation);
  SELF\representation_relationship_with_transformation.
    transformation_operator : kinematic_frame_based_transformation;
WHERE
  WR1: 'KINEMATIC_STRUCTURE_SCHEMA.KINEMATIC_LINK_REPRESENTATION' IN
         TYPEOF (SELF\representation_relationship.rep_1);
  WR2: 'KINEMATIC_STRUCTURE_SCHEMA.KINEMATIC_FRAME_BACKGROUND_REPRESENTATION'
         IN TYPEOF (SELF\representation_relationship.rep_2);
  WR3: SELF\representation_relationship_with_transformation.
           transformation_operator\kinematic_frame_based_transformation.
           transformer_frame\representation_item IN
         SELF\representation_relationship.rep_1.items;
END_ENTITY;
(*
```

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Attribute definitions:

SELF\representation_relationship_with_transformation.transformation_operator: the transformation operator for the kinematic_frame_background_representation_association.

Formal propositions:

WR1: The first representation related in a kinematic_frame_background_representation_association shall be a kinematic_link_representation.

WR2: The second representation related in a kinematic_frame_background_representation_association shall be a kinematic_frame_background_representation.

WR3: The rigid_placement which serves as the transformer_frame in the transformation_operator of a kinematic_frame_background_representation_association shall be in the items set of the kinematic_link_representation used as rep_1.

5.4.17su_parameters

su_parameters are an alternative method to axis2_placement_3d for specifying the placement of pairs on a link.

To describe the kinematic behaviour, the full shape representation of a link is not needed; rather it is sufficient to characterize the link by the transition from the link frame to all the pair frames. This shape information is captured by a set of characteristic parameters called Sheth-Uicker-Parameters, henceforth abbreviated "SU-parameters".

NOTE 1 - See figure 2. For a kinematic link with two pairs and for the link frame coinciding with the frame of one of the pairs, this may be interpreted as the transition from the frame at the beginning of the link to the frame at the following end.

The following notation is used for frame definitions:

coordinate axes of a link frame; x_k^r, y_k^r, z_k^r

origin of that link frame;

axes of the frame of a kinematic pair on that link; x_k, y_k, z_k

origin of that pair frame.

The following auxiliary vectors are introduced:

 \bar{t}_k unit vector along the common perpendicular between the two axes z_k^r and z_k , directed from z_k^r towards z_k . The common perpendicular itself is denoted by

 \overline{s}_k^r intersection point of the common perpendicular t_k with z_k^r ;

intersection point of the common perpendicular t_k with z_k .

Then the following notation applies to SU-parameters:

the (positive) distance from z_k^r to z_k , given by a_k

$$a_k = |\overline{s}_k - \overline{s}_k^r|$$

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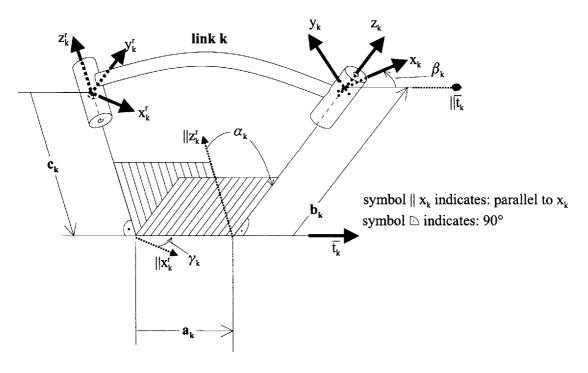


Figure 2 – Definition of the su_parameters

 α_k the angle from positive z_k^r to positive z_k , measured in the mathematically positive sense about \bar{t}_k and determined by

$$\sin \alpha_k = (\overline{z}_k^r \times \overline{z}_k) \cdot \overline{t}_k; \qquad \cos \alpha_k = \overline{z}_k^r \cdot \overline{z}_k$$

 b_k the deviation of \bar{o}_k from \bar{s}_k , measured along positive z_k and given by

$$b_k = (\overline{o}_k - \overline{s}_k) \cdot \overline{z}_k$$

 β_k the angle from positive \overline{t}_k to positive x_k , measured in the mathematically positive sense about positive z_k and determined by

$$\sin \beta_k = (\overline{t}_k \times \overline{x}_k) \cdot \overline{z}_k; \qquad \cos \beta_k = \overline{t}_k \cdot \overline{x}_k$$

 c_k the deviation of \overline{s}_k^r from \overline{o}_k^r , measured along positive z_k^r and given by

$$c_k = (\overline{s}_k^r - \overline{o}_k^r) \cdot \overline{z}_k^r$$

 γ_k the angle from positive x_k^r to positive \bar{t}_k , measured in the mathematically positive sense about positive z_k^r and determined by

$$\sin \gamma_k = (\overline{x}_k^r \times \overline{t}_k) \cdot \overline{z}_k^r; \qquad \cos \gamma_k = \overline{x}_k^r \cdot \overline{t}_k$$

NOTES

- 2 For a detailed description of the Sheth-Uicker parameters see [1].
- 3 In industrial robot technology the Denavit-Hartenberg parameters (DH-parameters) are widely

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used. See [2]. For kinematic structures with loops it is important to represent the information about the relative placement of the link axes separately from the present state of the pair. In contrast to DH-parameters, SU-parameters provide for this separation.

- 4 See annex F for information on the replacement of DH-parameters by SU-parameters.
- 5 An instance of **su_parameters** with SU-parameters as defined above is equivalent to an instance of **axis2_placement_3d** that has the following attribute values:

```
SELF\placement.location: cartesian_point ([(a_k \cos \gamma_k + b_k \sin \gamma_k \sin \alpha_k), (a_k \sin \gamma_k - b_k \cos \gamma_k \sin \alpha_k), (c_k + b_k \cos \alpha_k)]);
axis: direction ([(\sin \gamma_k \sin \alpha_k), (-\cos \gamma_k \sin \alpha_k), \cos \alpha_k]);
ref_direction: direction ([(\cos \gamma_k \cos \beta_k - \sin \gamma_k \cos \alpha_k \sin \beta_k), (\sin \gamma_k \cos \beta_k + \cos \gamma_k \cos \alpha_k \sin \beta_k), (\sin \alpha_k \sin \beta_k)].
```

EXPRESS specification:

```
*)

ENTITY su_parameters

SUBTYPE OF (representation_item);

a : length_measure;

alpha: plane_angle_measure;

b : length_measure;

beta: plane_angle_measure;

c : length_measure;

gamma: plane_angle_measure;

END_ENTITY;

(*

Attribute definitions:

a: SU-parameter a<sub>k</sub>.
```

b: SU-parameter b_k .

beta: SU-parameter β_k .

c: SU-parameter c_k .

gamma: SU-parameter γ_k .

5.4.18 kinematic_pair

A kinematic_pair defines the kinematic constraints between two adjacent links coinciding at a joint.

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EXPRESS specification:

```
*)
ENTITY kinematic_pair
 SUBTYPE OF (item_defined_transformation);
  joint : kinematic_joint;
DERIVE
  pair_placement_in_first_link_context
        : rigid_placement
        := SELF\item_defined_transformation.transform_item_1;
  pair_placement_in_second_link_context
        : rigid_placement
        := SELF\item defined_transformation.transform_item_2;
UNIQUE
  UR1: joint;
WHERE
  WR1: coordinated_pair_link_representation
         (joint.first_link, pair_placement_in_first_link_context);
  WR2: coordinated_pair_link_representation
         (joint.second_link, pair_placement_in_second_link_context);
END_ENTITY;
(*
```

Attribute definitions:

joint: the joint whose motion is constrained by the kinematic_pair.

pair_placement_in_first_link_context: the placement of the pair frame on the first link in the context of the first link, i.e., its link frame.

pair_placement_in_second_link_context: the placement of the pair frame on the second link in the context of the second link, i.e., its link frame.

Formal propositions:

UR1: Each kinematic_pair shall apply to a different joint.

WR1: There shall be a kinematic_link_representation related to joint.first_link, and it shall contain pair_placement_in_first_link_context in its items set. This condition is checked by the function coordinated_pair_link_representation.

WR2: There shall be a kinematic_link_representation related to joint.second_link, and it shall contain pair_placement_in_second_link_context in its items set. This condition is checked by the function coordinated_pair_link_representation.

NOTES

- 1 The relative position of the second link with respect to the first link is defined on the basis of three frames:
 - one frame, rigidly connected to the first link and placed in the context (i.e., with respect to the link frame) of the first link;

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- another frame, rigidly connected to the second link and placed in the context (i.e., with respect to the link frame) of the second link;
- a contact frame which specifies the point and plane of contact between the two links. This contact frame may or may not be physically connected with one of the links.

The type of the pair, together with the pair parameters, defines the placement of the contact frame relative to the first pair frame as well as the placement of the contact frame relative to the second pair frame. Thus, indirectly the placement of the two pair frames relative to each other is defined. See figure 3.

2 - The goal of a kinematic analysis of a mechanism is to determine the link frames for all the links of that mechanism such that they are consistent with the actual pair parameters. The consistency condition is as follows:

Consider one pair which connects two links and let

j indicate the first link of that pair;

k indicate the second link of that pair;

p indicate that pair as seen from the first link;

q indicate that pair as seen from the second link;

c indicate the common contact point (which may or may not be physically connected with both links);

 ${}^{0}LF_{j}$ and ${}^{0}LF_{k}$ be the rigid homogeneous matrix representation of the link frames of those links (both relative to the world coordinate system);

 ${}^{j}PF_{p}$ and ${}^{k}PF_{q}$ be the pair placements of pair p with respect to the first and second link of that pair, respectively,

then

 ${}^{0}PF_{p} = {}^{0}LF_{j}$ ${}^{j}PF_{p}$ is the rigid homogeneous matrix placing the first pair frame relative to the world coordinate system while

 ${}^{p}PF_{c}$ is the placement for the contact frame relative to the first pair frame. This placement is determined by the type of the pair and its actual pair parameters.

 ${}^{q}PF_{c}$ is the placement for the contact frame relative to the second pair frame. This placement is determined by the type of the pair and its actual pair parameters.

Consistency now requires that

$${}^{0}\boldsymbol{L}\boldsymbol{F}_{j}{}^{j}\boldsymbol{P}\boldsymbol{F}_{p}{}^{p}\boldsymbol{P}\boldsymbol{F}_{c}={}^{0}\boldsymbol{L}\boldsymbol{F}_{k}{}^{k}\boldsymbol{P}\boldsymbol{F}_{q}{}^{q}\boldsymbol{P}\boldsymbol{F}_{c}$$

Or else, for the second link placement relative to the world coordinate system is obtained ${}^{0}\mathbf{L}\mathbf{F}_{k}={}^{0}\mathbf{L}\mathbf{F}_{j}\,{}^{j}\mathbf{P}\mathbf{F}_{p}\,{}^{p}\mathbf{P}\mathbf{F}_{c}\,{}^{q}\mathbf{P}\mathbf{F}_{c}^{-1}\,{}^{k}\mathbf{P}\mathbf{F}_{q}^{-1}$

3 – For lower pairs the contact frame and the second pair frame shall be treated as identical. Hence, for lower pairs the rigid homogeneous matrix representation of ${}^q PF_c$ is a unit matrix.

5.4.19 pair_actuator

The pair_actuator identifies a kinematic_pair that is actuated. All degrees of freedom of a kinematic_pair that is identified by a pair_actuator are treated as being actuated.

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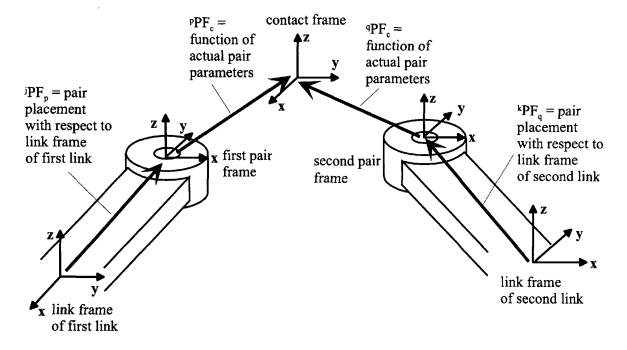


Figure 3 - Placement relationships of the pair frames relative to the mating links

NOTES

- 1 For a backward kinematic analysis the actuated pairs are used to achieve a prescribed path or a prescribed position. For a forward kinematic analysis pair values may be prescribed only for actuated pairs.
- 2 This part of ISO 10303 does not support actuation of individual degrees of freedom of a kinematic pair. Modelling of kinematic systems needs to be performed such that a kinematic pair is either fully actuated or not at all. Mixed situations such as, for example, a cylindrical pair can be avoided by using a revolute pair and a prismatic pair separately.

EXPRESS specification:

```
*)
ENTITY pair_actuator;
  actuated_pair : kinematic_pair;
  name : label;
UNIQUE
  UR1: actuated_pair;
END_ENTITY;
(*
```

Attribute definitions:

actuated_pair: the kinematic pair which is actuated.

name: the word or group of words by which the pair_actuator is referred to.

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Formal propositions:

UR1: Each pair_actuator shall apply to a different actuated_pair.

5.4.20 pair_value

The pair_value specifies the configuration of the two links that join a kinematic_pair.

EXPRESS specification:

```
*)
ENTITY pair_value;
  applies_to_pair: kinematic_pair;
END_ENTITY;
(*
```

Attribute definitions:

applies_to_pair: the kinematic_pair to which the pair_value applies.

5.4.21 simple_pair_range

The simple_pair_range specifies the allowable range of configurations of the two links that join a kinematic_pair.

NOTE – The range specification allows for only simple range specifications of each individual pair parameter value in the form "low bound – high bound".

EXPRESS specification:

```
*)
ENTITY simple_pair_range;
  applies_to_pair: kinematic_pair;
END_ENTITY;
(*
```

Attribute definitions:

applies_to_pair: the pair to which the range applies.

5.4.22 revolute_pair

The revolute_pair constrains the motion between two adjacent links to a rotation about a common axis. To measure the angle of rotation a frame is defined on each of the links such that local origins and the z-axes coincide and their positive directions agree. The motion of the second link with respect to the first link is defined as the angle required to rotate the x-axis of the first pair frame in positive direction around the common z-axis until it matches the x-axis of the second pair frame.

```
NOTE - See figure 4.
```

EXPRESS specification:

*)
ENTITY revolute_pair

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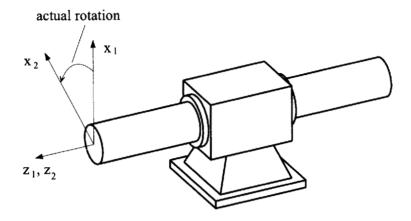


Figure 4 - Example of a joint representing a revolute pair

```
SUBTYPE OF (kinematic_pair);
END_ENTITY;
(*
```

5.4.23 revolute_pair_value

The revolute_pair_value specifies the value of the pair parameter for the revolute_pair.

EXPRESS specification:

```
*)
ENTITY revolute_pair_value
SUBTYPE OF (pair_value);
SELF\pair_value.applies_to_pair : revolute_pair;
actual_rotation : plane_angle_measure ;
END_ENTITY;
(*
```

Attribute definitions:

SELF\pair_value.applies_to_pair: the revolute_pair to which the revolute_pair_value applies.

actual_rotation: the value of the pair parameter.

5.4.24 revolute_pair_range

The revolute_pair_range specifies the lower bound and the upper bound of the parameter range for the revolute_pair.

EXPRESS specification:

```
*)
ENTITY revolute_pair_range
SUBTYPE OF (simple_pair_range);
SELF\simple_pair_range.applies_to_pair : revolute_pair;
```

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```
lower_limit_actual_rotation
                                          : rotational_range_measure;
  upper_limit_actual_rotation
                                          : rotational_range_measure;
WHERE
  WR1: (('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (lower_limit_actual_rotation))
        ('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (upper_limit_actual_rotation)))
       (lower_limit_actual_rotation < upper_limit_actual_rotation);</pre>
END_ENTITY;
```

Attribute definitions:

SELF\simple_pair_range.applies_to_pair: the revolute_pair to which the revolute_pair_range applies.

lower_limit_actual_rotation: the minimum value of the pair parameter.

upper_limit_actual_rotation: the maximum value of the pair parameter.

Formal propositions:

WR1: The range of the revolute_pair shall be positive when both bounds are not given as unlimited.

5.4.25prismatic_pair

The prismatic_pair constrains the motion between two adjacent links to a translation along a common axis. To measure the distance of translation a frame is defined on each of the links such that their corresponding coordinate axes coincide and their positive directions agree. The motion of the second link with respect to the first link is defined as the distance required to translate the xy-plane of the first pair frame in positive direction of the common z-axis until it coincides with the xy-plane of the second pair frame.

```
NOTE - See figure 5.
EXPRESS specification:
```

```
*)
ENTITY prismatic_pair
  SUBTYPE OF ( kinematic_pair);
END_ENTITY;
(*
```

prismatic_pair_value 5.4.26

The prismatic_pair_value is the value of the pair parameter for the prismatic_pair.

EXPRESS specification:

```
*)
ENTITY prismatic_pair_value
```

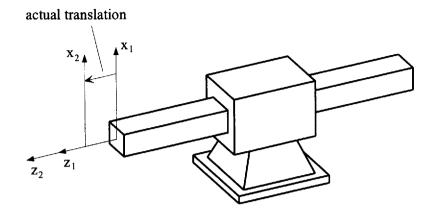


Figure 5 - Example of a joint representing a prismatic pair

```
SUBTYPE OF (pair_value);
SELF\pair_value.applies_to_pair : prismatic_pair;
actual_translation : length_measure;
END_ENTITY;
(*
```

Attribute definitions:

SELF\pair_value.applies_to_pair: the prismatic_pair to which the prismatic_pair_value applies.

actual_translation: the value of the pair parameter.

5.4.27 prismatic_pair_range

The **prismatic_pair_range** specifies the lower bound and the upper bound of the parameter range for the **prismatic_pair**.

EXPRESS specification:

```
*)
ENTITY prismatic_pair_range
  SUBTYPE OF (simple_pair_range);
  SELF\simple_pair_range.applies_to_pair : prismatic_pair;
  lower_limit_actual_translation
                                         : translational_range_measure;
                                         : translational_range_measure;
  upper_limit_actual_translation
WHERE
  WR1: (('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (lower_limit_actual_translation))
        ('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (upper_limit_actual_translation)))
       (lower_limit_actual_translation < upper_limit_actual_translation);</pre>
END_ENTITY;
(*
```

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Attribute definitions:

SELF\simple_pair_range.applies_to_pair: the prismatic_pair to which the prismatic_ pair_range applies.

lower_limit_actual_translation: the minimum value of the pair parameter.

upper_limit_actual_translation: the maximum value of the pair parameter.

Formal propositions:

WR1: The range of the prismatic_pair shall be positive when both bounds are not given as unlimited.

5.4.28screw_pair

A screw_pair constrains the motion between two adjacent links to a rotation about, and translation along, a common axis, where the translation is proportional to the rotation. The factor of proportionality is given by **pitch** which defines the translational displacement for one full rotation. The frames are defined on each of the links such that the z-axes coincide and the positive directions agree.

The motion of the second link with respect to the first link is specified by the angle required to rotate the x-axis of the first pair frame in positive direction around the common z-axis until its direction coincides with the direction of the x-axis of the second pair frame. The translation of the second link along the z-axis shall depend on the rotation according to

$$translation = \frac{pitch \cdot actual_rotation}{2\pi}$$

where actual_rotation is given in radians.

Hence a full rotation (actual_rotation = 2π) displaces the xy-plane of the second pair frame by the value pitch in the positive z-direction relative to the first pair frame.

NOTE 2 - The screw_pair does not distinguish which one of its links is driving or driven.

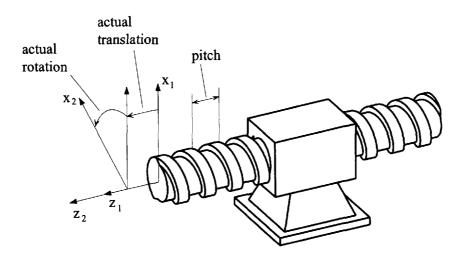
EXPRESS specification:

```
*)
ENTITY screw_pair
 SUBTYPE OF (kinematic_pair);
 pitch : length_measure;
END_ENTITY;
```

Attribute definitions:

pitch: the pitch of the screw.

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NOTE – The relationship between actual rotation and actual translation as drawn in the figure does not actually correspond to pitch. actual translation as drawn would result from an actual rotation covering more than a full revolution.

Figure 6 - Example of a joint representing a screw pair

5.4.29 screw_pair_value

A screw_pair_value specifies the value of the pair parameter of the screw_pair.

EXPRESS specification:

Attribute definitions:

SELF\pair_value.applies_to_pair: the screw_pair to which the screw_pair_value applies.

actual_rotation: the rotation angle of the screw_pair.

actual_translation: the resulting translation.

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5.4.30 screw_pair_range

The **screw_pair_range** specifies the lower bound and the upper bound of the parameter range for the **screw_pair**.

EXPRESS specification:

Attribute definitions:

SELF\simple_pair_range.applies_to_pair: the screw_pair to which the screw_pair_range applies.

lower_limit_actual_rotation: the minimum value of the pair parameter.

upper_limit_actual_rotation: the maximum value of the pair parameter.

Formal propositions:

WR1: The range of the screw_pair shall be positive when both bounds are not given as unlimited.

5.4.31 cylindrical_pair

The cylindrical_pair constrains the motion between two adjacent links to a translation along a common axis and a rotation about it.

```
NOTE - See figure 7.
```

To measure the displacement and the angle of rotation, a frame is defined on each of the links such that the z-axes coincide and the positive directions agree. The distance of translation is defined as the distance required to translate the xy-plane of the first pair frame in the positive direction of the common z-axis until it coincides with the xy-plane of the second pair frame. The angle of rotation is defined as the angle required to rotate the x-axis of the first pair frame in the positive direction around the common z-axis until its direction coincides with the direction of the x-axis of the second pair frame.

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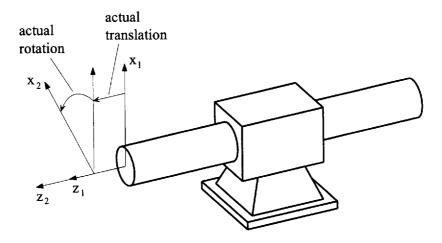


Figure 7 - Example of a joint representing a cylindrical pair

EXPRESS specification:

```
*)
ENTITY cylindrical_pair
  SUBTYPE OF (kinematic_pair);
END_ENTITY;
(*
```

5.4.32 cylindrical_pair_value

The $\ensuremath{ \mathbf{cylindrical_pair_value} }$ specifies the set of pair parameters for a $\ensuremath{ \mathbf{cylindrical_pair} }$.

EXPRESS specification:

```
*)
ENTITY cylindrical_pair_value
   SUBTYPE OF (pair_value);
   SELF\pair_value.applies_to_pair : cylindrical_pair;
   actual_translation : length_measure;
   actual_rotation : plane_angle_measure;
END_ENTITY;
(*
```

Attribute definitions:

SELF\pair_value.applies_to_pair: the cylindrical_pair to which the cylindrical_pair_value applies.

actual_translation: the translation value.

actual_rotation: the angle of rotation.

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5.4.33 cylindrical_pair_range

The **cylindrical_pair_range** specifies the lower bound and the upper bound of the parameter range for the **cylindrical_pair**.

EXPRESS specification:

```
ENTITY cylindrical_pair_range
 SUBTYPE OF (simple_pair_range);
 SELF\simple_pair_range.applies_to_pair : cylindrical_pair;
 lower_limit_actual_translation : translational_range_measure;
 upper_limit_actual_translation
                                       : translational_range_measure;
  lower_limit_actual_rotation
                                        : rotational_range_measure;
  upper_limit_actual_rotation
                                         : rotational_range_measure;
WHERE
  WR1: (('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
        TYPEOF (lower_limit_actual_translation))
        ('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
        TYPEOF (upper_limit_actual_translation)))
       (lower_limit_actual_translation < upper_limit_actual_translation);</pre>
  WR2: (('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
        TYPEOF (lower_limit_actual_rotation))
        ('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
        TYPEOF (upper_limit_actual_rotation)))
       (lower_limit_actual_rotation < upper_limit_actual_rotation);</pre>
END_ENTITY;
```

Attribute definitions:

SELF\simple_pair_range.applies_to_pair: the cylindrical_pair to which the cylindrical_pair_range applies.

lower_limit_actual_translation: the minimum value of translation for the cylindrical_pair.

upper_limit_actual_translation: the maximum value of translation for the cylindrical_pair.

lower_limit_actual_rotation: the minimum value of rotation for the cylindrical_pair.

upper_limit_actual_rotation: the maximum value of rotation for the cylindrical_pair.

Formal propositions:

WR1: The range of translation of the cylindrical_pair shall be positive when both bounds are not given as unlimited.

WR2: The range of rotation of the cylindrical_pair shall be positive when both bounds are not given as unlimited.

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5.4.34 spherical_pair

The spherical_pair constrains the motion between two adjacent links to the rotation about three independent axes that intersect in a common point. To measure the three angles of rotation, a frame system is defined on each of the links such that the origins of the frames coincide. The three angles of rotation are defined as the yaw, pitch, and roll angles. See 5.3.6. They are required to rotate the x-, y-, and z-axes of the first pair frame until the axis directions of this frame coincide with the axis directions of the second pair frame.

```
NOTE - See figure 8.

EXPRESS specification:

*)

ENTITY spherical_pair

SUBTYPE OF (kinematic_pair);

END_ENTITY;
```

5.4.35 spherical_pair_value

The spherical_pair_value specifies the set of pair parameters for a spherical_pair.

EXPRESS specification:

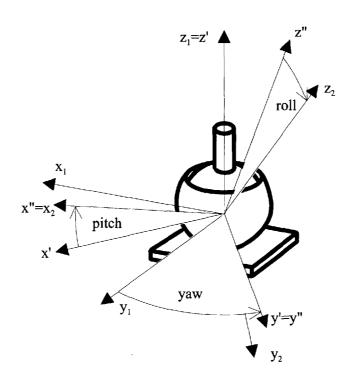
Attribute definitions:

SELF\pair_value.applies_to_pair: the spherical_pair to which the spherical_pair_value applies.

input_orientation: the input specification of the pair parameter values from which the actual_orientation is derived. input_orientation is either a ypr_rotation or a rotation_about_direction.

actual_orientation: the set of pair parameter values for a spherical_pair according to the ypr notation. This is derived from input_orientation by the function convert_spatial_to_ypr_rotation.

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NOTE – (x_1, y_1, z_1) is the first pair frame, and (x_2, y_2, z_2) is the second pair frame. (x', y', z') is an intermediate frame resulting from the yaw rotation of (x_1, y_1, z_1) about z_1 . (x'', y'', z'') results from the pitch rotation of (x', y', z') about y'. The roll rotation of (x'', y'', z'') about x'' produces (x_2, y_2, z_2) .

Figure 8 - Example of a joint representing a spherical pair

5.4.36 spherical_pair_range

The **spherical_pair_range** specifies the lower bound and the upper bound of the parameter range for a **spherical_pair**.

EXPRESS specification:

```
*)
ENTITY spherical_pair_range
  SUBTYPE OF (simple_pair_range);
  SELF\simple_pair_range.applies_to_pair : spherical_pair;
  lower_limit_yaw
                                         : rotational_range_measure;
                                         : rotational_range_measure;
  upper_limit_yaw
                                         : rotational_range_measure;
  lower_limit_pitch
  upper_limit_pitch
                                         : rotational_range_measure;
  lower_limit_roll
                                         : rotational_range_measure;
                                          : rotational_range_measure;
  upper_limit_roll
WHERE
  WR1: (('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (lower_limit_yaw))
        ('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
```

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```
TYPEOF (upper_limit_yaw)))
       XOR
       (lower_limit_yaw < upper_limit_yaw);</pre>
 WR2: (('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (lower_limit_pitch))
        OR
        ('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (upper_limit_pitch)))
       XOR
       (lower_limit_pitch < upper_limit_pitch);</pre>
  WR3: (('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (lower_limit_roll))
        OR
        ('KINEMATIC STRUCTURE SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (upper_limit_roll)))
       (lower_limit_roll < upper_limit_roll);</pre>
END_ENTITY;
```

Attribute definitions:

SELF\simple_pair_range.applies_to_pair: the spherical_pair to which the spherical_pair_range applies.

lower_limit_yaw: the minimum value of the yaw angle for the spherical_pair.

upper_limit_yaw: the maximum value of the yaw angle for the spherical_pair.

lower_limit_pitch: the minimum value of the pitch angle for the spherical_pair.

upper_limit_pitch: the maximum value of the pitch angle for the spherical_pair.

lower_limit_roll: the minimum value of the roll angle for the spherical_pair.

upper_limit_roll: the maximum value of the roll angle for the spherical_pair.

Formal propositions:

WR1: The range of rotation about the z-axis of the spherical_pair shall be positive when both bounds are not given as unlimited.

WR2: The range of rotation about the y-axis of the spherical_pair shall be positive when both bounds are not given as unlimited.

WR3: The range of rotation about the x-axis of the spherical_pair shall be positive when both bounds are not given as unlimited.

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5.4.37 universal_pair

The universal_pair constrains the motion between two adjacent links to two rotations about two intersecting axes.

```
NOTE - See figure 9.
```

To measure those two angles of rotation, a frame system is defined on each of the links such that the origins coincide in the intersection point of the axes, the first z-axis coincides with the first axis of rotation, and the second x-axis coincides with the second axis of rotation. A third constant rotation is inserted between these two variable rotations. In order to migrate from the first pair frame to the second pair frame the following sequence of rotations has to be performed:

- 1) rotation of the x_1,y_1 -axes about the z_1 -axis by the amount specified by the first angle yielding an intermediate frame denoted by $(x',y',z'=z_1)$;
- 2) rotation of the z', x'-axes about the y'-axis by the amount of the constant skew angle yielding a second intermediate frame denoted by (x'', y'' = y', z'');
- 3) rotation of the y'', z''-axes about the x''-axis by the amount specified by the second angle, yielding the final frame $(x_2 = x'', y_2, z_2)$.

EXPRESS specification:

Attribute definitions:

input_skew_angle: an optional attribute that, if present, defines the angle by which the intersection angle between the two axes of rotation deviates from a right angle.

skew_angle: the angle by which the intersection angle between the two axes of rotation deviates from a right angle. If **input_skew_angle** is given, the value of **skew_angle** becomes that of **input_skew_angle**; otherwise it becomes zero.

Formal propositions:

WR1: The absolute value of **skew_angle** shall represent an acute angle.

5.4.38 universal_pair_value

The universal_pair_value specifies the set of pair parameters for a universal_pair.



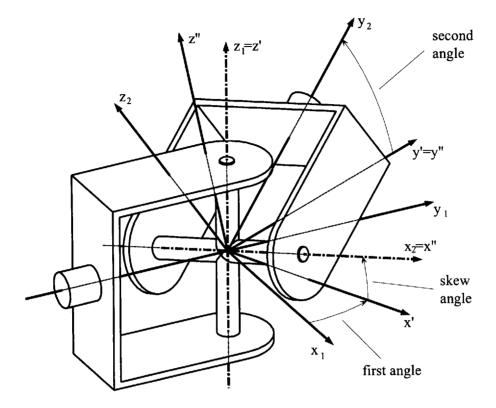


Figure 9 - Example of a joint representing a universal pair

EXPRESS specification:

```
*)
ENTITY universal_pair_value
  SUBTYPE OF (pair_value);
  SELF\pair_value.applies_to_pair : universal_pair;
  first_rotation_angle
                                 : plane_angle_measure;
                                 : plane_angle_measure;
  second_rotation_angle
END_ENTITY;
(*
```

Attribute definitions:

SELF\pair_value.applies_to_pair: the universal_pair to which the universal_pair_value applies.

first_rotation_angle: the angle of rotation around the first axis.

second_rotation_angle: the angle of rotation around the second axis.

universal_pair_range 5.4.39

The universal_pair_range specifies the lower bound and the upper bound of the parameter range for the universal_pair.

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EXPRESS specification:

```
*)
ENTITY universal_pair_range
 SUBTYPE OF (simple_pair_range);
 SELF\simple_pair_range.applies_to_pair : universal_pair;
 lower_limit_first_rotation
                                        : rotational_range_measure;
                                        : rotational_range_measure;
 upper_limit_first_rotation
 lower_limit_second_rotation
                                         : rotational_range_measure;
  upper_limit_second_rotation
                                         : rotational_range_measure;
WHERE
 WR1: (('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (lower_limit_first_rotation))
        OR
        ('KINEMATIC STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (upper_limit_first_rotation)))
       XNR
       (lower_limit_first_rotation < upper_limit_first_rotation);</pre>
  WR2: (('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (lower_limit_second_rotation))
        ('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (upper_limit_second_rotation)))
       (lower_limit_second_rotation < upper_limit_second_rotation);</pre>
END_ENTITY;
(*
```

Attribute definitions:

SELF\simple_pair_range.applies_to_pair: the universal_pair to which the universal_pair_range applies.

lower_limit_first_rotation: the minimum value of rotation around the first axis for the universal_pair.

upper_limit_first_rotation: the maximum value of rotation around the first axis for the universal_pair.

lower_limit_second_rotation: the minimum value of rotation around the second axis for the universal_pair.

upper_limit_second_rotation: the maximum value of rotation around the second axis for the **universal_pair**.

Formal propositions:

WR1: The range of rotation around the first axis of a universal_pair shall be positive when both bounds are not given as unlimited.

WR2: The range of rotation around the second axis of a universal_pair shall be positive when both bounds are not given as unlimited.

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5.4.40 planar_pair

The planar_pair constrains the motion between two adjacent links to translations along the x-axis and y-axis and a rotation about the z-axis. To measure the translations and the angle of rotation, a frame is defined on each of the links such that the x-, y-, and z-axes coincide and the positive directions agree. The translations in x- and y-directions are defined as the displacements required to translate the origin of the first pair frame in positive direction of the x- and y-axes until it coincides with the origin of the second pair frame. The angle of rotation is defined as the angle required to rotate the x-axis of the first pair frame in positive direction around the common z-axis until its direction coincides with the direction of the x-axis of the second pair frame.

```
NOTE - See figure 10.
EXPRESS specification:
*)
ENTITY planar_pair
  SUBTYPE OF (kinematic_pair);
END_ENTITY;
(*
```

5.4.41 planar_pair_value

The planar_pair_value specifies the set of pair parameters for the planar_pair.

EXPRESS specification:

```
*)
ENTITY planar_pair_value
   SUBTYPE OF (pair_value);
SELF\pair_value.applies_to_pair : planar_pair;
   actual_rotation : plane_angle_measure;
   actual_translation_x : length_measure;
   actual_translation_y : length_measure;
END_ENTITY;
(*
```

Attribute definitions:

SELF\pair_value.applies_to_pair: the planar_pair to which the planar_pair_value applies.

actual_rotation: the value of the angle of rotation for a planar_pair.

actual_translation_x: the value of translation in x-direction for a planar_pair.

actual_translation_y: the value of translation in y-direction for a planar_pair.

5.4.42 planar_pair_range

The **planar_pair_range** specifies the lower bound and the upper bound of the parameter range for the **planar_pair**.

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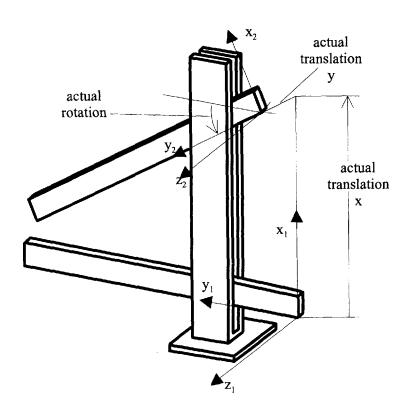


Figure 10 - Example of a joint representing a planar pair

EXPRESS specification:

```
*)
ENTITY planar_pair_range
 SUBTYPE OF (simple_pair_range);
 SELF\simple_pair_range.applies_to_pair : planar_pair;
                                         : rotational_range_measure;
 lower_limit_actual_rotation
                                         : rotational_range_measure;
  upper_limit_actual_rotation
  lower_limit_actual_translation_x
                                          : translational_range_measure;
 upper_limit_actual_translation_x
                                          : translational_range_measure;
  lower_limit_actual_translation_y
upper_limit_actual_translation_y
                                          : translational_range_measure;
                                          : translational_range_measure;
  WR1: (('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (lower_limit_actual_rotation))
        OR
        ('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (upper_limit_actual_rotation)))
       (lower_limit_actual_rotation < upper_limit_actual_rotation);</pre>
  WR2: (('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (lower_limit_actual_translation_x))
        ('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (upper_limit_actual_translation_x)))
```

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Attribute definitions:

SELF\simple_pair_range.applies_to_pair: the planar_pair to which the planar_pair_range applies.

lower_limit_actual_rotation: the minimum value of the angle of rotation for the planar_pair.

upper_limit_actual_rotation: the maximum value of the angle of rotation for the planar_pair.

lower_limit_actual_translation_x: the minimum value of translation in x-direction for the planar_pair.

upper_limit_actual_translation_x: the maximum value of translation in x-direction for the planar_pair.

lower_limit_actual_translation_y: the minimum value of translation in y-direction for the planar_pair.

upper_limit_actual_translation_y: the maximum value of translation in y-direction for the planar_pair.

Formal propositions:

WR1: The range of rotation of the planar_pair shall be positive when both bounds are not given as unlimited.

WR2: The range of translation in x-direction of the planar_pair shall be positive when both bounds are not given as unlimited.

WR3: The range of translation in y-direction of the planar_pair shall be positive when both bounds are not given as unlimited.

5.4.43 unconstrained_pair

The unconstrained_pair does not constrain the relative motion between two adjacent links.

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NOTES

- 1 The unconstrained pair may be helpful in early design stages or for kinematic analysis systems, because it allows to eliminate the constraints between two links without changing the topological structure.
- 2 The concept of pair range is not applicable to an unconstrained_pair.

EXPRESS specification:

```
*)
ENTITY unconstrained_pair
  SUBTYPE OF (kinematic_pair);
END_ENTITY;
(*
```

5.4.44 unconstrained_pair_value

An unconstrained_pair_value specifies the pair parameters for an unconstrained_pair.

EXPRESS specification:

```
*)
ENTITY unconstrained_pair_value
SUBTYPE OF (pair_value);
SELF\pair_value.applies_to_pair : unconstrained_pair;
actual_placement : axis2_placement_3d;
END_ENTITY;
(*
```

Attribute definitions:

SELF\pair_value.applies_to_pair: the unconstrained_pair to which the unconstrained_pair_value applies.

actual_placement: the placement of the second pair frame with respect to the first pair frame for the unconstrained_pair.

5.4.45 fully_constrained_pair

The fully_constrained_pair prevents any relative motion between two adjacent links. The two pair frames are always forced to coincide.

NOTES

- 1 The **fully_constrained_pair** may be helpful in early design stages or for kinematic analysis systems, because it allows to fix two links each to the other without changing the topological structure.
- 2 The concepts of pair value and pair range are not applicable to a fully_constrained_pair.

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EXPRESS specification:

```
*)
ENTITY fully_constrained_pair
   SUBTYPE OF (kinematic_pair);
END_ENTITY;
(*
```

5.4.46 point_on_surface_pair

The **point_on_surface_pair** constrains the motion of two links such that a point defined on the second link always lies on a surface defined on the first link. The actual location of this point on the surface is called the contact point. The contact point specifies an origin of a frame called the contact frame. The local normal to the surface in the contact point coincides with the z-axis of the contact frame. The x-axis of the contact frame is parallel to the tangent to the iso-parameter line of the surface for the first surface parameter, which passes the contact point, and points into the direction where the first surface parameter increases.

NOTES

1 - Translational motion of the second link is constrained to the two-dimensional parameter space of the surface, while its rotational motion about the contact point is not constrained. Therefore, a **point_on_surface_pair** behaves like a **spherical_pair** that additionally may move along a surface on the first link.

2 - See figure 11.

To support the measure of motion, a pair frame is defined on each of the links. The representation $f_1(u, v)$ is defined relative to the pair frame on the first link. The translational motion is given by the actual surface parameters of the contact point, u_1 and v_1 . The three angles of rotation are defined as the yaw, pitch, and roll angles. See 5.3.6. They are required to rotate the x-, y-, and z-axes of the contact frame until its directions coincide with the axis directions of the second pair frame. The origin of the pair frame on the second link coincides with the contact point. In order to migrate from the first pair frame to the second pair frame, the following sequence of transformations has to be performed:

1) Establish the contact frame ${}^{1}PF_{c}$ relative to the first pair frame:

$$\overline{origin}_c^1 = f_1(u_1, v_1)$$

$$\overline{x_{-}vector}_{c}^{1} = \frac{\partial f_{1}(u,v)}{\partial u}\bigg|_{u=u_{1},v=v_{1}}; \qquad \overline{x}_{c}^{1} = \frac{\overline{x_{-}vector}_{c}^{1}}{|\overline{x_{-}vector}_{c}^{1}|}$$

$$\left. \overline{w_vector}_c^1 = \frac{\partial f_1(u,v)}{\partial v} \right|_{u=u_1,v=v_1}; \qquad \overline{w}_c^1 = \frac{\overline{w_vector}_c^1}{\left| \overline{w_vector}_c^1 \right|}$$

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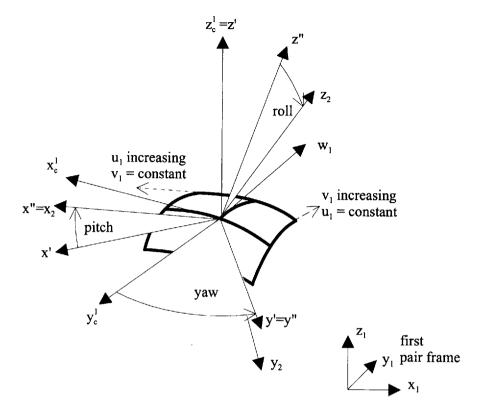


Figure 11 - Example of a point on surface pair

$$\overline{z}_{c}^{1} = \overline{w}_{c}^{1} \times \overline{x}_{c}^{1} ;$$

$$\overline{z}_{c}^{1} = \frac{\overline{z}_{c} vector_{c}^{1}}{|z_{c} vector_{c}^{1}|}$$

$$\overline{y}_{c}^{1} = \overline{y}_{c}^{1} \times \overline{x}_{c}^{1} ;$$

$$\overline{y}_{c}^{1} = \frac{\overline{y}_{c} vector_{c}^{1}}{|\overline{y}_{c} vector_{c}^{1}|}$$

 \overline{origin}_c^1 and the three direction vectors \overline{x}_c^1 , \overline{y}_c^1 , and \overline{z}_c^1 may be used to establish the rigid homogeneous matrix representation of the placement of the contact frame 1PF_c relative to the first pair frame.

- 2) Rotate the x_c^1, y_c^1 -axes about the z_c^1 -axis by the amount specified by the yaw angle. This yields an intermediate frame the axes of which are denoted by $(x', y', z' = z_c^1)$.
- 3) Rotate the z',x'-axes about the y'-axis by the amount specified by the pitch angle. This yields a second intermediate frame denoted by (x'',y''=y',z'').
- 4) Finally, rotate the y'',z''-axes about the x''-axis by the amount specified by the roll angle. The resulting frame $(x_2 = x'', y_2, z_2)$ now coincides with the pair frame on the second

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link.

EXPRESS specification:

Attribute definitions:

pair_surface: the surface on the first link of the pair on which the point on the second link is sliding.

Formal propositions:

WR1: The pair_surface of a point_on_surface_pair shall be in the items set of a kinematic_frame_background_representation which, in turn, is related to the kinematic_link_representation of the first link of the point_on_surface_pair by a kinematic_frame_background_representation_association. The transformer_frame in the transformation_operator of this relationship shall be the pair_placement_in_first_link_context of the point_on_surface_pair. These requirements are checked by the function frame_associated_to_background.

Informal propositions:

continuous surface: The surface used as pair_surface shall be smooth in its entire domain, and its tangent vectors shall change their direction only in a steady manner, regardless of whether the surface is composed of multiple surfaces or not.

NOTE 3 – This is equivalent to requiring the pair_surface to be G1 continuous throughout and that, in the case of a rectangular_composite_surface, the transition_code shall be at least cont_same_gradient at each segment junction curve. (See ISO 10303-42.)

5.4.47 point_on_surface_pair_value

The point_on_surface_pair_value specifies the pair parameters for the point_on_surface_pair.

EXPRESS specification:

```
*)
ENTITY point_on_surface_pair_value
SUBTYPE OF (pair_value);
SELF\pair_value.applies_to_pair : point_on_surface_pair;
actual_point_on_surface : point_on_surface;
input_orientation : spatial_rotation;
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```

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Attribute definitions:

SELF\pair_value.applies_to_pair: the point_on_surface_pair to which the point_on_surface_pair_value applies.

actual_point_on_surface: the positional value for the point on the surface.

input_orientation: the input specification of the rotational pair parameter values from which the actual_orientation is derived. input_orientation is either a ypr_rotation or a rotation_about_direction.

actual_orientation: the set of rotational pair parameter values for a point_on_surface_pair according to the ypr notation. This is derived from input_orientation by the function convert_spatial_to_ypr_rotation.

Formal propositions:

WR1: actual_point_on_surface shall be defined as a point on the pair_surface of the point_on_surface_pair referenced by applies_to_pair.

5.4.48 point_on_surface_pair_range

The **point_on_surface_pair_range** specifies the lower bound and the upper bound of the parameter range for the **point_on_surface_pair**.

EXPRESS specification:

```
*)
ENTITY point_on_surface_pair_range
  SUBTYPE OF (simple_pair_range);
  SELF\simple_pair_range.applies_to_pair : point_on_surface_pair;
  range_on_pair_surface
                                         : rectangular_trimmed_surface;
  lower_limit_yaw
                                         : rotational_range_measure;
  upper_limit_yaw
                                         : rotational_range_measure;
  lower_limit_pitch
                                         : rotational_range_measure;
  upper_limit_pitch
                                         : rotational_range_measure;
  lower_limit_roll
                                         : rotational_range_measure;
  upper_limit_roll
                                         : rotational_range_measure;
WHERE
  WR1: SELF\simple_pair_range.applies_to_pair\point_on_surface_pair.pair_surface
       :=: range_on_pair_surface.basis_surface;
  WR2: (('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (lower_limit_yaw))
```

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```
OR
        ('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (upper_limit_yaw)))
       (lower_limit_yaw < upper_limit_yaw);
 WR3: (('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (lower_limit_pitch))
        ('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (upper_limit_pitch)))
       XOR
       (lower_limit_pitch < upper_limit_pitch);
  WR4: (('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (lower_limit_roll))
        OR
        ('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (upper_limit_roll)))
       (lower_limit_roll < upper_limit_roll);</pre>
END_ENTITY;
```

Attribute definitions:

SELF\simple_pair_range.applies_to_pair: the point_on_surface_pair to which the point_on_surface_pair_range applies.

range_on_pair_surface: the admissible range for the positional pair parameter value on the contact surface on the first link.

lower_limit_yaw: the minimum value of the yaw angle for the point_on_surface_pair.

upper_limit_yaw: the maximum value of the yaw angle for the point_on_surface_pair.

lower_limit_pitch: the minimum value of the pitch angle for the point_on_surface_pair.

upper_limit_pitch: the maximum value of the pitch angle for the point_on_surface_pair.

lower_limit_roll: the minimum value of the roll angle for the point_on_surface_pair.

upper_limit_roll: the maximum value of the roll angle for the point_on_surface_pair.

Formal propositions:

WR1: The underlying surface of range_on_pair_surface in the range specification shall be identical with the surface pair_surface in the point_on_surface_pair specification.

WR2: The range of rotation about the z-axis of the point_on_surface_pair shall be positive when both bounds are not given as unlimited.

WR3: The range of rotation about the y-axis of the point_on_surface_pair shall be positive when both bounds are not given as unlimited.

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WR4: The range of rotation about the x-axis of the point_on_surface_pair shall be positive when both bounds are not given as unlimited.

5.4.49 surface_pair

A surface_pair constrains the motion of two links along a surface on each of the links such that they always have contact in at least one common point. This point lies on a surface of the links. The point is called the contact point. The contact point specifies an origin of a frame called a contact frame. The common tangential plane of the surfaces is the xy-plane of the contact frame. To measure motion, a pair frame is defined on each of the links. The surface representation f(u,v) of each surface is given in the corresponding pair frame. For the subsequent specification both surface representations need to be expressed in a common coordinate system. The world coordinate system is used for this purpose.

The following notation is used:

 u_p, v_p parameters of the surface on the first link;

 u_q, v_q parameters of the surface on the second link;

 ${}^{0}f_{p}(u_{p}, v_{p})$ representation of the surface on the first link relative to the world coordinate system;

 ${}^0f_q(u_q,v_q)$ representation of the surface on the second link relative to the world coordinate system;

 x_p, y_p, z_p axes of the first pair frame;

 x_q, y_q, z_q axes of the second pair frame;

 x_c^p , y_c^p , z_c^p axes of the contact frame, defined with respect to the first pair frame, but not taking into account the surface orientations and the respective rotation;

 x_c^q , y_c^q , z_c^q axes of the contact frame, defined with respect to the second pair frame;

 x_c , y_c , z_c axes of the contact frame, defined with respect to the first pair frame after the surface orientations and the respective rotation have been taken into account.

NOTE 1 – See figure 12 for an exploded view of a surface pair. There is a rotation angle of -15° between x_c^p and x_c^q , and **orientation** is FALSE.

The following equations apply to sliding_surface_pair (see 5.4.52) and rolling_surface_pair (see 5.4.54).

The contact frame is determined from both sides of the pair as follows, beginning with the second link:

$$\overline{origin}_c^q = \, {}^0\!f_q(u_q,v_q)$$

$$\overline{x_{-}vector}_{c}^{q} = \frac{\partial {}^{0}f_{q}(u,v)}{\partial u} \bigg|_{u=u_{q},v=v_{q}} ; \qquad \overline{x}_{c}^{q} = \frac{\overline{x_{-}vector}_{c}^{q}}{|\overline{x_{-}vector}_{c}^{q}|}$$

$$\overline{w_vector}_c^q = \left. \frac{\partial \,^0 f_q(u,v)}{\partial v} \right|_{u=u_q,v=v_q}; \qquad \overline{w}_c^q = \frac{\overline{w_vector}_c^q}{|\overline{w_vector}_c^q|}$$

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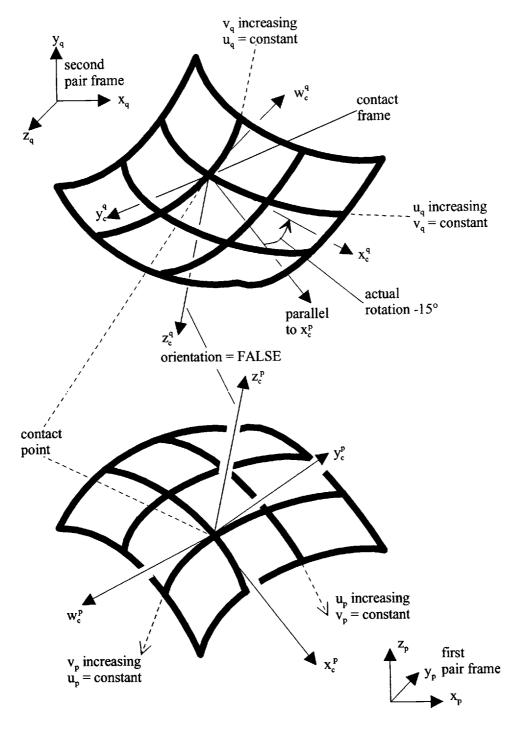


Figure 12 - Example of a surface pair.

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$$\overline{z_{-}vector}_{c}^{q} = \overline{w}_{c}^{q} \times \overline{x}_{c}^{q} ; \qquad \qquad \overline{z}_{c}^{q} = \frac{\overline{z_{-}vector}_{c}^{q}}{|z_{-}vector_{c}^{q}|}$$

$$\overline{y_{\cdot}vector_{c}^{q}} = \overline{z}_{c}^{q} \times \overline{x}_{c}^{q} \; ; \qquad \qquad \overline{y}_{c}^{q} = \frac{\overline{y_{\cdot}vector_{c}^{q}}}{|\overline{y_{\cdot}vector_{c}^{q}}|}$$

 \overline{origin}_c^q and the three direction vectors \overline{x}_c^q , \overline{y}_c^q , and \overline{z}_c^q may be used to establish the rigid homogeneous matrix representation of the placement of the contact frame ${}^q \boldsymbol{P} \boldsymbol{F}_c$ relative to the second pair frame.

NOTE 2 – See figure 3 for an illustration of the relationships between the frames.

The same analysis is performed for the first link:

$$\overline{origin}_c^p = {}^0f_p(u_p, v_p)$$

$$\overline{x_{-}vector_{c}^{p}} = \frac{\partial {}^{0}f_{p}(u,v)}{\partial u} \Big|_{u=u_{p},v=v_{p}}; \qquad \overline{x_{c}^{p}} = \frac{\overline{x_{-}vector_{c}^{p}}}{|\overline{x_{-}vector_{c}^{p}}|}$$

$$\overline{w_{-}vector_{c}^{p}} = \frac{\partial^{0}f_{p}(u,v)}{\partial v}\Big|_{u=u_{n},v=v_{n}}; \qquad \overline{w}_{c}^{p} = \frac{\overline{w_{-}vector_{c}^{p}}}{|\overline{w_{-}vector_{c}^{p}}|}$$

$$\overline{z_c} = \overline{w_c^p} \times \overline{x_c^p} ; \qquad \overline{z_c^p} = \frac{\overline{z_c} vector_c^p}{|\overline{z_c} vector_c^p|}$$

$$\overline{y_{-}vector_{c}^{p}} = \overline{z}_{c}^{p} \times \overline{x}_{c}^{p} ; \qquad \overline{y}_{c}^{p} = \frac{\overline{y_{-}vector_{c}^{p}}}{|y_{-}vector_{c}^{p}|}$$

The contact point shall be identically positioned, relative to the world coordinate system, irrespective of whether it is approached from the second or the first link.

$$\overline{origin}_c = \overline{origin}_c^p = \overline{origin}_c^q$$

Also the z-direction at the contact point shall be identical, relative to the world coordinate system, irrespective of whether it is approached from the second or the first link.

However, the direction vectors \overline{z}_c^q and \overline{z}_c^p , as evaluated above, are either

1)
$$\overline{z}_c = \overline{z}_c^q = \overline{z}_c^p$$
 or

2)
$$\overline{z}_c = \overline{z}_c^q = -\overline{z}_c^p$$

In case 1, orientation is TRUE and both z-directions are identical.

In case 2, **orientation** is FALSE and z_c^p (as well as y_c^p) is rotated by π about the x_c^p direction. Finally, x_c^p has to be rotated about z_c until it coincides with x_c .

NOTE 3 – The rotation angle to achieve this is defined by the actual_rotation attribute of slid-ing_surface_pair_value (see 5.4.52) and of rolling_surface_pair_value (see 5.4.54), respectively.

EXPRESS specification:

```
*)
ENTITY surface_pair
  SUBTYPE OF (kinematic_pair);
            : surface;
  surface_1
  surface_2 : surface;
  orientation : BOOLEAN;
WHERE
  WR1: frame_associated_to_background
         (SELF\kinematic_pair.pair_placement_in_first_link_context,
          surface_1);
 WR2: frame_associated_to_background
         (SELF\kinematic_pair.pair_placement_in_second_link_context,
          surface_2);
END_ENTITY:
(*
```

Attribute definitions:

surface_1: the contact surface on the first link, defined in the coordinate system specified by
SELF\kinematic_pair_placement_in_first_link_context.

surface_2: the contact surface on the second link, defined in the coordinate system specified
by SELF\kinematic_pair_pair_placement_in_second_link_context.

orientation: an indication of whether the z-direction of the second surface agrees with the z-direction of the first surface.

Formal propositions:

WR1: surface_1 of a surface_pair shall be in the items set of a kinematic_frame_back-ground_representation which, in turn, is related to the kinematic_link_representation of the first link of the surface_pair by a kinematic_frame_background_representation_association. The transformer_frame in the transformation_operator of this relationship shall be the pair_placement_in_first_link_context of the surface_pair. These requirements are checked by the function frame_associated_to_background.

WR2: surface_2 of a surface_pair shall be in the items set of a kinematic_frame_back-ground_representation which, in turn, is related to the kinematic_link_representation of the second link of the surface_pair by a kinematic_frame_background_representation_association. The transformer_frame in the transformation_operator of this relationship shall be the pair_placement_in_second_link_context of the surface_pair. These requirements are checked by the function frame_associated_to_background.

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Informal propositions:

continuous surfaces: The surfaces used as surface_1 and surface_2 shall be smooth in their entire domain, and their tangent vectors shall change their direction only in a steady manner, regardless of whether the surfaces are composed of multiple surfaces or not.

NOTE 4 - This is equivalent to requiring surface_1 and surface_2 to be G1 continuous throughout and that, in the case of a rectangular_composite_surface, the transition_code shall be at least cont_same_gradient at each segment junction curve. (See ISO 10303-42.)

orientation: If the directions z_q and z_c^p are identical, the orientation shall be set TRUE. If the directions z_q and z_c^p are oriented in the opposite direction to each other, the orientation shall be set FALSE.

5.4.50 surface_pair_range

The **surface_pair_range** specifies the lower bound and the upper bound of the parameter range for the **surface_pair**.

EXPRESS specification:

```
*)
ENTITY surface_pair_range
 SUBTYPE OF (simple_pair_range);
 SELF\simple_pair_range.applies_to_pair : surface_pair;
 range_on_surface_1
                                         : rectangular_trimmed_surface;
 range_on_surface_2
                                         : rectangular_trimmed_surface;
 lower_limit_actual_rotation
                                         : rotational_range_measure;
 upper_limit_actual_rotation
                                         : rotational_range_measure;
WHERE
 WR1: SELF\simple_pair_range.applies_to_pair\surface_pair.surface_1 :=:
       range_on_surface_1.basis_surface;
 WR2: SELF\simple_pair_range.applies_to_pair\surface_pair.surface_2 :=:
       range_on_surface_2.basis_surface;
 WR3: (('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (lower_limit_actual_rotation))
        ('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (upper_limit_actual_rotation)))
       (lower_limit_actual_rotation < upper_limit_actual_rotation);</pre>
END_ENTITY;
```

Attribute definitions:

SELF\simple_pair_range.applies_to_pair: the surface_pair to which the surface_pair_range applies.

range_on_surface_1: the admissible range for the positional pair parameter value on the first contact surface.

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range_on_surface_2: the admissible range for the positional pair parameter value on the second contact surface.

lower_limit_actual_rotation: the minimum value of the pair rotation parameter.

upper_limit_actual_rotation: the maximum value of the pair rotation parameter.

Formal propositions:

WR1: The underlying surface of range_on_surface_1 in the range specification shall be identical with the surface surface_1 in the surface_pair specification.

WR2: The underlying surface of range_on_surface_2 in the range specification shall be identical with the surface surface_2 in the surface_pair specification.

WR3: The range of rotation of the surface_pair shall be positive when both bounds are not given as unlimited.

5.4.51 sliding_surface_pair

A sliding_surface_pair specifies the sliding motion between the two contact surfaces of a surface_pair. See 5.4.49.

EXPRESS specification:

```
*)
ENTITY sliding_surface_pair
SUBTYPE OF (surface_pair);
END_ENTITY;
(*
```

5.4.52 sliding_surface_pair_value

The sliding_surface_pair_value specifies the set of pair parameters for the sliding_surface_pair. See 5.4.49.

EXPRESS specification:

```
#)
ENTITY sliding_surface_pair_value
  SUBTYPE OF (pair_value);
SELF\pair_value.applies_to_pair : sliding_surface_pair;
actual_point_on_surface_1 : point_on_surface;
actual_point_on_surface_2 : point_on_surface;
actual_rotation : plane_angle_measure;
WHERE
  WR1: SELF\pair_value.applies_to_pair\surface_pair.surface_1 :=:
        actual_point_on_surface_1.basis_surface;
WR2: SELF\pair_value.applies_to_pair\surface_pair.surface_2 :=:
        actual_point_on_surface_2.basis_surface;
END_ENTITY;
(*
```

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Attribute definitions:

SELF\pair_value.applies_to_pair: the sliding_surface_pair to which the sliding_surface_pair_value applies.

actual_point_on_surface_1: the contact point of the contact surface (surface_1) of the first link.

actual_point_on_surface_2: the contact point of the contact surface (surface_2) of the second link.

actual_rotation: the angle required to rotate the x_c^p -direction of the first link surface around the z_c -direction of that surface until it coincides with the x_c -direction of the second link surface. Formal propositions:

WR1: actual_point_on_surface_1 shall be defined as a point on surface_1 of the surface_pair referenced by applies_to_pair.

WR2: actual_point_on_surface_2 shall be defined as a point on surface_2 of the surface_pair referenced by applies_to_pair.

5.4.53 rolling_surface_pair

A rolling_surface_pair specifies the rolling motion between the two contact surfaces of a surface_pair.

EXPRESS specification:

```
*)
ENTITY rolling_surface_pair
  SUBTYPE OF (surface_pair);
END_ENTITY;
(*
```

5.4.54 rolling_surface_pair_value

The rolling_surface_pair_value specifies the set of pair parameters for the rolling_surface_pair. See 5.4.49.

EXPRESS specification:

```
*)
ENTITY rolling_surface_pair_value
SUBTYPE OF (pair_value);
SELF\pair_value.applies_to_pair : rolling_surface_pair;
actual_point_on_surface : point_on_surface;
actual_rotation : plane_angle_measure;
WHERE
WR1: SELF\pair_value.applies_to_pair\surface_pair.surface_1 :=:
    actual_point_on_surface.basis_surface;
END_ENTITY;
(*
```

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Attribute definitions:

SELF\pair_value.applies_to_pair: the rolling_surface_pair to which the rolling_surface_pair_value applies.

actual_point_on_surface: the contact point of the contact surface (surface_1) of the first link.

actual_rotation: the angle required to rotate the x_c^p -direction of the first link surface around the z_c -direction of that surface until it coincides with the x_c -direction of the second link surface.

Formal propositions:

WR1: actual_point_on_surface shall be defined as a point on surface_1 of the surface_pair referenced by applies_to_pair.

5.4.55 point_on_planar_curve_pair

The **point_on_planar_curve_pair** constrains the motion of two links such that a point defined on the second link always lies on a planar curve defined on the first link. The actual location of this point on the curve is called the contact point.

NOTE 1 — Translational motion of the second link is constrained to the one-dimensional parameter space of the curve, while its rotational motion about the contact point is not constrained. Therefore, a point_on_planar_curve_pair behaves like a spherical_pair that additionally may move along a curve on the first link.

The contact point specifies the origin of a frame called the contact frame. The x-axis of the contact frame is parallel to the tangent to the curve in the contact point and points into the direction where the curve parameter increases. The y-axis of the contact frame is normal to the plane in which the curve is defined. Hence, the z-axis of the contact frame coincides with a local normal to the curve which lies in the plane of the curve and passes the contact point.

NOTE 2 – See figure 13. In this case **orientation** is TRUE, as the y_c^1 -axis has the same direction as the z_1 -axis.

To support the measure of motion, a pair frame is defined on each of the links. The representation f(u) of the two-dimensional curve is given in the xy-plane of the pair frame on the first link. Therefore, the z-axis of this pair frame always serves as the normal to the plane of the curve.

NOTE 3 – The definition of the curve plane and of its normal as specified here becomes important for cases where the curve is a straight line.

The translational motion is given by the actual curve parameter of the contact point, u_1 . The three angles of rotation are defined as the yaw, pitch, and roll angles. See 5.3.6. They are required to rotate the x-, y-, and z-axes of the contact frame until its directions coincide with the axis directions of the second pair frame.

The origin of the pair frame on the second link coincides with the contact point, and the axes of this pair frame agree with the axes of the contact frame when all three rotations have been performed.

The following notation is used in the subsequent specification:

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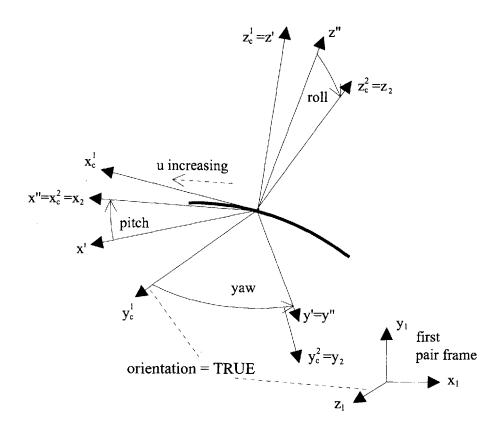


Figure 13 - Example of a point on planar curve pair

u	parameter of the curve on the first link;
u_1	parameter of the contact point on the curve on the first link;
f(u)	representation of the curve on the first link relative to the first pair frame;
x_1,y_1,z_1	axes of the first pair frame;
x_2,y_2,z_2	axes of the second pair frame;
x_c^1,y_c^1,z_c^1	axes of the contact frame, defined with respect to the first pair frame, but not
	taking into account the rotational motion;
x',y',z'	axes of the contact frame, defined with respect to the first pair frame, when
	the yaw rotation has been taken into account;
x'', y'', z''	axes of the contact frame, defined with respect to the first pair frame, when
	the yaw and pitch rotations have been taken into account;
x_c^2,y_c^2,z_c^2	axes of the contact frame, defined with respect to the first pair frame, when
	all the ypr rotations have been taken into account;

In order to migrate from the first pair frame to the second pair frame, the following sequence of transformations has to be performed:

1) Establish the contact frame ${}^{1}PF_{c}$ relative to the first pair frame:

$$\overline{origin}_c^1 = f(u_1)$$

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$$\overline{x_vector}_c^1 = \frac{df(u)}{du}\Big|_{u=u_1}$$
;

$$\overline{x}_{c}^{1} = \frac{\overline{x_vector}_{c}^{1}}{|\overline{x_vector}_{c}^{1}|}$$

 y_c^1 is required to be parallel to z_1 ; hence, either

$$\overline{y}_c^1 = \overline{z}_1$$

or

$$\overline{y}_c^1 = -\overline{z}_1$$

In the first case, orientation is TRUE and the direction of y_c^1 agrees with that of z_1 . In the second case, orientation is FALSE and the direction of y_c^1 is opposite to that of z_1 .

$$\overline{z_c^1} = \overline{x_c^1} \times \overline{y_c^1} ; \qquad \overline{z_c^1} = \frac{\overline{z_c vector_c^1}}{|\overline{z_c vector_c^1}|}$$

 \overline{origin}_c^1 and the three direction vectors \overline{x}_c^1 , \overline{y}_c^1 , and \overline{z}_c^1 may be used to establish the rigid homogeneous matrix representation of the placement of the contact frame 1PF_c relative to the first pair frame.

- 2) Rotate the x_c^1, y_c^1 -axes about the z_c^1 -axis by the amount specified by the yaw angle. This yields an intermediate frame the axes of which are denoted by $(x', y', z' = z_c^1)$.
- 3) Rotate the z',x'-axes about the y'-axis by the amount specified by the pitch angle. This yields a second intermediate frame denoted by (x'',y''=y',z'').
- 4) Finally, rotate the y'',z''-axes about the x''-axis by the amount specified by the roll angle. The resulting frame $(x_c^2 = x'', y_c^2, z_c^2)$ now coincides with the pair frame on the second link, denoted by (x_2, y_2, z_2) .

EXPRESS specification:

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Attribute definitions:

pair_curve: the planar curve on the first link of the pair on which the point on the second link is sliding.

orientation: a flag indicating whether the y-axis of the unrotated contact frame agrees with the z-axis of the pair frame on the first link.

Formal propositions:

WR1: The pair_curve of a point_on_planar_curve_pair shall be in the items set of a kinematic_frame_background_representation which, in turn, is related to the kinematic_link_representation of the first link of the point_on_planar_curve_pair by a kinematic_frame_background_representation_association. The transformer_frame in the transformation_operator of this relationship shall be the pair_placement_in_first_link_context of the point_on_planar_curve_pair. These requirements are checked by the function frame_associated_to_background.

Informal propositions:

planar curve: The curve used as pair_curve shall be planar.

continuous curve: The curve used as pair_curve shall be smooth in its entire domain, and its tangent vector shall change its direction only in a steady manner, regardless of whether the curve is composed of multiple curves or not.

NOTE 4 - This is equivalent to requiring the **pair_curve** to be G1 continuous throughout and that, in the case of a **composite_curve**, the **transition_code** shall be at least **cont_same_gradient** at each segment junction point. (See ISO 10303-42.)

orientation: If the directions z_1 and y_c^1 are identical, the orientation shall be TRUE. If the directions z_1 and y_c^1 are oriented in the opposite direction, the orientation shall be FALSE.

5.4.56 point_on_planar_curve_pair_value

The point_on_planar_curve_pair_value specifies the pair parameters for the point_on_planar_curve_pair.

EXPRESS specification:

WHERE

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Attribute definitions:

SELF\pair_value.applies_to_pair: the point_on_planar_curve_pair to which the point_on_planar_curve_pair_value applies.

actual_point_on_curve: the positional value for the point on the curve.

input_orientation: the input specification of the rotational pair parameter values from which the actual_orientation is derived. input_orientation is either a ypr_rotation or a rotation_about_direction.

actual_orientation: the array of rotational pair parameter values for a point_on_planar_curve_pair according to the ypr notation. This is derived from input_orientation by the function convert_spatial_to_ypr_rotation.

Formal propositions:

WR1: actual_point_on_curve shall be defined as a point on the pair_curve of the point_on_planar_curve_pair referenced by applies_to_pair.

5.4.57 point_on_planar_curve_pair_range

The **point_on_planar_curve_pair_range** specifies the lower bound and the upper bound of the parameter range for the **point_on_planar_curve_pair**.

EXPRESS specification:

```
*)
ENTITY point_on_planar_curve_pair_range
  SUBTYPE OF (simple_pair_range);
  SELF\simple_pair_range.applies_to_pair : point_on_planar_curve_pair;
                                         : trimmed_curve;
 range_on_pair_curve
  lower_limit_yaw
                                         : rotational_range_measure;
  upper_limit_yaw
                                         : rotational_range_measure;
  lower_limit_pitch
                                         : rotational_range_measure;
  upper_limit_pitch
                                         : rotational_range_measure;
  lower_limit_roll
                                         : rotational_range_measure;
  upper_limit_roll
                                         : rotational_range_measure;
WHERE
 WR1: SELF\simple_pair_range.applies_to_pair\
            point_on_planar_curve_pair.pair_curve
       :=: range_on_pair_curve.basis_curve;
  WR2: (('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (lower_limit_yaw))
        ('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (upper_limit_yaw)))
       XOR
```

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Attribute definitions:

SELF\simple_pair_range.applies_to_pair: the point_on_planar_curve_pair to which the point_on_planar_curve_pair_range applies.

range_on_pair_curve: the admissible range for the positional pair parameter value on the contact curve on the first link.

lower_limit_yaw: the minimum value of the yaw angle for the point_on_planar_curve_pair.

upper_limit_yaw: the maximum value of the yaw angle for the point_on_planar_curve_pair.

lower_limit_pitch: the minimum value of the pitch angle for the point_on_planar_curve_pair.

upper_limit_pitch: the maximum value of the pitch angle for the point_on_planar_curve_pair.

lower_limit_roll: the minimum value of the roll angle for the point_on_planar_curve_pair.

upper_limit_roll: the maximum value of the roll angle for the point_on_planar_curve_pair. Formal propositions:

WR1: The underlying curve of range_on_pair_curve in the range specification shall be identical with the curve pair_curve in the point_on_planar_curve_pair specification.

WR2: The range of rotation about the z-axis of the point_on_planar_curve_pair shall be positive when both bounds are not given as unlimited.

WR3: The range of rotation about the y-axis of the **point_on_planar_curve_pair** shall be positive when both bounds are not given as unlimited.

WR4: The range of rotation about the x-axis of the point_on_planar_curve_pair shall be positive when both bounds are not given as unlimited.

5.4.58 planar_curve_pair

A planar_curve_pair constrains the motion of two links along a planar curve on each of the links. Both curves lie in a common plane whose normal is called \bar{z}_c . The point of contact lies on the curves. The point is called the contact point, and the contact point specifies the origin of a frame called a contact frame. The common plane is the xy-plane of the contact frame. To measure motion, a pair frame is defined on each of the links. The representation f(u) of the twodimensional curves is given in the xy-plane of the corresponding pair frame. For the subsequent specification both curve representations need to be expressed in a common coordinate system. The world coordinate system is used for this purpose.

The following notation is used:

parameter of the curve on the first link; u_p

parameter of the curve on the second link;

 ${}^0 f_p(u_p)$ representation of the curve on the first link relative to the world coordinate system:

 $^{0}f_{q}(u_{q})$ representation of the curve on the second link relative to the world coordinate system;

axes of the first pair frame; x_p, y_p, z_p

axes of the second pair frame; x_q, y_q, z_q

 x_c^p, y_c^p, z_c^p axes of the contact frame, defined with respect to the first pair frame, but not taking into account the curve orientations;

 $x_c^q,\,y_c^q,\,z_c^q$ axes of the contact frame, defined with respect to the second pair frame;

axes of the contact frame, defined with respect to the first pair frame after the x_c, y_c, z_c curve orientations have been taken into account.

NOTE 1 - See figure 14 for an exploded view of a curve pair. In this case orientation is FALSE, as the x-axes have opposite directions.

The following equations apply to sliding_curve_pair and rolling_curve_pair.

The contact frame is determined from both sides of the pair as follows, beginning with the second link:

$$\overline{origin}_c^q = {}^0\!f_q(u_q)$$

 $\overline{z}_c^q = \overline{z}_c$ (normal of the common plane)

$$\left. \overline{y_vector}_c^q = \frac{d^{\,0}f_q(u)}{du} \right|_{u=u_q}; \qquad \qquad \overline{y}_c^q = \frac{\overline{y_vector}_c^q}{\overline{|y_vector}_c^q|}$$

$$\overline{x_{-}vector_{c}^{q}} = \overline{y}_{c}^{q} \times \overline{z}_{c}^{q} \; ; \qquad \qquad \overline{x}_{c}^{q} = \frac{\overline{x_{-}vector_{c}^{q}}}{|\overline{x_{-}vector_{c}^{q}}|}$$

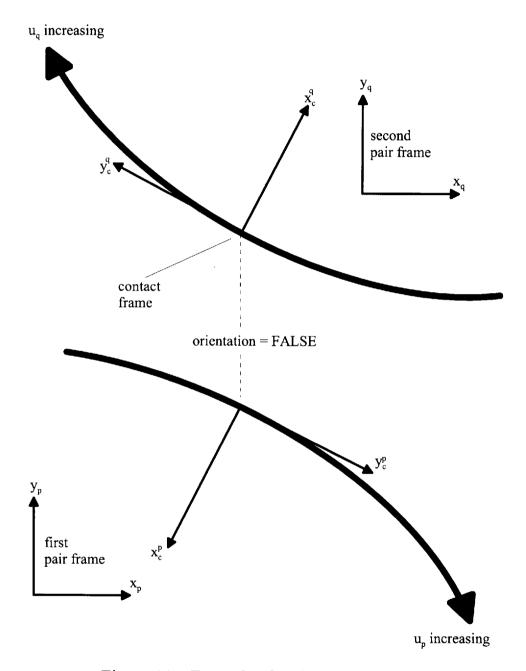


Figure 14 - Example of a planar curve pair.

 \overline{origin}_c^q and the three direction vectors \overline{x}_c^q , \overline{y}_c^q , and \overline{z}_c^q may be used to establish the rigid homogeneous matrix representation of the placement of the contact frame ${}^{q}PF_{c}$ relative to the second pair frame.

NOTE 2 - See figure 3 for an illustration of the relationships between the frames.

The same analysis is performed for the first link.

$$\overline{origin}_c^p = {}^0f_p(u_p)$$

 $\overline{z}_c^p = \overline{z}_c$ (normal of the common plane)

$$\overline{y_{\cdot}vector_{c}^{p}} = \frac{d^{0}f_{p}(u)}{du}\Big|_{u=u_{p}}; \qquad \overline{y}_{c}^{p} = \frac{\overline{y_{\cdot}vector_{c}^{p}}}{|\overline{y_{\cdot}vector_{c}^{p}}|};$$

$$\overline{x_{-}vector_{c}^{p}} = \overline{y}_{c}^{p} \times \overline{z}_{c}^{p} \; ; \qquad \qquad \overline{x}_{c}^{p} = \frac{\overline{x_{-}vector_{c}^{p}}}{|\overline{x_{-}vector_{c}^{p}}|}$$

The contact point shall be identically positioned, relative to the world coordinate system, irrespective of whether it is approached from the second or the first link.

$$\overline{origin}_c = \overline{origin}_c^p = \overline{origin}_c^q$$

The z-directions are all normal to the same plane; hence

$$\overline{z}_c = \overline{z}_c^p = \overline{z}_c^q$$

At this stage, the direction vectors \overline{x}_c^q and \overline{x}_c^p are either

- 1) $\overline{x}_c = \overline{x}_c^q = \overline{x}_c^p$ or
- $2) \quad \overline{x}_c = \overline{x}_c^q = -\overline{x}_c^p$

In case 1, orientation is TRUE and both x-directions are identical.

In case 2, orientation is FALSE and x_c^p (as well as y_c^p) is rotated by π about the z_c direction. EXPRESS specification:

```
ENTITY planar_curve_pair
```

SUBTYPE OF (kinematic_pair); : curve;

curve_1 curve_2 : curve;

orientation : BOOLEAN;

WHERE

*)

WR1: frame_associated_to_background

(SELF\kinematic_pair.pair_placement_in_first_link_context,

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Attribute definitions:

curve_1: the contact curve on the first link, defined in the coordinate system specified by SELF\kinematic_pair.pair_placement_in_first_link_context. This curve shall lie within a plane.

curve_2: the contact curve on the second link, defined in the coordinate system specified by SELF\kinematic_pair_pair_placement_in_second_link_context. This curve shall lie within a plane.

orientation: a flag indicating whether the x-axis-directions agree.

Formal propositions:

WR1: curve_1 of a planar_curve_pair shall be in the items set of a kinematic_frame_background_representation which, in turn, is related to the kinematic_link_representation of the first link of the planar_curve_pair by a kinematic_frame_background_representation_association. The transformer_frame in the transformation_operator of this relationship shall be the pair_placement_in_first_link_context of the planar_curve_pair. These requirements are checked by the function frame_associated_to_background.

WR2: curve_2 of a planar_curve_pair shall be in the items set of a kinematic_frame_background_representation which, in turn, is related to the kinematic_link_representation of the second link of the planar_curve_pair by a kinematic_frame_background_representation_association. The transformer_frame in the transformation_operator of this relationship shall be the pair_placement_in_second_link_context of the planar_curve_pair. These requirements are checked by the function frame_associated_to_background.

Informal propositions:

planar curves: The curves used as curve_1 and curve_2 shall be planar curves.

continuous curves: The curves used as curve_1 and curve_2 shall be smooth in their entire domain, and their tangent vectors shall change their direction only in a steady manner, regardless of whether the curves are composite or not.

NOTE 3 – This is equivalent to requiring **curve_1** and **curve_2** to be G1 continuous throughout and that, in the case of a **composite_curve**, the **transition_code** shall be at least **cont_same_gradient** at each segment junction point. (See ISO 10303-42.)

orientation: If the directions x_q and x_c^p are identical, the orientation shall be TRUE. If the directions x_q and x_c^p are oriented in the opposite direction, the orientation shall be FALSE.

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5.4.59 planar_curve_pair_range

The planar_curve_pair_range specifies the lower bound and the upper bound of the parameter range of the planar_curve_pair.

EXPRESS specification:

Attribute definitions:

SELF\simple_pair_range.applies_to_pair: the planar_curve_pair to which the planar_curve_pair_range applies.

range_on_curve_1: the admissible range for the positional pair parameter value on the curve on the first link of the pair.

range_on_curve_2: the admissible range for the positional pair parameter value on the curve on the second link of the pair.

Formal propositions:

WR1: The underlying curve of range_on_curve_1 in the range specification shall be identical with the curve curve_1 in the planar_curve_pair specification.

WR2: The underlying curve of range_on_curve_2 in the range specification shall be identical with the curve curve_2 in the planar_curve_pair specification.

5.4.60 sliding_curve_pair

A sliding_curve_pair specifies the sliding motion between the curves on the two links of a planar_curve_pair.

EXPRESS specification:

```
*)
ENTITY sliding_curve_pair
  SUBTYPE OF (planar_curve_pair);
END_ENTITY;
(*
```

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5.4.61 sliding_curve_pair_value

The sliding_curve_pair_value specifies the pair parameters for the sliding_curve_pair.

EXPRESS specification:

```
*)
ENTITY sliding_curve_pair_value
  SUBTYPE OF (pair_value);
  SELF\pair_value.applies_to_pair : sliding_curve_pair;
  actual_point_on_curve_1 : point_on_curve;
  actual_point_on_curve_2 : point_on_curve;
WHERE
  WR1: SELF\pair_value.applies_to_pair\planar_curve_pair.curve_1 :=:
        actual_point_on_curve_1.basis_curve;
  WR2: SELF\pair_value.applies_to_pair\planar_curve_pair.curve_2 :=:
        actual_point_on_curve_2.basis_curve;
END_ENTITY;
(*
```

Attribute definitions:

SELF\pair_value.applies_to_pair: the sliding_curve_pair to which the sliding_curve_pair_value applies.

actual_point_on_curve_1: the contact point, defined in the parameter space of the curve on the first link.

actual_point_on_curve_2: the contact point, defined in the parameter space of the curve on the second link.

Formal propositions:

WR1: actual_point_on_curve_1 shall be defined as a point on curve_1 of the planar_curve_pair referenced by applies_to_pair.

WR2: actual_point_on_curve_2 shall be defined as a point on curve_2 of the planar_curve_pair referenced by applies_to_pair.

5.4.62 rolling_curve_pair

A rolling_curve_pair specifies the rolling motion between the curves on the two links of a planar_curve_pair.

EXPRESS specification:

```
*)
ENTITY rolling_curve_pair
  SUBTYPE OF (planar_curve_pair);
END_ENTITY;
(*
```

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5.4.63 rolling_curve_pair_value

The rolling_curve_pair_value specifies the pair parameter for the rolling_curve_pair.

EXPRESS specification:

```
*)
ENTITY rolling_curve_pair_value
   SUBTYPE OF (pair_value);
   SELF\pair_value.applies_to_pair : rolling_curve_pair;
   actual_point_on_curve_1 : point_on_curve;
WHERE
   WR1: SELF\pair_value.applies_to_pair\planar_curve_pair.curve_1 :=:
        actual_point_on_curve_1.basis_curve;
END_ENTITY;
(*
```

Attribute definitions:

SELF\pair_value.applies_to_pair: the rolling_curve_pair to which the rolling_curve_pair_value applies.

actual_point_on_curve_1: the contact point, defined in the parameter space of the curve on the first link.

Formal propositions:

WR1: actual_point_on_curve_1 shall be defined as a point on curve_1 of the planar_curve_pair referenced by applies_to_pair.

5.4.64 gear_pair

The **gear_pair** constrains the motion between two adjacent links to a rolling (and potentially sliding) motion of the second link along the first link.

To measure the motion of the second link with respect to the first link, a frame is defined on each of the links such that the origin lies in the center of the rolling circle of the respective link.

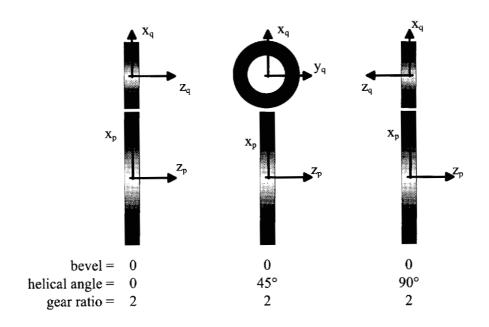
NOTE 1 - See figure 15, where different values of the constants "bevel", "helical_angle", and "gear_ratio" are shown. The lower gear always represents the first link; the upper gear is the second link.

The direction of the z-axis is perpendicular to the plane of the circle. In a reference situation (with both rotation values being zero) the x-axis of the first link points from the origin towards the point of contact with the second link, while on the second link the x-axis points away from the point of contact.

Motion is measured in terms of the rotation of the contact point about the z-axis of the first link. The motion of the second link results from an analysis of the rolling process. At any instance the motion of the second link may be considered as a rotation of the second gear axis about the first gear axis while maintaining the distance (sum of the radii), the bevel, and the helical angle plus a rotation of the second gear about its own axis according to:

 $actual_rotation_2 = -gear_ratio \cdot actual_rotation_1$

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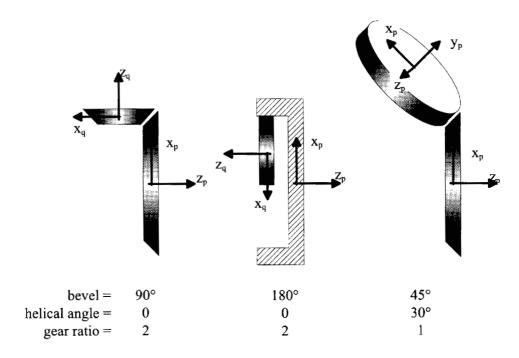


Figure 15 - Examples of gear pairs in different situations.

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Thus absolute bevel values between 0 and $\frac{\pi}{2}$ represent external gears while absolute bevel values between $\frac{\pi}{2}$ and π represent internal gears.

The angle between the two x-axis directions is given by the bevel according to

$$\overline{x}_p \cdot \overline{x}_q = \cos(bevel)$$

with $bevel \in]-\pi,\pi]$,

where in case of $\cos(bevel) = 0$, the sign of the bevel is defined according to:

$$\overline{y}_p \cdot (\overline{x}_p \times \overline{x}_q) = sign(bevel)$$

The angle between the two y-axis directions is given by the helical angle according to:

$$\overline{y}_p \cdot \overline{y}_q = \cos(helical_angle)$$

with $helical_angle \in]-\pi,\pi],$

where in case of $cos(helical_angle) = 0$, the sign of the helical angle is defined according to:

$$\overline{x}_q \cdot (\overline{y}_p \times \overline{y}_q) = sign(helical_angle)$$

NOTE 2 – In some cases the gear ratio depends on the radii of the rolling circles and also on the characteristics of the gear toothing such as in worm gears. For this reason the gear ratio is defined and not derived from the ratio of the two radii. Hence, the two radii are used to determine the geometrical arrangement of the two gears relative to each other in conjunction with bevel and helical angle, while the gear ratio determines the ratio of the second gear motion with respect to the rotation of the contact point about the first gear axis.

One way to construct the geometrical arrangement of the second gear relative to the first one is as follows:

An auxiliary frame is introduced at the point of contact with its axes x_a , y_a , and z_a all parallel to the respective axes of the first link frame. Now the auxiliary frame is rotated by the angle bevel about its y_a -axis followed by a rotation by the helical angle about the (previously rotated) x_a -axis. Now the x_a - y_a -plane represents the plane in which the second gear lies.

EXPRESS specification:

```
*)
ENTITY gear_pair
   SUBTYPE OF (kinematic_pair);
   radius_first_link : length_measure;
   radius_second_link : length_measure;
   bevel : plane_angle_measure;
   helical_angle : plane_angle_measure;
   gear_ratio : REAL;
END_ENTITY;
(*
```

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Attribute definitions:

radius_first_link: the radius of the rolling circle of the first link.

radius_second_link: the radius of the rolling circle of the second link.

bevel: the angle between the two x-axes.

helical_angle: the angle between the two y-axes.

gear_ratio: the gear ratio of the pair.

5.4.65 gear_pair_value

The gear_pair_value specifies the pair parameters for the gear_pair.

NOTE – If the gear pair is part of a more complex gear mechanism, the gear pair values as defined here may not be the primary design targets. In the case of a planetary gear mechanism, for example, it is more important to know the rotation angles of the planetary gears with respect to an inertial coordinate system than the rotation angles between the planetary gears and the frames which support them. See [1] for a detailed description of this specific example.

For a given configuration of pairs within a mechanism, the more global motion parameters can be derived, in general, from the individual pair parameters and vice versa. This is not possible, however, generically without knowledge of the configuration. Therefore, the specification of functions which provide such derivations is left to an application protocol for which these derivations are required.

EXPRESS specification:

Attribute definitions:

SELF\pair_value.applies_to_pair: the gear_pair to which the gear_pair_value applies.

actual_rotation_1: the value of the pair parameter of the first link.

actual_rotation_2: the value of the pair parameter of the second link.

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5.4.66 gear_pair_range

The **gear_pair_range** specifies the lower bound and the upper bound of the parameter range of the **gear_pair**.

EXPRESS specification:

```
*)
ENTITY gear_pair_range
  SUBTYPE OF (simple_pair_range);
  SELF\simple_pair_range.applies_to_pair : gear_pair;
                                : rotational_range_measure;
  lower_limit_actual_rotation_1
  upper_limit_actual_rotation_1
                                        : rotational_range_measure;
WHERE
  WR1: (('KINEMATIC STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (lower_limit_actual_rotation_1))
        ('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (upper_limit_actual_rotation_1)))
       (lower_limit_actual_rotation_1 <
        upper_limit_actual_rotation_1);
END_ENTITY;
```

Attribute definitions:

SELF\simple_pair_range.applies_to_pair: the gear_pair to which the gear_pair_range applies.

lower_limit_actual_rotation_1: the minimum value of the pair parameter of the first link.

upper_limit_actual_rotation_1: the maximum value of the pair parameter of the first link.

Formal propositions:

WR1: The range of rotation of the **gear_pair** shall be positive when both bounds are not given as unlimited.

5.4.67 rack_and_pinion_pair

The **rack_and_pinion_pair** describes a pinion rolling on a rack where the rotation axis of the pinion is perpendicular to the direction of the rack.

NOTE – See figure 16. The rack and pinion pair may be considered as a special case of the rolling_curve_pair with one curve being a straight line and the other a circle.

The rack is always the first link; the pinion is the second link. The rack_and_pinion_pair constrains the motion between two adjacent links to a translation along a common axis and a rotation about an axis perpendicular to it.

To measure the motion of the second link with respect to the first link, a frame is defined on each of the links. On the pinion, the origin is the center of the rolling circle. The direction of the z-axis on both rack and pinion is perpendicular to the plane of the circle.

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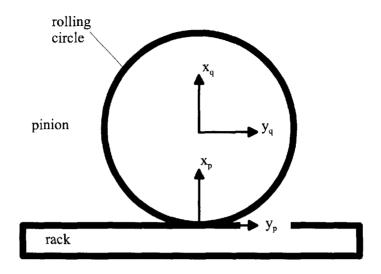


Figure 16 - Example of a rack and pinion pair in the reference situation

In a reference situation (with both pair parameter values being zero), the x-axis of the pinion points from the origin away from the point of contact with the rack. In the same reference situation, the x-axis of the rack points from the point of contact towards the center of the pinion. Motion is measured in terms of the translation of the contact point along the y-axis of the rack (first link). The motion of the second link results from an analysis of the rolling process. At any instance the motion of the second link is composed of a translation and a rotation where the rotation part is calculated from:

$$actual_rotation = \frac{actual_displacement}{pinion_radius}$$

EXPRESS specification:

```
*)
ENTITY rack_and_pinion_pair
  SUBTYPE OF (kinematic_pair);
  pinion_radius : length_measure;
END_ENTITY;
(*
```

Attribute definitions:

pinion_radius: the radius of the rolling circle of the pinion.

5.4.68 rack_and_pinion_pair_value

The rack_and_pinion_pair_value specifies the pair parameters for the rack_and_pinion_pair. EXPRESS specification:

```
*)
ENTITY rack_and_pinion_pair_value
SUBTYPE OF (pair_value);
```

```
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```

Attribute definitions:

SELF\pair_value.applies_to_pair: the rack_and_pinion_pair to which the rack_and_pinion_pair_value applies.

actual_displacement: the value of the pair parameter for the rack.

actual_rotation: the resulting rotation of the pinion.

5.4.69 rack_and_pinion_pair_range

The rack_and_pinion_pair_range specifies the lower bound and the upper bound of the parameter range for the rack_and_pinion_pair.

EXPRESS specification:

```
*)
ENTITY rack_and_pinion_pair_range
  SUBTYPE OF (simple_pair_range);
  SELF\simple_pair_range.applies_to_pair : rack_and_pinion_pair;
                                   : translational_range_measure;
  lower_limit_rack_displacement
                                         : translational_range_measure;
  upper_limit_rack_displacement
WHERE
  WR1: (('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (lower_limit_rack_displacement))
        OR
        ('KINEMATIC_STRUCTURE_SCHEMA.UNLIMITED_RANGE' IN
         TYPEOF (upper_limit_rack_displacement)))
       (lower_limit_rack_displacement < upper_limit_rack_displacement);</pre>
END_ENTITY;
```

Attribute definitions:

SELF\simple_pair_range.applies_to_pair: the rack_and_pinion_pair to which the rack_and_pinion_pair_range applies.

lower_limit_rack_displacement: the minimum value of the pair parameter for the rack.

upper_limit_rack_displacement: the maximum value of the pair parameter for the rack.

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Formal propositions:

WR1: The range of motion of the rack_and_pinion_pair shall be positive when both bounds are not given as unlimited.

5.4.70 kinematic_substructure

A kinematic_substructure specifies the topological characteristics of a mechanism in terms of tree or network structures.

NOTES

1 – Using graph theory, the topology of a mechanism is represented by a directed graph, where the links correspond to the nodes, and the joints correspond to the edges. This graph can be derived from the definition of the links and joints. If the topology of a mechanism is defined only by this minimal information, it is referred to as "lower level topology" within this part of ISO 10303.

Graph theory provides a means to capture connectivity information which may be applied to the describe the topological structure of mechanisms. The geometrical and mechanical properties are not conveyed. If the full topological information including connectivity information is provided explicitly, this is referred to as "higher level topology" within this part of ISO 10303.

A general graph may be composed of two basic types of subgraphs:

- Trees;
- Networks.

If, in addition to the lower level of topology, the higher level topology is provided in a kinematic model, this higher level of topology is represented by kinematic substructures. These kinematic substructures are:

- a kinematic tree structure, whose graph representation is a single oriented tree and which consists only of oriented kinematic joints connecting the kinematic links;
- a kinematic network structure, whose graph representation consists of oriented kinematic loops.
- 2 See [3] for methods that can be applied to analyze a kinematic_substructure.

EXPRESS specification:

Attribute definitions:

parent_structure: the kinematic_structure of which the kinematic_substructure forms a component.

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5.4.71 kinematic_network_structure

The kinematic_network_structure represents a subgraph of network type; i.e., the mechanism is composed of closed kinematic chains.

NOTES

- 1 See figure 17 for an illustration of a kinematic network structure.
- 2 This entity is present in an instance of a kinematics model only if the kinematic structure takes the form of a directed graph.

EXPRESS specification:

```
*)
ENTITY kinematic_network_structure
  SUBTYPE OF (kinematic_substructure);
END_ENTITY;
(*
```

5.4.72 kinematic_tree_structure

The kinematic_tree_structure represents a subgraph of tree type; i.e., the mechanism is composed of open kinematic chains.

NOTES

- 1 See figure 18 for an illustration of a kinematic tree structure.
- 2 This entity is present in an instance of a kinematics model only if the kinematic structure takes the form of a directed graph.

EXPRESS specification:

```
*)
ENTITY kinematic_tree_structure
  SUBTYPE OF (kinematic_substructure);
END_ENTITY;
(*
```

5.4.73 kinematic_loop

The **kinematic_loop** represents a cycle in the subgraph. It is the representation of a closed kinematic chain in a mechanism, where the last link in the chain is again connected to the first link by a joint. The **kinematic_loop** is analogous to the loop in the topology model, where the joints correspond to the edges and the links correspond to the vertices of the topology model. The loop shall be pointed to by at least one **joint_logical_relationship**.

Every kinematic_joint shall be oriented such that the list of kinematic_joints have a common orientation within the loop.

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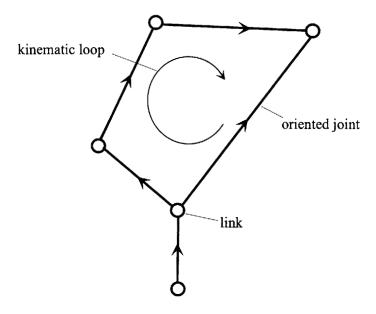


Figure 17 - Example of a kinematic network structure

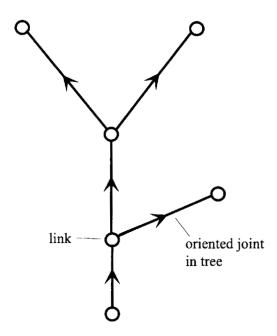


Figure 18 - Example of a kinematic tree structure

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NOTE - This entity is present in an instance of a kinematics model only if the kinematic structure takes the form of a directed graph.

EXPRESS specification:

```
ENTITY kinematic_loop;
  network : kinematic_network_structure;
WHERE
  WR1 : SIZEOF(USEDIN(SELF,
        'kinematic_structure_schema.joint_logical_relationship.loop'))>0;
  WR2 : SIZEOF (QUERY( relation_1 <* USEDIN(SELF,
         'kinematic_structure_schema.joint_logical_relationship.loop') |
          SIZEOF(QUERY( relation_2 <* (USEDIN (SELF,</pre>
            'kinematic_structure_schema.joint_logical_relationship.loop')
             - relation_1) |
               NOT(connected_in_simple_loop (relation_1,relation_2))))>0
                ))=0:
END ENTITY:
(*
```

Attribute definitions:

network: the network structure that contains the loop.

Formal propositions:

WR1: The loop shall consist of at least one joint_logical_relationship, i.e., of at least two joints.

WR2: Every oriented_joint in a kinematic_loop shall be connected to every other oriented_joint in that kinematic loop, either directly through a single joint_logical_relationship entity, or indirectly through a number of joint_logical_relationship entities. This ensures that a kinematic_loop consists of exactly one loop.

joint_logical_relationship 5.4.74

The joint_logical_relationship is used to relate two oriented_joints that form part of a loop.

NOTE - This entity is present in an instance of a kinematics model only if the kinematic structure takes the form of a directed graph.

EXPRESS specification:

```
*)
ENTITY joint_logical_relationship;
                                   : kinematic_loop;
 previous_joint_logical_structure : oriented_joint;
 next_joint_logical_structure
                                   : oriented_joint;
UNIQUE
  UR1: loop, previous_joint_logical_structure;
  UR2: loop, next_joint_logical_structure;
WHERE
  WR1 : previous_joint_logical_structure.exit_link :=:
        next_joint_logical_structure.advent_link;
```

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```
END_ENTITY;
(*
```

Attribute definitions:

loop: the kinematic_loop of which the $previous_joint_logical_structure$ and $next_joint_logical_structure$ form components.

previous_joint_logical_structure: the first of two adjacent oriented_joints in the loop.

next_joint_logical_structure: the second of two adjacent oriented_joints in the loop.

Formal propositions:

UR1: An oriented_joint shall be used by a kinematic_loop only once in the role of previous_joint_logical_structure.

UR2: An oriented_joint shall be used by a kinematic_loop only once in the role of next_joint_logical_structure.

WR1: The exit link of the previous oriented_joint shall be the advent link of the next oriented_joint.

5.4.75 oriented_joint

The **oriented_joint** is used to indicate the direction of traversal of a joint.

NOTE – This entity is present in an instance of a kinematics model only if the kinematic structure takes the form of a directed graph.

EXPRESS specification:

Attribute definitions:

joint: the joint whose orientation is to be indicated.

orientation: the direction of traversal of a joint. If orientation is true, the joint shall be entered from the first link and left via the second link of the joint. If orientation is false, the direction of traversal shall be opposite.

advent_link: the link entering the joint. This is either the first link or the second link, depending on orientation, which is evaluated by the function assign_directed_link.

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exit_link: the link leaving the joint. This is either the second link or the first link, depending on orientation, which is evaluated by the function assign_directed_link.

5.4.76 oriented_joint_in_tree

The oriented_joint_in_tree is used to identify the kinematic_tree_structure to which the oriented_joint belongs.

NOTE – This entity is present in an instance of a kinematics model only if the kinematic structure takes the form of a directed graph.

EXPRESS specification:

```
*)
ENTITY oriented_joint_in_tree
   SUBTYPE OF (oriented_joint);
   parent_structure : kinematic_tree_structure;
END_ENTITY;
(*
```

Attribute definitions:

parent_structure: the kinematic_tree_structure of which the oriented_joint is a constituent.

5.4.77 advent_oriented_joint

An advent_oriented_joint indicates that the role of an oriented_joint is either an exit from one substructure, or an advent to the next. advent_oriented_joint distinguishes which oriented_joints are within a kinematic_substructure and which oriented_joints connect substructures.

NOTE – This entity is present in an instance of a kinematics model only if the kinematic structure takes the form of a directed graph.

EXPRESS specification:

```
*)
ENTITY advent_oriented_joint
  SUBTYPE OF (oriented_joint);
END_ENTITY;
(*
```

5.5 kinematic_structure_schema function definitions

5.5.1 ypr_index

The **ypr_index** function establishes an ordered sequence of angles of rotation for a linear transformation. The function returns 1 if the angle of rotation is of type **yaw**. The function returns 2 if the angle of rotation is of type **pitch**. The function returns 3 if the angle of rotation is of type **roll**. The type of the function is INTEGER.

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EXPRESS specification:

```
*)

FUNCTION ypr_index (ypr : ypr_enumeration): INTEGER;

CASE ypr OF

yaw : RETURN (1);

pitch : RETURN (2);

roll : RETURN (3);

END_CASE;

END_FUNCTION;

(*
```

Argument definitions:

ypr: one axis of rotation as specified by the ypr_enumeration (see 5.3.6).

5.5.2 representation_of_link

This function returns the kinematic_link_representation that is related to link via a kinematic_link_representation_relation. If there is no such relation, an indeterminate value (?) is returned.

EXPRESS specification:

Argument definitions:

link: the kinematic_link for which the related kinematic_link_representation is wanted.

5.5.3 suitably_based_mechanism

This function checks whether the base of a mechanism is related to the context of the kinematic_ground_representation which is associated with the containing_property of the mechanism. If the mechanism_base_placement identified by mbp relates the base of mech to the corresponding context, directly or indirectly, in an acyclic way, the function returns TRUE. The function returns FALSE otherwise. The type of the function is BOOLEAN.

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```
EXPRESS specification:
```

```
*)
FUNCTION suitably_based_mechanism (mbp : mechanism_base_placement;
                                   mech: mechanism): BOOLEAN;
 LOCAL
    kprop : kinematic_property_definition;
    kgrep : kinematic_ground_representation;
    klrep : kinematic_link_representation;
          : kinematic_link;
    klnk
    kjnts : BAG OF kinematic_joint;
    nmechs: BAG OF mechanism;
    nmbps : BAG OF mechanism_base_placement;
  END_LOCAL;
  kprop := mech.containing_property;
  IF ('KINEMATIC_STRUCTURE_SCHEMA.KINEMATIC_GROUND_REPRESENTATION' IN
      TYPEOF (mbp\representation_relationship.rep_1)) THEN
    kgrep := mbp\representation_relationship.rep_1;
    IF (kgrep.property_definition_representation.definition :=:
        kprop) THEN
      RETURN (TRUE);
    ELSE
      RETURN (FALSE);
    END_IF;
  ELSE
    klrep := mbp\representation_relationship.rep_1;
           := klrep.link_representation_relation.topological_aspects;
    klnk
    kjnts := USEDIN (klnk,
                'KINEMATIC_STRUCTURE_SCHEMA.KINEMATIC_JOINT.FIRST_LINK') +
              USEDIN (klnk,
                'KINEMATIC_STRUCTURE_SCHEMA.KINEMATIC_JOINT.SECOND_LINK');
    nmechs := USEDIN (kjnts[1].structure,
                'KINEMATIC_STRUCTURE_SCHEMA.MECHANISM.STRUCTURE_DEFINITION');
    IF (nmechs[1] :=: mech) THEN
      RETURN (FALSE);
    ELSE
      IF (nmechs[1].containing_property :<>: kprop) THEN
        RETURN (FALSE);
      ELSE
        nmbps := USEDIN (nmechs[1], 'KINEMATIC_STRUCTURE_SCHEMA.'+
                         'MECHANISM_BASE_PLACEMENT.BASE_OF_MECHANISM');
        IF (SIZEOF (nmbps) = 0) THEN
          RETURN (FALSE);
        ELSE
          RETURN (suitably_based_mechanism (nmbps[1], mech));
        END_IF;
      END_IF;
    END_IF;
```

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```
END_IF;
END_FUNCTION;
(*
```

Argument definitions:

mbp: the mechanism_base_placement that defines the placement of the base of mech.

mech: the mechanism whose base is being placed by mbp.

5.5.4 unique_link_usage

This function checks whether link belongs to only one mechanism. It returns TRUE if all kinematic_joints that use link as their first_link or as their second_link are in the joints set of the same kinematic_structure, and if this kinematic_structure serves as the structure_definition of precisely one mechanism. The function returns FALSE otherwise. The type of the function is BOOLEAN.

EXPRESS specification:

```
FUNCTION unique_link_usage (link : kinematic_link) : BOOLEAN;
 LOCAL
   mechs : SET OF mechanism;
    joints : SET OF kinematic_joint;
   struct : kinematic_structure;
 END_LOCAL;
  joints := bag_to_set
              (USEDIN (link,
                 'KINEMATIC_STRUCTURE_SCHEMA.KINEMATIC_JOINT.FIRST_LINK') +
               USEDIN (link,
                 'KINEMATIC_STRUCTURE_SCHEMA.KINEMATIC_JOINT.SECOND_LINK'));
 struct := joints[1].structure;
 REPEAT i := 2 TO SIZEOF (joints);
    IF (joints[i].structure :<>: struct) THEN
      RETURN (FALSE);
   END_IF;
 END_REPEAT;
 mechs := bag_to_set
             (USEDIN (struct,
                'KINEMATIC_STRUCTURE_SCHEMA.MECHANISM.STRUCTURE_DEFINITION'));
 IF (SIZEOF (mechs) <> 1) THEN
   RETURN (FALSE);
 END_IF;
 RETURN (TRUE);
END_FUNCTION;
(*
```

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Argument definitions:

link: the kinematic_link whose usage is to be checked.

5.5.5 coordinated_pair_link_representation

This function checks whether the definition of a kinematic_pair is coordinated with an existing kinematic_link_representation for a specified kinematic_link identified by link. The function returns TRUE if link is related to a kinematic_link_representation, and if pair_placement is in the items set of this kinematic_link_representation. The function returns FALSE otherwise. The type of the function is BOOLEAN.

EXPRESS specification:

```
*)
FUNCTION coordinated_pair_link_representation
    (link
                    : kinematic_link;
     pair_placement : rigid_placement) : BOOLEAN;
  LOCAL
                 : kinematic_link_representation;
    link_rep
  END_LOCAL;
  link_rep := representation_of_link (link);
  IF (link_rep = ?) THEN
    RETURN (FALSE);
    IF NOT (pair_placement IN link_rep\representation.items) THEN
      RETURN (FALSE);
    ELSE
      RETURN (TRUE);
    END_IF;
  END_IF;
END_FUNCTION;
```

Argument definitions:

link: the kinematic_link whose representation is to be coordinated with the pair definition which uses pair_placement.

pair_placement: a rigid_placement that serves as pair_placement_in_first_link_context or as pair_placement_in_second_link_context of a kinematic_pair.

5.5.6 frame_associated_to_background

The function frame_associated_to_background checks whether the kinematic_frame_background identified by background is in the items set of a kinematic_frame_background_representation. It also checks whether this kinematic_frame_background_representation is related to the kinematic_link_representation that has the rigid_placement identified by frame in its items set. This relationship is through a kinematic_frame_background_-

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representation_association, the transformation_operator of which uses frame as transformer_frame. The function returns TRUE if frame and background match these conditions; it returns FALSE otherwise. The type of the function is BOOLEAN.

EXPRESS specification:

```
*)
FUNCTION frame_associated_to_background
            : rigid_placement;
   background : kinematic_frame_background) : BOOLEAN;
  LOCAL
   rep_bag : BAG OF kinematic_frame_background_representation;
    trf_bag : BAG OF kinematic_frame_based_transformation;
    trm_bag : BAG OF kinematic_frame_based_transformation;
    ass_bag : BAG OF kinematic_frame_background_representation_association;
            : kinematic_frame_background_representation;
    ass
            : kinematic_frame_background_representation_association;
 END_LOCAL:
  rep_bag := USEDIN (background\representation_item,
                     'KINEMATIC_STRUCTURE_SCHEMA.' +
                     'KINEMATIC_FRAME_BACKGROUND_REPRESENTATION\' +
                     'REPRESENTATION.ITEMS');
  IF SIZEOF (rep_bag) = 0 THEN
   RETURN (FALSE);
 END_IF;
  trf_bag := USEDIN (frame,
                     'KINEMATIC_STRUCTURE_SCHEMA.' +
                     'KINEMATIC_FRAME_BASED_TRANSFORMATION.' +
                     'TRANSFORMER_FRAME');
  IF SIZEOF (trf_bag) = 0 THEN
   RETURN (FALSE);
  END_IF;
  REPEAT i := 1 TO HIINDEX (rep_bag);
   rep := rep_bag[i];
    ass_bag := USEDIN (rep\representation,
                'KINEMATIC_STRUCTURE_SCHEMA.' +
                'KINEMATIC_FRAME_BACKGROUND_REPRESENTATION_ASSOCIATION\' +
                'REPRESENTATION_RELATIONSHIP_WITH_TRANSFORMATION\' +
                'REPRESENTATION_RELATIONSHIP.REP_2');
    IF SIZEOF (ass_bag) > 0 THEN
      REPEAT j:= 1 TO HIINDEX (ass_bag);
        ass := ass_bag[j];
        trm_bag := QUERY (trm <* trf_bag |</pre>
          (trm\functionally_defined_transformation :=:
           ass\representation_relationship_with_transformation.
```

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Argument definitions:

frame: a rigid_placement which is checked for its role as the transformer_frame in the relationship between the kinematic_link_representation which contains frame in its items set and the kinematic_frame_background_representation the items set of which contains background.

background: the kinematic_frame_background which is checked whether it is in the items set of a kinematic_frame_background_representation which is related to the kinematic_link_representation of frame, using frame as the transformer_frame.

5.5.7 plane_angle_for_pair_in_radian

The function plane_angle_for_pair_in_radian converts the specified angle to an equivalent plane_angle_measure whose unit is radian. The conversion factor is evaluated from the plane_angle_unit in the units set of a global_unit_assigned_context which is the context_of_items of the first_link of the joint of the specified pair. The type of the function is plane_angle_measure. If the appropriate units are found, the function returns the converted plane_angle_measure; the function returns an indeterminate value (?) otherwise.

EXPRESS specification:

```
*)
FUNCTION plane_angle_for_pair_in_radian
         (pair : kinematic_pair;
          angle : plane_angle_measure) : plane_angle_measure;
  LOCAL
    converted_angle : plane_angle_measure := angle;
                    : kinematic_link_representation
    link_rep
                    := representation_of_link (pair.joint.first_link);
    link_cntxt
                   : representation_context;
    pa_units
                   : SET OF unit := [];
    pau
                    : unit;
  END_LOCAL;
  link_cntxt := link_rep\representation.context_of_items;
```

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```
IF NOT ('MEASURE_SCHEMA.GLOBAL_UNIT_ASSIGNED_CONTEXT'
        IN TYPEOF (link_cntxt)) THEN
  RETURN (?);
END_IF;
pa_units := QUERY (unit <* link_cntxt\global_unit_assigned_context.units |</pre>
                   'MEASURE_SCHEMA.PLANE_ANGLE_UNIT' IN TYPEOF (unit));
IF SIZEOF (pa_units) <> 1 THEN
  RETURN (?);
END_IF;
pau := pa_units[1];
IF (NOT ('MEASURE_SCHEMA.SI_UNIT' IN TYPEOF (pau)) AND
    NOT ('MEASURE_SCHEMA.CONVERSION_BASED_UNIT' IN TYPEOF (pau))) THEN
  RETURN (?);
END_IF;
REPEAT WHILE ('MEASURE_SCHEMA.CONVERSION_BASED_UNIT' IN TYPEOF (pau));
  converted_angle := converted_angle *
                     pau\conversion_based_unit.conversion_factor.
                     value_component;
  pau := pau\conversion_based_unit.conversion_factor.unit_component;
  IF ((NOT ('MEASURE_SCHEMA.SI_UNIT' IN TYPEOF (pau)) AND
       NOT ('MEASURE_SCHEMA.CONVERSION_BASED_UNIT' IN TYPEOF (pau))) OR
      (NOT ('MEASURE_SCHEMA.PLANE_ANGLE_UNIT' IN TYPEOF (pau)))) THEN
    RETURN (?);
  END_IF;
END_REPEAT;
IF (pau\si_unit.name <> si_unit_name.radian) THEN
  RETURN (?);
END_IF;
CASE pau\si_unit.prefix OF
  si_prefix.exa : RETURN (1.E18 * converted_angle);
  si_prefix.peta : RETURN (1.E15 * converted_angle);
  si_prefix.tera : RETURN (1.E12 * converted_angle);
  si_prefix.giga : RETURN (1.E9 * converted_angle);
  si_prefix.mega : RETURN (1.E6 * converted_angle);
  si_prefix.kilo : RETURN (1.E3 * converted_angle);
  si_prefix.hecto : RETURN (1.E2 * converted_angle);
  si_prefix.deca : RETURN (1.E1 * converted_angle);
si_prefix.deci : RETURN (1.E-1 * converted_angle);
  si_prefix.centi : RETURN (1.E-2 * converted_angle);
  si_prefix.milli : RETURN (1.E-3 * converted_angle);
  si_prefix.micro : RETURN (1.E-6 * converted_angle);
  si_prefix.nano : RETURN (1.E-9 * converted_angle);
  si_prefix.pico : RETURN (1.E-12 * converted_angle);
   si_prefix.femto : RETURN (1.E-15 * converted_angle);
```

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```
si_prefix.atto : RETURN (1.E-18 * converted_angle);
OTHERWISE : RETURN (converted_angle);
END_CASE;
END_FUNCTION;
(*
```

Argument definitions:

pair: the kinematic_pair the context of whose pair_placement_in_first_link_context is to be evaluated for the conversion factor.

angle: the angle that is converted to an angle in radians.

5.5.8 convert_plane_angle_for_pair_from_radian

The function convert_plane_angle_for_pair_from_radian converts an angle expression, specified as angle_expr, the angle unit of which is radian, to an equivalent plane_angle_measure with a unit as specified in the respective context. The conversion factor is evaluated from the plane_angle_unit in the units set of a global_unit_assigned_context which is the context_of_items of the first_link of the joint of the specified pair. The type of the function is plane_angle_measure. If the appropriate units are found, the function returns the converted plane_angle_measure; the function returns an indeterminate value (?) otherwise.

EXPRESS specification:

```
*)
FUNCTION convert_plane_angle_for_pair_from_radian
                    : kinematic_pair;
          angle_expr : REAL) : plane_angle_measure;
  LOCAL
                : kinematic_link_representation
    link_rep
                := representation_of_link (pair.joint.first_link);
    link_cntxt : representation_context;
    pa_units : SET OF unit := [];
               : unit;
   pau
    conv_factor : REAL := 1.0;
                : plane_angle_measure;
    result
  END_LOCAL;
  link_cntxt := link_rep\representation.context_of_items;
  IF NOT ('MEASURE_SCHEMA.GLOBAL_UNIT_ASSIGNED_CONTEXT'
          IN TYPEOF (link_cntxt)) THEN
    RETURN (?);
  END_IF;
  pa_units := QUERY (unit <* link_cntxt\global_unit_assigned_context.units |</pre>
                     'MEASURE_SCHEMA.PLANE_ANGLE_UNIT' IN TYPEOF (unit));
  IF SIZEOF (pa_units) <> 1 THEN
    RETURN (?);
```

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```
END_IF;
  pau := pa_units[1];
  IF (NOT ('MEASURE_SCHEMA.SI_UNIT' IN TYPEOF (pau)) AND
      NOT ('MEASURE_SCHEMA.CONVERSION_BASED_UNIT' IN TYPEOF (pau))) THEN
    RETURN (?):
  END_IF;
  REPEAT WHILE ('MEASURE_SCHEMA.CONVERSION_BASED_UNIT' IN TYPEOF (pau));
    conv_factor := conv_factor *
                      pau\conversion_based_unit.conversion_factor.
                      value_component;
    pau := pau\conversion_based_unit.conversion_factor.unit_component;
    IF ((NOT ('MEASURE_SCHEMA.SI_UNIT' IN TYPEOF (pau)) AND
          NOT ('MEASURE_SCHEMA.CONVERSION_BASED_UNIT' IN TYPEOF (pau))) OR
         (NOT ('MEASURE_SCHEMA.PLANE_ANGLE_UNIT' IN TYPEOF (pau)))) THEN
      RETURN (?);
    END_IF:
  END_REPEAT;
  IF (pau\si_unit.name <> si_unit_name.radian) THEN
    RETURN (?);
  END_IF;
  CASE pau\si_unit.prefix OF
    si_prefix.exa : conv_factor := 1.E18 * conv_factor;
    si_prefix.peta : conv_factor := 1.E15 * conv_factor;
    si_prefix.tera : conv_factor := 1.E12 * conv_factor;
si_prefix.giga : conv_factor := 1.E9 * conv_factor;
si_prefix.mega : conv_factor := 1.E6 * conv_factor;
si_prefix.kilo : conv_factor := 1.E3 * conv_factor;
    si_prefix.hecto : conv_factor := 1.E2 * conv_factor;
    si_prefix.deca : conv_factor := 1.E1 * conv_factor;
    si_prefix.deci
                        : conv_factor := 1.E-1 * conv_factor;
    si_prefix.centi : conv_factor := 1.E-2 * conv_factor;
    si_prefix.milli : conv_factor := 1.E-3 * conv_factor;
    si_prefix.micro : conv_factor := 1.E-6 * conv_factor;
    si_prefix.nano : conv_factor := 1.E-9 * conv_factor;
si_prefix.pico : conv_factor := 1.E-12 * conv_factor;
si_prefix.femto : conv_factor := 1.E-15 * conv_factor;
    si_prefix.atto : conv_factor := 1.E-18 * conv_factor;
  OTHERWISE
                         : ;
  END_CASE;
  result := angle_expr / conv_factor;
  RETURN (result);
END_FUNCTION;
(*
```

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Argument definitions:

pair: the kinematic_pair the context of whose pair_placement_in_first_link_context is to be evaluated for the conversion factor.

angle_expr: the angle expression in radian that is converted to an angle with the unit which is required in the context of pair.

5.5.9 convert_spatial_to_ypr_rotation

The function convert_spatial_to_ypr_rotation converts the specified rotation, which is either a ypr_rotation or a rotation_about_direction, to its equivalent representation as a ypr_rotation. The units for the yaw, pitch, and roll angles of the ypr_rotation are evaluated from the plane_angle_unit in the units set of a global_unit_assigned_context which is the context_of_items of the first_link of the joint of the specified pair. This evaluation is done by a call to the function plane_angle_for_pair_in_radian.

If rotation is already of type ypr_rotation, it is returned immediately. Otherwise, convert_spatial_to_ypr_rotation returns either a ypr_rotation that is equivalent to the rotation_about_direction which has been used as the rotation argument, or an indeterminate value (?), if the unit evaluation has not been successful. The type of the function is ypr_rotation.

EXPRESS specification:

```
FUNCTION convert_spatial_to_ypr_rotation (pair
                                                   : kinematic_pair;
                                          rotation : spatial_rotation)
                                                   : ypr_rotation;
  LOCAL
    axis
               : direction;
              : plane_angle_measure; -- rotation angle in application
    angle
                                       -- specific units
    conv_angle : plane_angle_measure;
                                       -- rotation angle in radians
    ya, pa, ra : plane_angle_measure;
                                       -- yaw, pitch, and roll angle
            : REAL;
                                        -- unit conversion factor
    ucf
    dx, dy, dz : REAL;
                                        -- components of direction vector
    s_a, c_a : REAL;
                                        -- sine and cosine of rotation angle
              : ARRAY [1 : 3] OF
    rotmat
                ARRAY [1:3] OF REAL; -- rotation matrix
              : REAL;
    cm1
              : REAL;
    s_y, c_y
    s_r, c_r
              : REAL;
  END_LOCAL;
  -- If rotation is already a ypr_rotation, return it immediately
  IF 'KINEMATIC_STRUCTURE_SCHEMA.YPR_ROTATION' IN TYPEOF (rotation) THEN
    RETURN (rotation);
  END_IF;
  -- rotation is a rotation_about_direction
  axis := normalise (rotation\rotation_about_direction.direction_of_axis);
```

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```
angle := rotation\rotation_about_direction.rotation_angle;
-- a zero rotation is converted trivially
IF (angle = 0.0) THEN
 RETURN ([0.0, 0.0, 0.0]);
END_IF;
dx := axis.direction_ratios[1];
dy := axis.direction_ratios[2];
dz := axis.direction_ratios[3];
-- provide angle measured in radian
conv_angle := plane_angle_for_pair_in_radian (pair, angle);
IF (conv_angle = ?) THEN
 RETURN (?);
END_IF;
ucf := angle / conv_angle;
s_a := SIN (conv_angle);
c_a := COS (conv_angle);
-- axis parallel either to x-axis or to z-axis?
IF (dy = 0.0) AND (dx * dz = 0.0) THEN
  REPEAT WHILE (conv_angle <= - PI);</pre>
    conv_angle := conv_angle + 2.0 * PI;
  END_REPEAT;
  REPEAT WHILE (conv_angle > PI);
    conv_angle := conv_angle - 2.0 * PI;
  END_REPEAT;
  ya := ucf * conv_angle;
  IF (conv_angle <> PI) THEN
   ra := - ya;
  ELSE
   ra := ya;
  END_IF;
  IF (dx <> 0.0) THEN
    -- axis parallel to x-axis - use x-axis as roll axis
    IF (dx > 0.0) THEN
      RETURN ([0.0, 0.0, ya]);
      RETURN ([0.0, 0.0, ra]);
    END_IF;
  ELSE
    -- axis parallel to z-axis - use z-axis as yaw axis
    IF (dz > 0.0) THEN
      RETURN ([ya, 0.0, 0.0]);
    ELSE
      RETURN ([ra, 0.0, 0.0]);
```

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```
END_IF;
  END_IF;
END_IF;
-- axis parallel to y-axis - use y-axis as pitch axis
IF ((dy <> 0.0) \text{ AND } (dx = 0.0) \text{ AND } (dz = 0.0)) \text{ THEN}
  IF (c_a \ge 0.0) THEN
    ya := 0.0;
    ra := 0.0;
  ELSE
    ya := ucf * PI;
    ra := ya;
  END_IF;
  pa := ucf * ATAN (s_a, ABS (c_a));
  IF (dy < 0.0) THEN
    pa := ~ pa;
  END_IF;
  RETURN ([ya, pa, ra]);
END_IF;
-- axis not parallel to any axis of coordinate system
-- compute rotation matrix
cm1 := 1.0 - c_a;
rotmat := [ [ dx * dx * cm1 + c_a,
               dx * dy * cm1 - dz * s_a
               dx * dz * cm1 + dy * s_a],
             [ dx * dy * cm1 + dz * s_a,
               dy * dy * cm1 + c_a
               dy * dz * cm1 - dx * s_a],
             [ dx * dz * cm1 - dy * s_a,
               dy * dz * cm1 + dx * s_a,
               dz * dz * cm1 + c_a ] ];
-- rotmat[1][3] equals SIN (pitch_angle)
IF (ABS (rotmat[1][3]) = 1.0) THEN
  -- |pa| = PI/2
  BEGIN
     IF (rotmat[1][3] = 1.0) THEN
      pa := 0.5 * PI;
    ELSE
      pa := -0.5 * PI;
    END_IF;
     -- In this case, only the sum or difference of roll and yaw angles
     -- is relevant and can be evaluated from the matrix.
     -- According to IP 'rectangular pitch angle' for ypr_rotation,
     -- the roll angle is set to zero.
```

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```
ra := 0.0;
    ya := ATAN (rotmat[2][1], rotmat[2][2]);
    -- result of ATAN is in the range [-PI/2, PI/2].
    -- Here all four quadrants are needed.
    IF (rotmat[2][2] < 0.0) THEN
      IF ya <= 0.0 THEN
        ya := ya + PI;
      ELSE
        ya := ya - PI;
      END_IF;
    END_IF;
  END:
ELSE
  -- COS (pitch_angle) not equal to zero
    ya := ATAN (- rotmat[1][2], rotmat[1][1]);
    IF (rotmat[1][1] < 0.0) THEN
      IF (ya <= 0.0) THEN
        ya := ya + PI;
      ELSE
        ya := ya - PI;
      END_IF;
   END_IF;
   ra := ATAN (-rotmat[2][3], rotmat[3][3]);
   IF (rotmat[3][3] < 0.0) THEN
      IF (ra <= 0.0) THEN
       ra := ra + PI;
     ELSE
       ra := ra - PI;
     END_IF;
   END_IF;
   s_y := SIN (ya);
   c_y := COS(ya);
   s_r := SIN (ra);
   c_r := COS (ra);
   IF ((ABS (s_y) > ABS (c_y)) AND
       (ABS (s_y) > ABS (s_r)) AND
       (ABS (s_y) > ABS (c_r)) THEN
     cm1 := - rotmat[1][2] / s_y;
   ELSE
     IF ((ABS (c_y) > ABS (s_r)) AND (ABS (c_y) > ABS (c_r))) THEN
       cm1 := rotmat[1][1] / c_y;
     ELSE
       IF (ABS (s_r) > ABS (c_r)) THEN
         cm1 := - rotmat[2][3] / s_r;
```

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Argument definitions:

pair: the kinematic_pair the context of whose pair_placement_in_first_link_context is to be evaluated with regard to the plane_angle_unit.

rotation: the spatial_rotation that is to be converted by the function.

5.5.10 assign_directed_link

The function assign_directed_link checks the orientation of a kinematic_joint. This function returns joint.first_link, if orientation is true and joint.second_link otherwise. The type of the function is kinematic_link.

EXPRESS specification:

```
*)
FUNCTION assign_directed_link
  (joint : kinematic_joint; orientation : BOOLEAN ) : kinematic_link;
  IF (orientation) THEN
        RETURN (joint.first_link);
  ELSE
        RETURN (joint.second_link);
  END_IF;
END_FUNCTION;
(*
```

Argument definitions:

joint: a kinematic_joint for which the kinematic_link is determined.

orientation: a boolean indicating the direction of traversal of a joint.

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5.5.11 connected_in_simple_loop

This function checks if two given joint_logical_relationships are related to the same loop, and if the orientation of the oriented_joints which they relate is consistent. The function returns TRUE if relation_1 and relation_2 match these conditions. The function returns FALSE otherwise. The type of the function is BOOLEAN.

EXPRESS specification:

```
*)
FUNCTION connected_in_simple_loop( relation_1 : joint_logical_relationship;
                                   relation_2 : joint_logical_relationship)
  : BOOLEAN;
  LOCAL
   next_jlr_in_loop_set : SET [1:?] OF joint_logical_relationship;
  IF ((relation_1.loop:<>: relation_2.loop) OR
       (relation_1 :=: relation_2)) THEN
          RETURN (FALSE);
  ELSE
    IF (relation_1.next_joint_logical_structure :=:
        relation_2.previous_joint_logical_structure) THEN
       RETURN (TRUE);
   ELSE
      next_jlr_in_loop_set :=
          QUERY (relation <* USEDIN (relation_1.next_joint_logical_structure,
          'kinematic_structure_schema.joint_logical_relationship.' +
          'previous_joint_logical_structure')
           | relation.loop :=: relation_1.loop);
      IF (SIZEOF(next_jlr_in_loop_set) <> 1) THEN
          RETURN (FALSE);
      ELSE
          RETURN (connected_in_simple_loop(next_jlr_in_loop_set [1],
                  relation_2));
      END_IF;
    END_IF;
  END_IF;
END_FUNCTION;
```

Argument definitions:

relation_1: a joint_logical_structure_relationship which is checked whether it is connected with relation_2.

relation_2: the second joint_logical_structure_relationship which is checked whether it is connected with relation_1.

```
*)
END_SCHEMA; -- end kinematic_structure_schema
(*
```

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6 Kinematic motion representation

The following EXPRESS declaration begins the kinematic_motion_representation_schema and identifies the necessary external references.

EXPRESS specification:

```
*)
SCHEMA kinematic_motion_representation_schema;
REFERENCE FROM geometry_schema
    (cartesian_point,
     curve):
REFERENCE FROM measure_schema
    (length_measure,
     measure_with_unit,
     parameter_value,
     plane_angle_measure);
REFERENCE FROM representation_schema
    (functionally_defined_transformation,
     representation_item);
REFERENCE FROM kinematic_structure_schema
    (rotation_about_direction,
     spatial_rotation,
     ypr_rotation);
    NOTES
```

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1 - The schemas referenced above can be found in the following parts of ISO 10303:

kinematic_structure_schema Clause 5 of this part of ISO 10303 geometry_schema ISO 10303-42 measure_schema ISO 10303-41

representation_schema ISO 10303-43

2 - See annex D for a graphical representation of this schema using the EXPRESS-G notation.

6.1 Introduction

The subject of the kinematic_motion_representation_schema is the description of motion. It specifies different types of paths that comprise the motion for a kinematic model.

6.2 Fundamental concepts and assumptions

Motion in this part of ISO 10303 is defined in terms of a parameter t. t is a non-decreasing parameter as motion progresses. Several motions may be synchronised by the requirement that

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the actual state of all motion in a kinematic model is controlled by a single parameter t which appears as an attribute in the kinematic_control and in the kinematic_result.

6.3 kinematic_motion_representation_schema type definition: motion_parameter_measure

The motion_parameter_measure is a mechanism by which different poses in the course of a motion are distinguished. The motion parameter may be defined with or without units.

NOTE - To introduce time aspects, the motion parameter may be defined with time units.

EXPRESS specification:

```
*)
TYPE motion_parameter_measure = SELECT
  (parameter_value,
  measure_with_unit);
END_TYPE;
```

kinematic_motion_representation_schema entity definitions

translation 6.4.1

A translation specifies a displacement in Cartesian coordinate space R^3 .

EXPRESS specification:

```
*)
ENTITY translation;
  x : length_measure;
  y : length_measure;
  z : length_measure;
END_ENTITY;
```

Attribute definitions:

x: displacement in x-direction.

y: displacement in y-direction.

z: displacement in z-direction.

transform 6.4.2

A transform specifies a linear transformation of a frame along a path, composed of a rotation and a translation. First the rotation shall be performed and then the translation.

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EXPRESS specification:

```
*)
ENTITY transform
SUBTYPE OF (functionally_defined_transformation);
rotation_component : spatial_rotation;
translation_component : translation;
END_ENTITY;
(*
```

Attribute definitions:

rotation_component: the rotational part of the transform.

translation_component: the displacement part of the transform.

6.4.3 path_node

A path_node describes a constituent of a path definition. It consists of a linear transformation and its associated motion parameter.

EXPRESS specification:

```
*)
ENTITY path_node;
  control_transform : transform;
  t_parameter : motion_parameter_measure;
END_ENTITY;
(*
```

Attribute definitions:

control_transform: a linear transformation that specifies a local frame on a path.

t_parameter: the parameter t of a path which corresponds to the control transform.

6.4.4 kinematic_path

A kinematic_path describes a path or a segment of a path along which motion is to take place.

EXPRESS specification:

```
*)
ENTITY kinematic_path
SUPERTYPE OF (ONEOF (path_element, composite_path))
SUBTYPE OF (representation_item);
END_ENTITY;
(*
```

6.4.5 path_element_connection

A path_element_connection is the connection of two adjacent path_elements. The parameter t at the end of the previous path_element is the same as the parameter t at the start of the next path_element.

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EXPRESS specification:

Attribute definitions:

previous_element: the first element in a sequence of two path_elements.

next_element: the second element in a sequence of two path_elements.

Formal propositions:

WR1: The path_node at the end of the previous path_element shall be identical with the path_node at the start of the next path_element.

WR2: The unit_components of the parameter values of the two path_elements shall be identical.

6.4.6 composite_path

A composite_path is a collection of path_elements joined end to end. The composite_path has its own t parameter range; the path_elements are re-parametrised in such a way that the sum of the lengths of their individual t parameter ranges fits the length of the parameter range of the composite_path, and the ratio between the lengths of the individual parameter ranges remains unchanged.

EXPRESS specification:

```
*)
ENTITY composite_path

SUBTYPE OF (kinematic_path);
elements: SET [1:?] OF path_element_connection;
t_start: motion_parameter_measure;
t_end: motion_parameter_measure;
WHERE

WR1: increasing_measure_value (t_start, t_end);
WR2: compare_unit_components (t_start, t_end);
WR3: connected_in_simple_path (elements);
END_ENTITY;
(*
```

Attribute definitions:

elements: the path_element_connections that define the path_elements, their sequence and connectivity.

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t_start: the parameter value at the start of the composite_path.

 $t_end:$ the parameter value at the end of the $composite_path$.

Formal propositions:

WR1: The parameters shall be increasing.

WR2: The unit_components of the parameter values at the start and end of a composite_path shall be identical.

WR3: Every path_element in a composite_path shall be connected to every other path_element in that composite_path, either directly through a single path_element_connection, or indirectly through a number of path_element_connections, in such a way that the path_elements form a single open coherent chain without gaps or branches. This is checked by the function connected_in_simple_path.

6.4.7 path_element

A path_element is a kinematic_path that describes either a point-to-point, a linear, a circular, or a general curve-based type of motion.

EXPRESS specification:

```
*)
ENTITY path_element
 SUPERTYPE OF (ONEOF (point_to_point_path,
                       circular_path,
                       linear_path,
                       curve_based_path))
 SUBTYPE OF (kinematic_path);
 node_from : path_node;
 node_to
          : path_node;
WHERE
  WR1: compare_unit_components (node_from.t_parameter,
                                node_to.t_parameter);
 WR2: increasing_measure_value (node_from.t_parameter,
                                 node_to.t_parameter);
END_ENTITY;
```

Attribute definitions:

node_from: the frame where the path_element starts.

node_to: the frame where the path_element ends.

Formal propositions:

WR1: The unit_components of the parameter values of the two path_nodes shall be identical.

WR2: The parameter t shall be increasing from the beginning to the end of the path_element.

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6.4.8 point_to_point_path

A point_to_point_path defines the frames which are to be traversed. It does not have a prescribed interpolation.

NOTE - The interpolation is left to the software that uses the data.

EXPRESS specification:

```
*)
ENTITY point_to_point_path
   SUBTYPE OF (path_element);
END_ENTITY;
(*
```

6.4.9 circular_path

A circular_path describes a portion of a complete kinematic_path such that the interpolation rule gives a circle for the translational part of the motion of the origin of the frame of the kinematic_link. The interpolation for the orientation is performed in synchronous fashion with the interpolation of translation.

EXPRESS specification:

Attribute definitions:

via_point: an intermediate point through which the circular_path passes.

Formal propositions:

WR1: The endpoint of a circular_path shall not coincide with its startpoint.

WR2: the via_point of a circular_path shall not coincide with either its startpoint or its endpoint.

6.4.10 linear_path

A linear_path is an arcwise connected bounded linear path element defined by the two transforms of the path_nodes at the beginning and the end of the path element. transforms

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between the values of the motion parameters given in these **path_node**s are obtained by linear interpolation between the **transforms** specified in **node_from** and **node_to** of the **linear_path**.

EXPRESS specification:

```
*)
ENTITY linear_path
  SUBTYPE OF (path_element);
END_ENTITY;
(*
```

6.4.11 curve_based_path

A curve_based_path describes a portion of a complete kinematic_path such that the interpolation rule follows a curve for the translational part of the motion of the origin of the frame of the kinematic_link. The interpolation for the orientation is performed in synchronous fashion with the interpolation of translation.

EXPRESS specification:

```
*)
ENTITY curve_based_path
   SUBTYPE OF (path_element);
   path_curve : curve;
WHERE
   WR1: SELF\path_element.node_to.control_transform.translation_component <>
        SELF\path_element.node_from.control_transform.translation_component;
END_ENTITY;
(*
```

Attribute definitions:

path_curve: the curve which defines the translational interpolation between the path_nodes that are connected by the curve_based_path.

Formal propositions:

WR1: The endpoint of a curve_based_path shall not coincide with its startpoint.

Informal propositions:

startpoint on curve: The startpoint of a curve_based_path shall lie on the curve which is referenced as path_curve.

endpoint on curve: The endpoint of a curve_based_path shall lie on the curve which is referenced as path_curve.

6.5 kinematic_motion_representation_schema function definitions

6.5.1 connected_in_simple_path

The connected_in_simple_path function checks whether a composite_path is simply connected. The function returns TRUE if the connections connect all the path_elements of

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the path in such a way that they form an open (i.e., acyclic) coherent chain without gaps or branches. The function returns FALSE otherwise. The type of the function is BOOLEAN.

EXPRESS specification:

```
*)
FUNCTION connected in simple path (connections : SET OF path element connection)
                                                 : BOOLEAN:
 LOCAL
     connection_set : SET [0 : ?] OF path_element_connection;
             : INTEGER;
                   : INTEGER;
     pec0
    necbranch : INTEGER;
pecbranch : INTEGER;
  END_LOCAL;
  IF SIZEOF (connections) > 1 THEN
    connection_set := QUERY (pec1 <* connections |</pre>
                         SIZEOF (QUERY (pec2 <* connections - pec1 |
                           pec1.next_element :=: pec2.previous_element)) = 0);
    nec0 := SIZEOF (connection_set);
    connection_set := QUERY (pec1 <* connections |</pre>
                         SIZEOF (QUERY (pec2 <* connections - pec1 |
                           pec2.next_element :=: pec1.previous_element)) = 0);
    pec0 := SIZEOF (connection_set);
    connection_set := QUERY (pec1 <* connections |</pre>
                         SIZEOF (QUERY (pec2 <* connections - pec1 |
                           pec1.next_element :=: pec2.previous_element)) > 1);
    necbranch := SIZEOF (connection_set);
    connection_set := QUERY (pec1 <* connections |</pre>
                         SIZEOF (QUERY (pec2 <* connections - pec1 |
                           pec2.next_element :=: pec1.previous_element)) > 1);
    pecbranch := SIZEOF (connection_set);
    IF ((nec0 <> 1) OR (pec0 <> 1) OR (necbranch > 0) OR (pecbranch > 0)) THEN
      RETURN (FALSE);
    ELSE
      RETURN (TRUE);
    END_IF;
  ELSE
    RETURN (TRUE);
  END_IF;
END_FUNCTION;
```

Argument definitions:

connections: the set of path_element_connections which has to be checked.

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6.5.2 compare_unit_components

The compare_unit_components function checks the units of two given path parameters of the type motion_parameter_measure. The function returns TRUE if the units are identical. The function returns FALSE if the units are different. The type of the function is BOOLEAN.

EXPRESS specification:

```
*)
FUNCTION compare_unit_components (parm1 : motion_parameter_measure;
                                  parm2 : motion_parameter_measure) : BOOLEAN;
   IF (('MEASURE_SCHEMA.PARAMETER_VALUE' IN TYPEOF (parm1)) AND
       ('MEASURE_SCHEMA.PARAMETER_VALUE' IN TYPEOF (parm2))) THEN
         RETURN (TRUE);
   ELSE
     IF (('MEASURE_SCHEMA.MEASURE_WITH_UNIT' IN TYPEOF (parm1)) AND
         ('MEASURE_SCHEMA.MEASURE_WITH_UNIT' IN TYPEOF (parm2))) THEN
        IF (parm1.unit_component = parm2.unit_component) THEN
            RETURN (TRUE);
        ELSE
            RETURN (FALSE):
        END_IF;
     ELSE
       RETURN (FALSE);
     END_IF;
  END_IF;
END_FUNCTION;
```

Argument definitions:

parm1: the first path parameter which is checked for identical units with the second path parameter.

parm2: the second path parameter which is checked for identical units with the first path parameter.

6.5.3 increasing_measure_value

The increasing_measure_value function compares the values of two given path parameters of the type motion_parameter_measure. The function returns TRUE if the value of the first parameter is less than the value of the second parameter. The function returns FALSE if the value of the second parameter is less than or equal to the value of the first parameter. The type of the function is BOOLEAN. This function assumes that both parameters are either parameter_values or given in the same units.

EXPRESS specification:

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```
RETURN (TRUE);
   ELSE
      RETURN (FALSE);
   END_IF;
 ELSE
    IF ('MEASURE_SCHEMA.MEASURE_WITH_UNIT' IN TYPEOF (parm1)) THEN
      IF (parm1.value_component < parm2.value_component) THEN</pre>
        RETURN (TRUE);
      ELSE
        RETURN (FALSE);
      END_IF;
   ELSE
      RETURN (FALSE);
   END_IF;
 END_IF;
END_FUNCTION;
(*
```

Argument definitions:

parm1: the first path parameter whose value is compared with the value of the second path parameter.

parm2: the second path parameter whose value is compared with the value of the first path parameter.

6.5.4 non_coincident_coordinates

This function checks whether a given **translation** coincides with a given **cartesian_point** or not. It returns TRUE if **trltn** does not coincide with **crtpt**. It returns FALSE otherwise. The type of the function is BOOLEAN.

EXPRESS specification:

Argument definitions:

crtpt: the cartesian_point whose non-coincidence with trltn has to be checked.

trltn: the translation whose non-coincidence with crtpt has to be checked.

```
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```

```
*)
END_SCHEMA; -- end kinematic_motion_representation_schema
(*
```

7 Kinematic analysis control and result

The following EXPRESS declaration begins the kinematic_analysis_control_and_result_schema and identifies the necessary external references.

EXPRESS specification:

```
*)
SCHEMA kinematic_analysis_control_and_result_schema;
REFERENCE FROM kinematic_motion_representation_schema
    (kinematic_path,
     motion_parameter_measure);
REFERENCE FROM kinematic_structure_schema
    (kinematic_joint,
     kinematic_link_representation,
     mechanism,
     pair_value,
     rigid_placement);
{\tt REFERENCE} \  \, {\tt FROM} \  \, {\tt geometry\_schema}
     (geometric_representation_context);
REFERENCE FROM representation_schema
     (representation,
     representation_relationship);
(*
     NOTES
```

1 - The schemas referenced above can be found in the following parts of ISO 10303:

kinematic_motion_representation_schema Clause 6 of this part of ISO 10303 kinematic_structure_schema Clause 5 of this part of ISO 10303 geometry_schema ISO 10303-42 representation_schema ISO 10303-43

2 - See annex D for a graphical representation of this schema using the EXPRESS-G notation.

7.1 Introduction

The subject of the kinematic_analysis_control_and_result_schema is the identification and analysis of configurations of kinematic_structures and the interpolation between configurations. The schema covers the prescribed paths and the paths resulting from analysis.

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7.2 Fundamental concepts and assumptions

A kinematic analysis is a specific presentation of the kinematic behaviour of a mechanical product. There are two possible ways to check the kinematic behaviour of a kinematic structure:

- forward analysis;
- backward analysis.

The forward analysis specifies the motion of a kinematic structure in terms of a sequence of configurations and of the interpolations between them. The result of a forward analysis is the path of specified frames on specified links.

The backward analysis specifies the motion of a kinematic structure with a prescribed path defined by frames. The result of a backward analysis is the sequence of configuration definitions in the form of the pair parameter values for a sufficiently large number of pairs to control the motion.

A configuration of a kinematic structure is defined by the specification of pair values for a set of pairs of the kinematic structure.

7.3 kinematic_analysis_control_and_result_schema type definitions

7.3.1 interpolation_type

The interpolation_type describes the method of interpolation between two configuration definitions of a kinematic structure.

EXPRESS specification:

```
*)
TYPE interpolation_type = ENUMERATION OF
  (undefined,
   synchronous,
   linear);
END_TYPE;
(*
```

Enumerated item definitions:

undefined: an interpolation in which all pair parameters shall match the set of pair parameter values defined in the next configuration definition.

synchronous: an interpolation in which all pair parameters are interpolated such that the pair parameters pass from one value to the next one at the same rate. The rate may vary proportionally among the pairs.

linear: an interpolation in which all pair parameters are interpolated such that the pair parameters pass from one value to the next one at the same rate. The rate remains constant.

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7.3.2 kinematic_analysis_definition

A kinematic_analysis_definition allows a reference to either an interpolated_configuration_sequence or a prescribed_path. With an interpolated_configuration_sequence, motion is specified in terms of the pair parameters of a kinematic_structure. With a prescribed_path, motion is specified in Cartesian space.

EXPRESS specification:

```
*)
TYPE kinematic_analysis_definition = SELECT
  (interpolated_configuration_sequence,
   prescribed_path);
END_TYPE;
```

kinematic result 7.3.3

A kinematic_result allows a reference to either an interpolated_configuration_sequence or a resulting_path. With an interpolated_configuration_sequence, motion is specified in terms of the pair parameters of a kinematic_structure, where all the interpolations between the configuration definitions in the sequence are undefined. With a resulting_path, motion is specified in Cartesian space.

EXPRESS specification:

```
*)
TYPE kinematic_result = SELECT
  (interpolated_configuration_sequence,
   resulting_path);
END_TYPE;
(*
```

kinematic_analysis_control_and_result_schema entity definitions

configuration_interpolation

The configuration_interpolation specifies the interpolation of the configurations between two configuration definitions.

EXPRESS specification:

```
*)
ENTITY configuration_interpolation;
 previous_configuration_definition : configuration_definition;
 next_configuration_definition
                                    : configuration_definition;
  interpolation
                                    : interpolation_type;
END_ENTITY ;
(*
```

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Attribute definitions:

previous_configuration_definition: the configuration_definition from which the interpolation starts.

next_configuration_definition: the configuration_definition at which the interpolation finishes.

interpolation: the type of interpolation from the previous configuration definition to the next.

kinematic_control 7.4.2

The kinematic_control identifies the control information necessary for a forward or a backward analysis of a mechanism. The prescribed_path is used for the backward analysis and the interpolated_configuration_sequence is used for the forward analysis.

EXPRESS specification:

```
*)
ENTITY kinematic_control;
  controlled_mechanism
                               : mechanism;
  contained_kinematic_programs : SET [1 : ?] OF kinematic_analysis_definition;
END_ENTITY;
(*
```

Attribute definitions:

controlled_mechanism: the mechanism to which the control information applies.

contained_kinematic_programs: a set of motion definitions.

7.4.3 founded_kinematic_path

A founded_kinematic_path specifies the geometric founding of a kinematic_path in the context of a representation.

EXPRESS specification:

```
*)
ENTITY founded_kinematic_path
 SUBTYPE OF (representation);
                                       : SET [1 : ?] OF kinematic_path;
 SELF\representation.items
 SELF\representation.context_of_items : geometric_representation_context;
DERIVE
           : SET [1 : ?] OF kinematic_path := SELF\representation.items;
 founding : geometric_representation_context
           := SELF\representation.context_of_items;
END_ENTITY;
```

Attribute definitions:

SELF\representation.items: a set of kinematic_paths which are to be founded.

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SELF\representation.context_of_items: the geometric_representation_context in which the items are founded.

paths: the set of kinematic_paths that are founded.

founding: the context of the path.

7.4.4 motion_link_relationship

A motion_link_relationship describes the relation of a founded_kinematic_path with a frame on a kinematic_link_representation.

EXPRESS specification:

```
*)
ENTITY motion_link_relationship
  SUPERTYPE OF (ONEOF (prescribed_path, resulting_path))
  SUBTYPE OF (representation_relationship);
  SELF\representation_relationship.rep_1 : founded_kinematic_path;
 SELF\representation_relationship.rep_2 : kinematic_link_representation;
                                         : rigid_placement;
  related_frame
DERIVE
  motion
             : founded_kinematic_path
             := SELF\representation_relationship.rep_1;
  frame_link : kinematic_link_representation
             := SELF\representation_relationship.rep_2;
WHERE
  WR1: related_frame IN frame_link\representation.items;
END_ENTITY;
```

Attribute definitions:

SELF\representation_relationship.rep_1: a founded_kinematic_path which specifies a motion.

SELF\representation_relationship.rep_2: a kinematic_link_representation that is to be moved.

related_frame: the frame on a link that is to be moved along the founded_kinematic_path defined as motion.

motion: the founded_kinematic_path that specifies the motion. motion is derived from the inherited rep_1 attribute.

frame_link: the kinematic_link_representation in the context of which the related_frame is geometrically founded that is to be moved along motion. frame_link is derived from the inherited rep_2 attribute.

Formal propositions:

WR1: The related_frame shall be in the items set of frame_link.

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7.4.5 configuration_definition

A configuration_definition specifies a configuration of a kinematic_structure in terms of pair parameter sets.

EXPRESS specification:

```
*)
ENTITY configuration_definition;
  pair_values : SET [1 : ?] OF pair_value;
  t_parameter : motion_parameter_measure;
END_ENTITY;
(*
```

Attribute definitions:

pair_values: the set of values applied to the pairs that specify a configuration_definition.

t_parameter: the parameter associated to the configuration_definition.

7.4.6 interpolated_configuration_sequence

An interpolated_configuration_sequence specifies the motion (forward analysis) of a kinematic_structure in terms of a set of configuration_interpolations. These define the sequence of configuration_definitions and the interpolation between them.

EXPRESS specification:

```
*)
ENTITY interpolated_configuration_sequence;
interpolation : SET [1 : ?] OF configuration_interpolation;
END_ENTITY;
(*
Attribute definitions:
```

interpolation: the interpolation between the configurations.

7.4.7 prescribed_path

A prescribed_path specifies the continuous motion for a control frame that is defined on a kinematic_link. A prescribed_path may be used for backward analysis. All transforms belonging to this path are given relative to the coordinate system identified as the context in which motion is geometrically founded.

If the exact path cannot be achieved for any reason, any combination of joints may be used to achieve a path whose average distance from the prescribed path is minimized. If no controlling joints are given, any joints may be used to achieve the prescribed path.

EXPRESS specification:

```
*)
ENTITY prescribed_path
SUBTYPE OF (motion_link_relationship);
controlling_joints : OPTIONAL SET [1 : 6] OF kinematic_joint;
```

```
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```

```
END_ENTITY;
(*
```

Attribute definitions:

controlling_joints: an optional set of the kinematic_joints which are used to achieve the prescribed path motion.

NOTE – The individual degrees of freedom of a joint depend on the type of the pair that references the joint. Values to the degrees of freedom are assigned by the appropriate subtype of pair_value which always specifies values for all the individual degrees of freedom of a pair. On the other hand, the number of all individual degrees of freedom for the joints in the controlling_joints set must not exceed six in order to avoid the backward analysis problem becoming indeterminate. For this reason, if a pair with more than one degree of freedom (e.g., a cylindrical_pair) is associated with any joint in the controlling_joints set, the size of this set will be less than six.

7.4.8 kinematic_analysis_result

The **kinematic_analysis_result** supplies the result information from the kinematic simulation of a **mechanism**.

EXPRESS specification:

```
*)
ENTITY kinematic_analysis_result;
  analysed_mechanism
                      : mechanism;
  contained_kinematic_results : SET [1 : ?] OF kinematic_result;
WHERE
  WR1: (SIZEOF (QUERY (result <* contained_kinematic_results |
                'KINEMATIC_ANALYSIS_SCHEMA.RESULTING_PATH' IN TYPEOF (result)))
        > 0)
       XOR
       (SIZEOF (QUERY (result <* contained_kinematic_results |
                (('KINEMATIC_ANALYSIS_SCHEMA.' +
                  'INTERPOLATED_CONFIGURATION_SEQUENCE' IN TYPEOF (result))
                 (SIZEOF (QUERY (sequence <* result\
                            interpolated_configuration_sequence.interpolation |
                          (sequence.interpolation <> undefined ))) > 0)))) = 0);
END_ENTITY;
(*
```

Attribute definitions:

analysed_mechanism: the mechanism whose motion produced the results.

contained_kinematic_results: a list of the motions, called results.

Formal propositions:

WR1: If there are no kinematic_results in the contained_kinematic_results set which are of type resulting_path, the interpolation attributes of all the configuration_interpolation instances in all the interpolated_configuration_sequence instances in the contained_kinematic_results set shall all have the value undefined.

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7.4.9 kinematic_analysis_consistency

A kinematic_analysis_consistency relates the result of a kinematic analysis to its input. It asserts that result has been obtained from an analysis using control as its input.

EXPRESS specification:

```
*)
ENTITY kinematic_analysis_consistency;
  control : kinematic_control;
  result : kinematic_analysis_result;
WHERE
  WR1: control.controlled_mechanism :=: result.analysed_mechanism;
END_ENTITY;
(*
```

Attribute definitions:

control: the kinematic_control providing the input for the analysis.

result: the kinematic_analysis_result which contains the results of the analysis.

Formal propositions:

WR1: Input and result data shall be related to the same mechanism.

7.4.10 resulting_path

A resulting_path describes a continuous rigid object motion for a control frame which is on a kinematic_link. The resulting_path may be obtained from the forward analysis. All transforms belonging to the path are given relative to the coordinate system identified as the context in which motion is geometrically founded.

EXPRESS specification:

```
*)
ENTITY resulting_path
   SUBTYPE OF (motion_link_relationship);
   controlling_joints : SET [1 : ?] OF kinematic_joint;
END_ENTITY;
(*
```

Attribute definitions:

controlling_joints: the kinematic_joints which have been used to achieve the resulting path motion.

Informal propositions:

controlling pair requirement: All the pairs which were used to achieve this resulting_path shall be given.

```
*)
END_SCHEMA; -- end kinematic_analysis_control_and_result_schema
(*
```

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Annex A

(normative)

Short names of entities

Table A.1 provides the short names of entities specified in this part of ISO 10303. Requirements on the use of short names are found in the implementation methods included in ISO 10303.

Table A.1 - Short names of entities

Entity name	Short name
ADVENT_ORIENTED_JOINT	ADORJN
CIRCULAR_PATH	CRCPTH
COMPOSITE_PATH	CMPPTH
CONFIGURATION DEFINITION	CNFDFN
CONFIGURATION_INTERPOLATION	CNFINT
CURVE_BASED_PATH	CRBSPT
CYLINDRICAL_PAIR	CYLPR
CYLINDRICAL PAIR RANGE	CYPRRN
CYLINDRICAL_PAIR_VALUE	CYPRVL
FOUNDED_KINEMATIC_PATH	FNKNPT
FULLY_CONSTRAINED_PAIR	FLCNPR
GEAR_PAIR	GRPR
GEAR_PAIR_RANGE	GRPRRN
GEAR_PAIR_VALUE	GRPRVL
INITIAL_STATE	INTSTT
INTERPOLATED_CONFIGURATION_SEQUENCE	INCNSQ
JOINT LOGICAL RELATIONSHIP	JNLGRL
KINEMATIC_ANALYSIS_CONSISTENCY	KNANCN
KINEMATIC_ANALYSIS_RESULT	KNANRS
KINEMATIC_CONTROL	KNMCNT
KINEMATIC_FRAME_BACKGROUND_REPRESENTATION	KFBR
KINEMATIC_FRAME_BACKGROUND_REPRESENTATION_ASSOCIATION	KFBRA
KINEMATIC_FRAME_BASED_TRANSFORMATION	KFBT
KINEMATIC_GROUND_REPRESENTATION	KNGRRP
KINEMATIC_JOINT	KNMJNT
KINEMATICLINK	KNMLNK
KINEMATIC_LINK_REPRESENTATION	KNLNRP
KINEMATIC LINK REPRESENTATION ASSOCIATION	KLRA
KINEMATIC_LINK_REPRESENTATION_RELATION	KLRR
KINEMATICLOOP	KNMLP
KINEMATIC_NETWORK_STRUCTURE	KNNTST

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Table A.1 – (continued)

Entity name	Short name
KINEMATIC_PAIR	KNMPR
KINEMATIC_PATH	KNMPTH
KINEMATIC_PROPERTY_DEFINITION	KNPRDF
KINEMATIC_PROPERTY_REPRESENTATION_RELATION	KPRR
KINEMATIC_STRUCTURE	KNMSTR
KINEMATIC_SUBSTRUCTURE	KNMSBS
KINEMATIC_TREE_STRUCTURE	KNTRST
LINEAR_PATH	LNRPTH
MECHANISM	MCHNSM
MECHANISM BASE PLACEMENT	MCBSPL
MOTION_LINK_RELATIONSHIP	MTLNRL
ORIENTED_JOINT	ORNJNT
ORIENTED_JOINT_IN_TREE	OJIT
PAIR_ACTUATOR	PRACT
PAIR_VALUE	PRVL
PATH_ELEMENT	PTHELM
PATH_ELEMENT_CONNECTION	PTELCN
PATH_NODE	PTHND
PLANAR_CURVE_PAIR	PLCRPR
PLANAR_CURVE_PAIR_RANGE	PCPR
PLANAR_PAIR	PLNPR
PLANAR_PAIR_RANGE	PLPRRN
PLANAR_PAIR_VALUE	PLPRVL
POINT_ON_PLANAR_CURVE_PAIR	POPCP
POINT_ON_PLANAR_CURVE_PAIR_RANGE	POPCPR
POINT_ON_PLANAR_CURVE_PAIR_VALUE	POPCPV
POINT_ON_SURFACE_PAIR	POSP
POINT_ON_SURFACE_PAIR_RANGE	POSPR
POINT_ON_SURFACE_PAIR_VALUE	POSPV
POINT_TO_POINT_PATH	PTPP
PRESCRIBED_PATH	PRSPTH
PRISMATIC_PAIR	PRSPR
PRISMATIC_PAIR_RANGE	PRPRRN
PRISMATIC_PAIR_VALUE	PRPRVL
RACK_AND_PINION_PAIR	RAPP
RACK_AND_PINION_PAIR_RANGE	RAPPR
RACK_AND_PINION_PAIR_VALUE	RAPPV
RESULTING_PATH	RSLPTH

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Table A.1 – (concluded)

Entity name	Short name
REVOLUTE_PAIR	RVLPR
REVOLUTE_PAIR_RANGE	RVPRRN
REVOLUTE_PAIR_VALUE	RVPRVL
ROLLING_CURVE_PAIR	RLCRPR
ROLLING_CURVE_PAIR_VALUE	RCPV
ROLLING_SURFACE_PAIR	RLSRPR
ROLLING_SURFACE_PAIR_VALUE	RSPV
ROTATION_ABOUT_DIRECTION	RTABDR
SCREW_PAIR	SCRPR
SCREW_PAIR_RANGE	SCPRRN
SCREW_PAIR_VALUE	SCPRVL
SIMPLE_PAIR_RANGE	SMPRRN
SLIDING_CURVE_PAIR	SLCRPR
SLIDING_CURVE_PAIR_VALUE	SCPV
SLIDING_SURFACE_PAIR	SLSRPR
SLIDING_SURFACE_PAIR_VALUE	SSPV
SPHERICAL_PAIR	SPHPR
SPHERICAL_PAIR_RANGE	SPPRRN
SPHERICAL_PAIR_VALUE	SPPRVL
SURFACE_PAIR	SRFPR
SURFACE_PAIR_RANGE	SRPRRN
SU_PARAMETERS	SPRM
TRANSFORM	TRNSFR
TRANSLATION	TRNSLT
UNCONSTRAINED_PAIR	UNCPR
UNCONSTRAINED_PAIR_VALUE	UNPRV
UNIVERSAL_PAIR	UNVPR
UNIVERSAL_PAIR_RANGE	UNPRRN
UNIVERSAL_PAIR_VALUE	NPRVL

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Annex B

(normative)

Information object registration

B.1 Document identification

In order to provide for unambiguous identification of an information object in an open system, the object identifier

```
\{ \text{ iso standard } 10303 \text{ part}(105) \text{ version}(1) \}
```

is assigned to this part of ISO 10303. The meaning of this value is defined in ISO/IEC 8824-1, and is described in ISO 10303-1.

B.2 Schema identification

B.2.1 kinematic_structure_schema identification

In order to provide for unambiguous identification of the kinematic_structure_schema in an open system, the object identifier

```
{ iso standard 10303 part(105) version(1) object(1) kinematic-structure-schema(1) }
```

is assigned to the kinematic_structure_schema schema (see clause 5). The meaning of this value is defined in ISO/IEC 8824-1, and is described in ISO 10303-1.

B.2.2 kinematic_motion_representation_schema identification

In order to provide for unambiguous identification of the kinematic_motion_representation_schema in an open system, the object identifier

```
{ iso standard 10303 part(105) version(1) object(1) kinematic-motion-representation-schema(2) }
```

is assigned to the kinematic_motion_representation_schema schema (see clause 6). The meaning of this value is defined in ISO/IEC 8824-1, and is described in ISO 10303-1.

B.2.3 kinematic_analysis_control_and_result_schema identification

In order to provide for unambiguous identification of the kinematic_analysis_control_and_result_schema in an open system, the object identifier

```
{ iso standard 10303 part(105) version(1) object(1) kinematic-analysis-control-and-result-schema(3) }
```

is assigned to the kinematic_analysis_control_and_result_schema schema (see clause 7). The meaning of this value is defined in ISO/IEC 8824-1, and is described in ISO 10303-1.

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Annex C (informative)

EXPRESS listing

This annex provides a listing of the short names and a listing of the EXPRESS specified in this part of ISO 10303. No text or annotation is included. This annex is provided only in computer-interpretable form.

NOTE – The information provided on this diskette is informative; the normative text is that contained in the body of this part of ISO 10303.

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Annex D

(informative)

EXPRESS-G figures

Figures D.1 through D.9 correspond to the *EXPRESS* listing given in annex C. The figures use the *EXPRESS-G* graphical notation for the *EXPRESS* language. *EXPRESS-G* is defined in annex D of ISO 10303-11.

NOTE – In figure D.5 and in figure D.6, all subtypes of kinematic_pair_value and of simple_pair_range actually redeclare their inherited attribute applies_to_pair. These redeclaring relationships have been omitted in these figures for clarity.

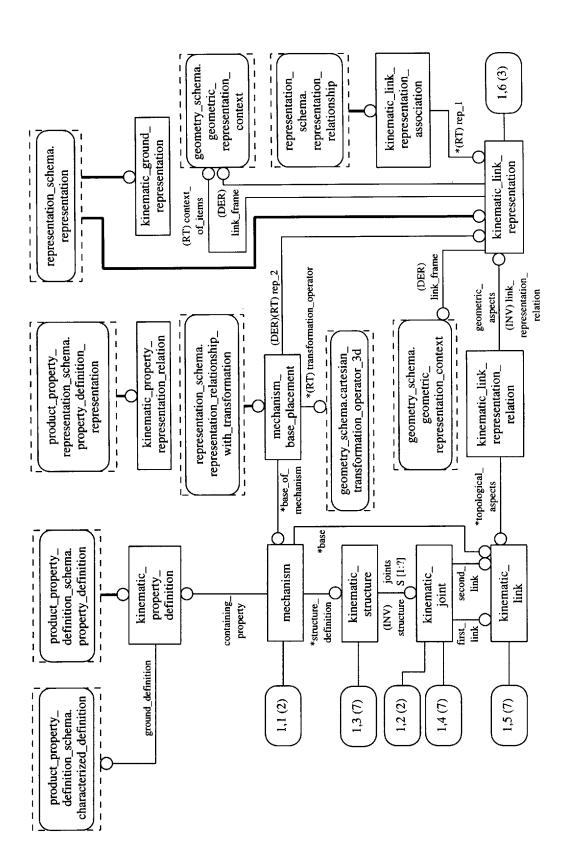


Figure D.1 – Graphical notation of the major aspects of the kinematic_structure_schema. (See also figures D.2 to D.7)

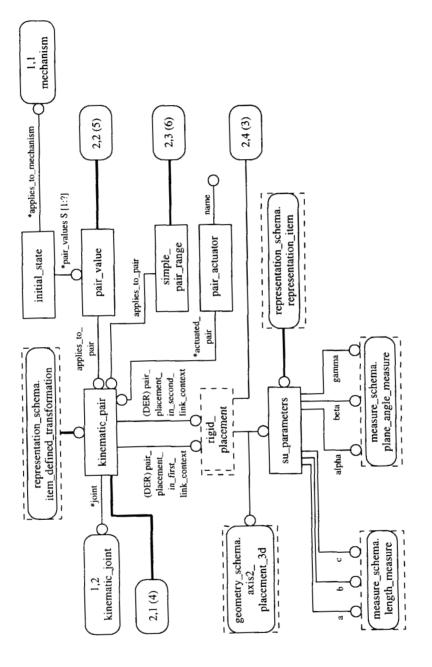


Figure D.2 - Graphical notation of the major aspects of the kinematic structure schema. (See also figures D.1 and D.3 to D.7)

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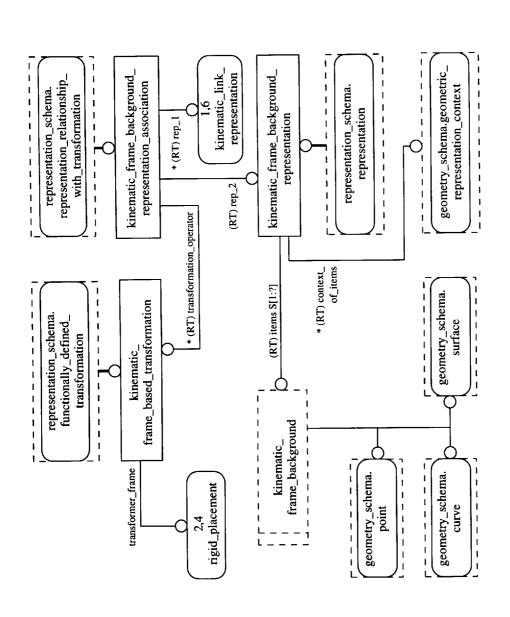


Figure D.3 – Graphical notation of the major aspects of the kinematic structure schema. (See also figures D.1, D.2 and D.4 to D.7)

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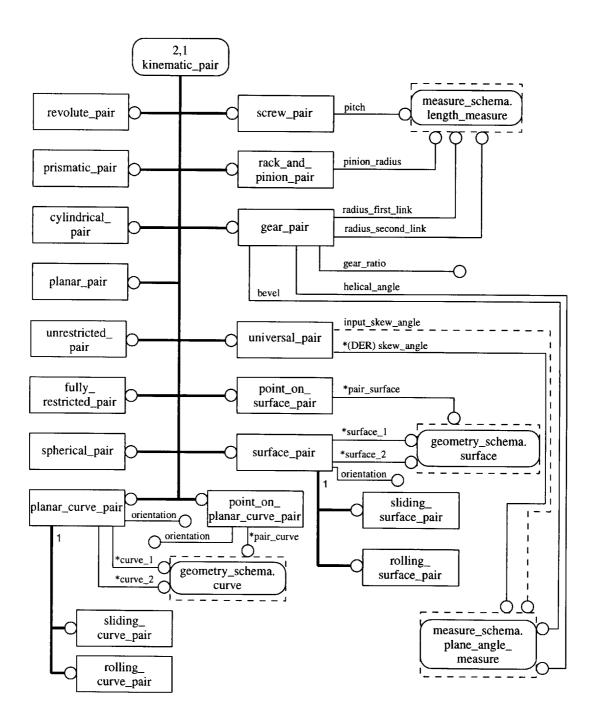


Figure D.4 – Graphical notation of the major aspects of the kinematic_structure_schema.

(See also figures D.1 to D.3 and D.5 to D.7)

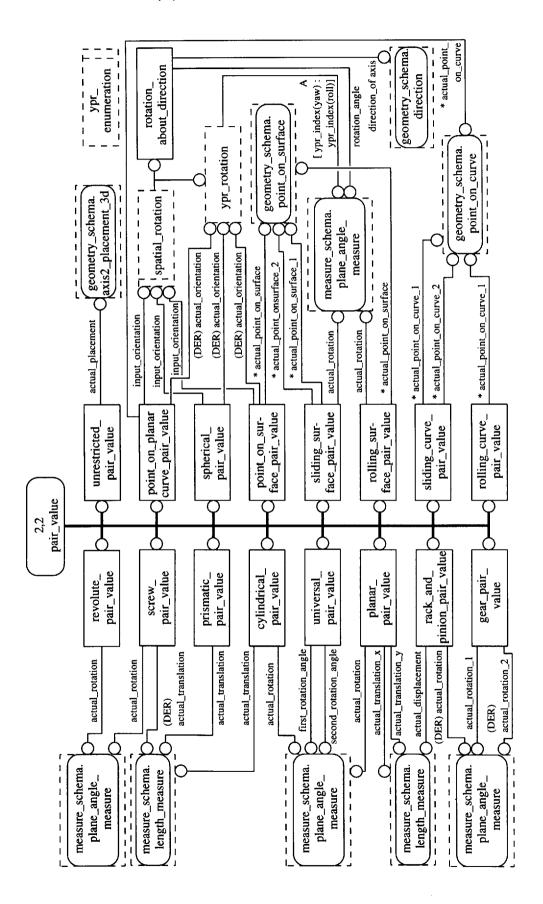
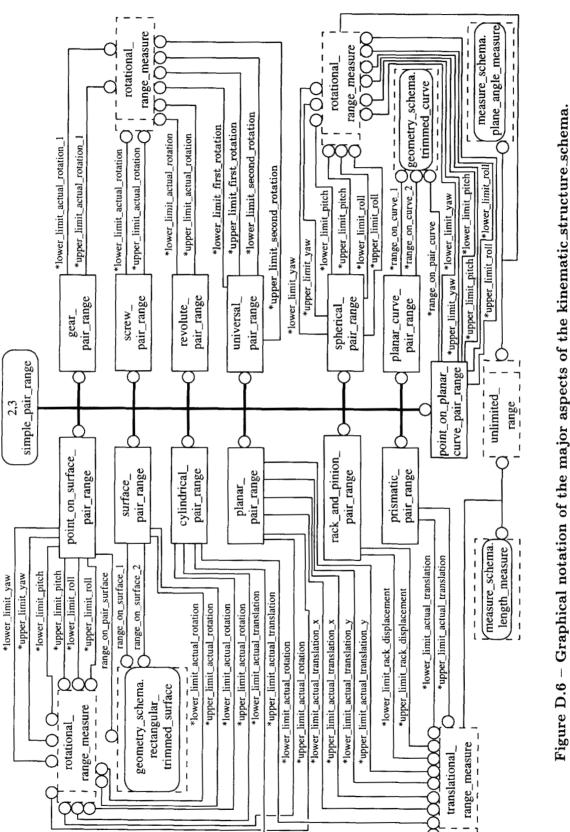


Figure D.5 – Graphical notation of the major aspects of the kinematic structure schema. (See also figures D.1 to D.4, D.6, and D.7)



(See also figures D.1 to D.5 and D.7)

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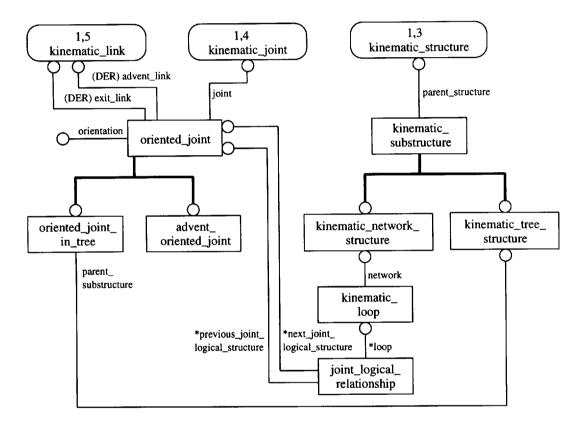


Figure D.7 - Graphical notation of the major aspects of the kinematic_structure_schema.

(See also figures D.1 to D.6)

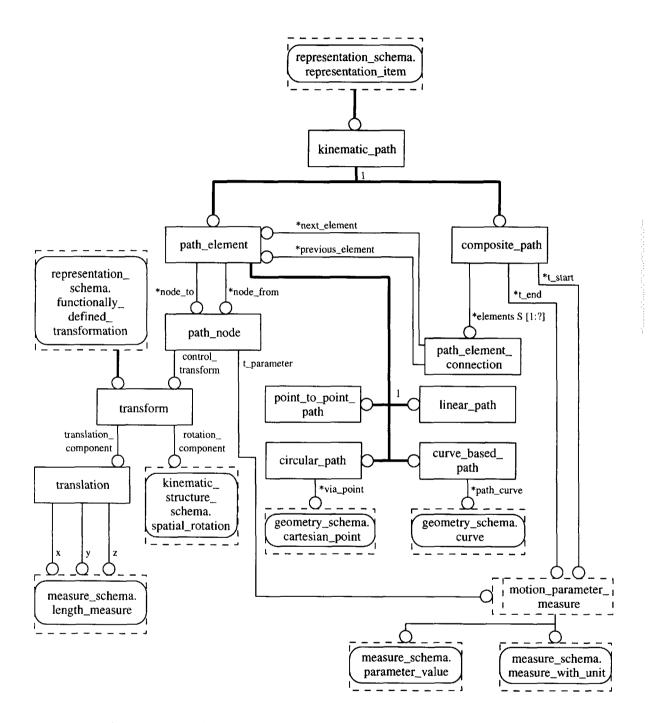


Figure D.8 – Graphical notation of the major aspects of the kinematic_motion_representation_schema

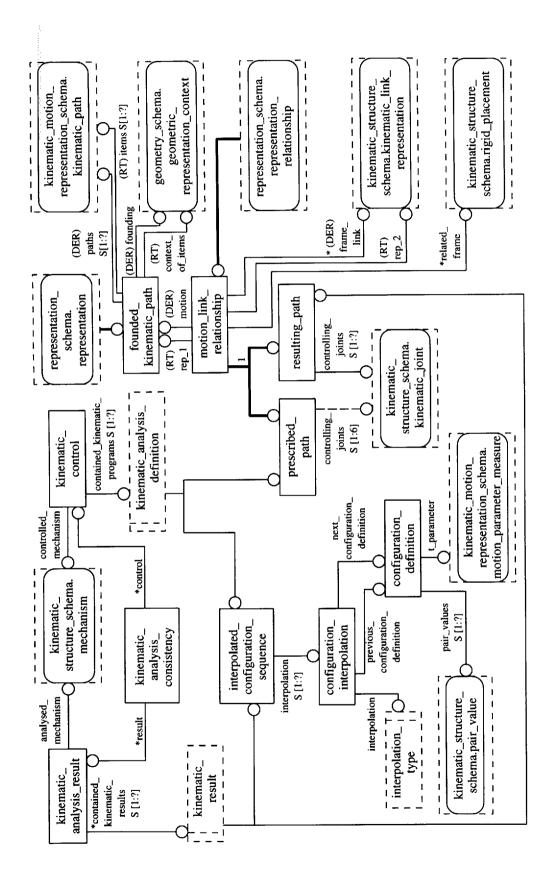


Figure D.9 - Graphical notation of the major aspects of the kinematic_analysis_control_and_result_schema

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Annex E

(informative)

Rotation matrix corresponding to ypr_rotation

This annex provides additional information. It is included here in order to ensure a common understanding of the semantics of **ypr_rotation** (see 5.3.7).

A **ypr_rotation** defines a sequence of three rotations about the yaw, pitch, and roll axes (in this order). In this part of ISO 10303, this rotation sequence is applied mainly to frames; in the case of a **spherical_pair_value**, e.g., it relates the axis directions of the pair frame on the second link of a **spherical_pair** to the axis directions of the pair frame on the first link of the same pair. It may be applied, however, to any vector-valued quantity in \mathbb{R}^3 .

E.1 Matrix representation of ypr_rotation

Let \overline{v} be a 3D vector to which a **ypr_rotation** is applied, and let \overline{w} be the same vector, but measured with respect to the unrotated, i.e., inertial coordinate system. Then the transformation from \overline{v} to \overline{w} can be written in matrix notation as follows:

$$\overline{w} = \boldsymbol{T}_{ypr} \, \overline{v} = \boldsymbol{T}_{roll} \, \boldsymbol{T}_{pitch} \, \boldsymbol{T}_{yaw} \, \overline{v}$$

where

$$oldsymbol{T}_{ypr} = oldsymbol{T}_{roll} \, oldsymbol{T}_{pitch} \, oldsymbol{T}_{yaw}$$

(the rightmost transformation is performed first). Since the yaw, pitch, and roll rotations are rotations about the z-, y-, and x-axis, respectively, of temporary coordinate systems, it is easily shown that

$$m{T}_{yaw} = egin{bmatrix} \cos lpha & -\sin lpha & 0 \ \sin lpha & \cos lpha & 0 \ 0 & 0 & 1 \end{bmatrix}$$

with α being the yaw angle,

$$m{T}_{pitch} = egin{bmatrix} \coseta & 0 & \sineta \ 0 & 1 & 0 \ -\sineta & 0 & \coseta \end{bmatrix}$$

with β being the pitch angle, and

$$m{T}_{roll} = egin{bmatrix} 1 & 0 & 0 \ 0 & \cos \gamma & -\sin \gamma \ 0 & \sin \gamma & \cos \gamma \end{bmatrix}$$

with γ being the roll angle. Hence, the rotation matrix for the entire **ypr_rotation** becomes

$$\boldsymbol{T}_{ypr} = \begin{bmatrix} \cos\alpha\cos\beta & -\sin\alpha\cos\beta & \sin\beta \\ (\sin\alpha\cos\gamma + \cos\alpha\sin\beta\sin\gamma) & (\cos\alpha\cos\gamma - \sin\alpha\sin\beta\sin\gamma) & -\cos\beta\sin\gamma \\ (\sin\alpha\sin\gamma - \cos\alpha\sin\beta\cos\gamma) & (\cos\alpha\sin\gamma + \sin\alpha\sin\beta\cos\gamma) & \cos\beta\cos\gamma \end{bmatrix}$$

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E.2 EXPRESS function

compute_rotation_matrix_from_ypr_rotation

The function **compute_rotation_matrix_from_ypr_rotation** computes the rotation matrix which corresponds to a **ypr_rotation**, given by its angles **yaw**, **pitch**, and **roll**, according to the notation specified in E.1. The function returns an ARRAY [1:3] OF ARRAY [1:3] OF REAL.

NOTES

- 1 This function is provided as an example for applications which need rotations to be given in matrix notation rather than in terms of ypr angles. It should fit into a schema that USEs or REFERENCEs the kinematic_structure_schema (see clause 5).
- 2 The term 'rotation matrix' is not used uniquely within the scientific community. The result of **compute_rotation_matrix_from_ypr_rotation** is valid only for a notation as used in E.1.

EXPRESS specification:

```
FUNCTION compute_rotation_matrix_from_ypr_rotation
         (yaw
                : REAL;
          pitch : REAL;
                : REAL;
          roll
          factor : REAL)
                 : ARRAY [1 : 3] OF ARRAY [1 : 3] OF REAL;
  LOCAL
    y, p, r : REAL;
    result : ARRAY [1 : 3] OF ARRAY [1 : 3] OF REAL;
  END_LOCAL;
  y := factor * yaw;
  p := factor * pitch;
  r := factor * roll;
  result := [ COS(y) * COS(p),
                - SIN(y) * COS(p),
                  SIN(p)],
                  SIN(y) * COS(r) + COS(y) * SIN(p) * SIN(r),
                  COS(y) * COS(r) - SIN(y) * SIN(p) * SIN(r),
                - COS(p) * SIN(r)],
                  SIN(y) * SIN(r) - COS(y) * SIN(p) * COS(r),
                  COS(y) * SIN(r) + SIN(y) * SIN(p) * COS(r),
                  COS(p) * COS(r) ] ];
  RETURN (result);
END_FUNCTION;
```

Argument definitions:

yaw: The yaw angle of the ypr_rotation which is being evaluated.

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NOTE 3 - For an attribute ypr of type ypr_rotation in an entity e, the actual parameter for yaw could be either e.ypr[ypr_index(ypr_enumeration.yaw)] or just e.ypr[1].

pitch: The pitch angle of the ypr_rotation which is being evaluated.

NOTE 4 - For an attribute ypr of type ypr_rotation in an entity e, the actual parameter for pitch could be either e.ypr[ypr_index(ypr_enumeration.pitch)] or just e.ypr[2].

roll: The roll angle of the ypr_rotation which is being evaluated.

NOTE 5 - For an attribute **ypr** of type **ypr_rotation** in an entity **e**, the actual parameter for **roll** could be either **e.ypr[ypr_index(ypr_enumeration.roll)**] or just **e.ypr[3**].

factor: The conversion factor that is required to convert yaw, pitch, and roll into equivalent angle measurements using radian as the plane angle unit.

NOTE 6 – ISO 10303-11 requires the parameters of the SIN and COS functions to be expressed in radians.

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Annex F (informative)

Replacement of DH-Parameters by SU-Parameters

This annex provides additional information.

The principle of the DH-notation is to relate a target frame on a link (denoted k, e.g.) to that pair frame on the preceding link (denoted k-1) in the kinematic chain which belongs to the pair by which link k is connected to link k-1. The target frame may either be a pair frame of another pair on link k or any other frame on link k, e.g., a tool center point frame. The four DH-parameters a_k^{DH} , α_k^{DH} , θ_k^{DH} , and s_k^{DH} define the transformation from the relating pair frame on link k-1 to the target frame on link k, including the motion in the pair shared by both links. See [2] for details of the DH-notation.

The use of DH-parameters is commonly restricted to links that are connected to their predecessor by either a revolute pair or a prismatic pair. One could imagine its application also to cylindrical pairs and to screw pairs.

When using SU-parameters, the relationship between the pair frames of the shared pair is separated from the kinematic link description. The pair is characterised by a transformation involving the pair parameters, which is specific to the pair type, whereas the link data relevant to kinematics are constant transformations from an arbitrarily chosen, but fixed link frame to the various pair frames on the same link. See 5.4.17.

A pair and a link whose data are specified using DH-notation can easily be redefined using SU-notation. The resulting frame definition will probably not take full advantage of the flexibility given by the SU-notation, but it will be a valid definition. The following paragraphs provide a guidance to such a redefinition. The 'target frame' of the DH-notation is chosen as the link frame of link k, as it is usually done implicitly also with the DH-notation. The SU-parameters for the pair frame on link k which mates with the 'relating' pair frame on the preceeding link k-1 are derived from the inverse of the transformation matrix defined by the DH-parameters, with zero pair parameters. Angles are given in radians; occasionally, the given values have to be replaced by the equivalent values in the plane angle units that are actually used by an application.

Revolute pair: For a link k connected to its predecessor k-1 by a revolute pair, the pair transformation corresponds essentially to the yaw rotation as given in E.1, replacing there α by the pair parameter θ_k^{DH} . The SU-parameters for the pair frame of the revolute pair on link k, as defined in 5.4.17, are found by setting $a_k = a_k^{DH}$, $\alpha_k = \alpha_k^{DH}$, $b_k = -s_k^{DH}$, $\beta_k = \pi$, $c_k = 0$, and $\gamma_k = \pi$.

Prismatic pair: For a link k connected to its predecessor k-1 by a prismatic pair, the pair transformation is a pure translational transformation along the z-axes, with s_k^{DH} being the pair parameter. The SU-parameters for the pair frame of the prismatic pair on link k are found by setting $a_k = a_k^{DH}$, $\alpha_k = \alpha_k^{DH}$, $b_k = 0$, $\beta_k = \pi - \theta_k^{DH}$, $c_k = 0$, and $\gamma_k = \pi$.

Cylindrical pair and screw pair: For a link k connected to its predecessor k-1 by a cylindrical pair or by a screw pair, the pair transformation is composed of a translational transformation along the z-axes (pair parameter s_k^{DH}) and a rotational yaw transformation (pair parameter θ_k^{DH}). In the case of a cylindrical pair, the pair parameters s_k^{DH} and θ_k^{DH} are independent one from the other, whereas for a screw pair one of them depends functionally on the

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other (see 5.4.29). The SU-parameters for the pair frame of the cylindrical pair or of the screw pair on link k are found by setting $a_k = a_k^{DH}$, $\alpha_k = \alpha_k^{DH}$, $b_k = 0$, $\beta_k = \pi$, $c_k = 0$, and $\gamma_k = \pi$. Here it is supposed that both pair frames of the cylindrical or screw pair coincide if both parameters, s_k^{DH} and θ_k^{DH} , are equal to zero.

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Annex G (informative)

Bibliography

- [1] SHETH, U.N. & UICKER, J.J.; A generalized symbolic notation for mechanisms, Journal of Engineering for Industry, Trans. ASME, Feb. 1971.
- [2] DENAVIT, J. & HARTENBERG, R.S.; A kinematic notation for lower pair mechanisms based on matrices, Journal of Applied Mechanics, Vol. 22, Trans. ASME, Vol. 77, Series E, 1955.
- [3] HARTSFIELD, N. & RINGEL, G.; Pearls in Graph Theory: a Comprehensive Introduction, Academic Press, Inc., San Diego, 1990.

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