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Analytical colorimetry

Part 2: Saunderson correction, solutions of the Kubelka-Munk equation, tinting strength, hiding power



BS ISO 18314-2:2015

National foreword

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Analytical colorimetry —

Part 2:

Saunderson correction, solutions of the Kubelka-Munk equation, tinting strength, hiding power

Analyse colorimétrique —

Partie 2: Correction de Saunderson, solutions de l'équation de Kubelka-Munk, force colorante, pouvoir couvrant





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Foreword

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The committee responsible for this document is ISO/TC 256, *Pigments, dyestuffs and fillers*.

ISO 18314 consists of the following parts, under the general title *Analytical colorimetry*:

- Part 1: Practical colour measurement
- Part 2: Saunderson correction, solutions of the Kubelka-Munk equation, tinting strength, hiding power
- Part 3: Special indices

Analytical colorimetry —

Part 2:

Saunderson correction, solutions of the Kubelka-Munk equation, tinting strength, hiding power

1 Scope

This part of ISO 18314 specifies the Saunderson correction for different measurement geometries and the solutions of the Kubelka-Munk equation for hiding and transparent layers. It also specifies methods for the calculations of the tinting strength including the residual colour difference with different criteria and of the hiding power.

The procedures for preparing the samples for these measurements are not part of this part of ISO 18314. They are agreed between the contracting parties or are described in other national or International Standards.

2 Terms, definitions, symbols, and abbreviated terms

2.1 Terms and definitions

For the purposes of this document, the following terms and definitions apply.

2.1.1

tinting strength

measure of the ability of a colorant, based on its absorption, to impart colour to other materials

2.1.2

relative tinting strength

Cre

percentage ratio of those mass fractions of the coloured pigment reference and test samples ($m_{\rm r}$ and $m_{\rm t}$, respectively) that cause the particular tinting strength criterion used to have identical values for the reference and test samples

2.1.3

tinting strength criterion

parameter that describes the colouring effect of a colorant, based on its absorption

Note 1 to entry: The tinting strength criteria used in this part of ISO 18314 are the following:

- value of the Kubelka-Munk function at the absorption maximum;
- weighted sum of the Kubelka-Munk function values;
- tristimulus value Y;
- the smallest of the tristimulus values X, Y, Z;
- shade depth parameter B.

Examples of other tinting strength parameters not used in this part of ISO 18314 are the following:

- unweighted sum of the Kubelka-Munk function values;
- chromaticity given by the three colour coordinates (L*, a*, b*);

reflectance factor at the absorption maximum.

2.1.4

residual colour difference

colour difference that remains between the white reductions of the reference and test samples when the tinting strength criterion values are the same or have been equalized

EXAMPLE Given by ΔE^* .

2.1.5

standard shade depth

shade depth

measure of the intensity of a colour sensation, which increases with increasing chroma and decreases with increasing lightness

Note 1 to entry: Standard shade depths are values set by convention. For colourimetric purposes, the standard shade depth is defined by the shade depth parameter B = 0, which is calculated from the tristimulus value, Y, and the chromaticity coordinates, *x* and *y*.

2.1.6

hiding power

ability of a pigmented medium to hide the colour or the colour differences of a substrate

2.2 Symbols and abbreviated terms

a	constant
α^*	CIELAB colour coordinate
$a(\varphi)$	factor
$a(\lambda)$	auxiliary variable
<i>b</i> *	CIELAB colour coordinate
$b(\lambda)$	auxiliary variable
В	shade depth parameter
C_{rel}	relative tinting strength
D_{m}	hiding power value indicating the area of the contrast substrate concerned, in \mbox{m}^2 , which can be coated with 1 \mbox{kg}
$D_{ m V}$	hiding power value indicating the area of the contrast substrate concerned, in \mbox{m}^2 , which can be coated with 1 \mbox{l}
$F(\lambda)$	Kubelka-Munk function
$F'(\lambda)$	modified Kubelka-Munk function
$g(\lambda)$	weighting function (defined as the sum of the colour matching functions $\bar{x}(\lambda)$, $\bar{y}(\lambda)$, and $\bar{z}(\lambda)$ for a 10° standard observer)
h	thickness

K

coefficient

- $K(\lambda)$ absorption coefficient
- $(K/S)_r$ Kubelka-Munk value of reference sample
- $(K/S)_t$ Kubelka-Munk value of test sample
- *L** CIELAB lightness
- $m_{\rm r}$ mass fraction of coloured pigment reference sample
- *m*_t mass fraction of coloured pigment test sample
- *n* refractive index
- r_0 reflection coefficient at the surface for directional light incident perpendicular from outside
- $\frac{-}{r_0}$ reflection coefficient at the surface for directional light incident parallel under 45° from outside
- r_2 reflection coefficient for light incident diffusely from the inside of the specimen
- $R(\lambda)$ reflectance spectrum
- $R(\lambda)$ reflectance of infinitely thick layer
- $R(\lambda)^*$ reflectance of the sample
- $R(\lambda)_{\text{ob}}^*$ Saunderson-corrected reflectance of the black substrate
- $R(\lambda)^*$ Saunderson-corrected reflectance of the white substrate
- $R(\lambda)_{h}^{*}$ Saunderson-corrected reflectance of the sample on black substrate
- $R(\lambda)_{w}^{*}$ Saunderson-corrected reflectance of the sample on white substrate
- $R'(\lambda)$ modified reflectance spectrum including surface effects
- s saturation
- $S(\lambda)$ scattering coefficient
- T weighted sum
- *x, y* chromaticity coordinates
- *X, Y, Z* tristimulus values
- ΔE^* residual colour difference

$$\Delta E_{ab}^{\star}$$
 CIELAB colour difference

 φ hue angle

 $arphi_0$ closest angle in the table below the hue angle

3 Saunderson correction

3.1 General

For colourimetric calculation it is necessary to account for surface phenomena to obtain viable results. The formulas are known as Saunderson correction, their derivation can be found in References [1] and [2] The necessary coefficients are solutions of the Fresnel formulae [3] depending on the index of refraction for the given binder.

The formulae are derived assuming an ideal surface, a perfectly hiding layer and a perfectly diffuse scattering of light inside the interior of the specimen. Any deviation from these assumptions shall lead to consideration of the usefulness of the following calculations.

The formulae given here are for two of the most widespread geometries: diffuse incidence, 0° observation (d/0°) and 45° incidence, 0° observation (45°/0°). In nearly every colourimeter used, the measurement angle is not 0° but 8° . This deviation is not considered problematic.

The constants necessary for the calculation are the following:

 r_0 : reflection coefficient at the surface for directional light incident perpendicular from outside. For n = 1.5 $r_0 = 0.040$.

reflection coefficient at the surface for directional light incident parallel under 45° from outside. For n = 1.5, $\overline{r_0} = 0.050$.

 r_2 : reflection coefficient for light incident diffusely from the inside of the specimen. For $n = 1,5, r_2 = 0,596$.

3.2 Incidence diffuse, observation 0° (d/0°)

The constant a = 1 if a gloss trap is closed and a = 0 if the gloss trap is open and the specular reflection is excluded.

$$R(\lambda) = ar_0 + \frac{(1 - r_0)(1 - r_2)R(\lambda) *}{1 - r_2R(\lambda) *} \tag{1}$$

for
$$a = 1$$
:
$$R(\lambda)^* = \frac{R(\lambda) - r_0}{1 - r_0 - r_2 \left[1 - R(\lambda)\right]}$$
 (2)

for
$$a = 1$$
: $R(\lambda)^* = \frac{R(\lambda)}{1 - r_0 - r_2 + r_2[r_0 + R(\lambda)]}$ (3)

3.3 Incidence 45°, observation 0° (45°: 0°)

$$R(\lambda) = \frac{\left(1 - r_0\right)\left(1 - \overline{r_0}\right)\frac{1}{n^2}R(\lambda)^*}{1 - r_2R(\lambda)^*} \tag{4}$$

$$R(\lambda)^* = \frac{n^2 R(\lambda)}{1 - r_0 - \overline{r}_0 + r_0 \overline{r}_0 + n^2 r_2 R(\lambda)}$$
(5)

4 Solution of the Kubelka-Munk equations

The Kubelka-Munk theory describes the reflection of a pigmented layer by two constants: absorption $[K(\lambda)]$ and scattering $[S(\lambda)]$. It is based on the following assumptions:

- a) ideally diffuse radiation distribution on the irradiation side;
- b) ideally diffuse radiation distribution in the interior of the layer;
- c) no consideration of surface phenomena resulting from the discontinuity in refractive index.

For an infinitely thick, respectively hiding layer with a reflectance of $R(\lambda)_{\infty}$, the following solutions are found, which allow the determination of the relation between the scattering and the absorption coefficient:

$$\frac{K(\lambda)}{S(\lambda)} = \frac{\left(1 - R(\lambda)_{\infty}\right)^2}{2 R(\lambda)_{\infty}} \equiv F(R(\lambda)_{\infty})$$
 (6)

respectively the inverse:

$$R(\lambda)_{\infty} = 1 + \frac{K(\lambda)}{S(\lambda)} - \sqrt{2\left(\frac{K(\lambda)}{S(\lambda)}\right) + \left(\frac{K(\lambda)}{S(\lambda)}\right)^2}$$
(7)

For the determination of the scattering and absorption coefficient two different methods can be applied (the Saunderson correction shall be used):

Method 1 Measurement of the reflectance of an infinite thick (respectively hiding) layer and the reflectance $R(\lambda)^*$ of a coating of the thickness, h, on a substrate of the reflection $R(\lambda)_0^*$.

$$a(\lambda) = \frac{1}{2} \left[\frac{1}{R(\lambda)_{\infty}^*} + R(\lambda)_{\infty}^* \right]$$
 (8)

$$b(\lambda) = a(\lambda) - R(\lambda)_{\infty}^{*} = \frac{1}{2} \left[\frac{1}{R(\lambda)_{\infty}^{*}} - R(\lambda)_{\infty}^{*} \right]$$
(9)

$$S(\lambda) = \frac{1}{b(\lambda)h} \operatorname{Arcoth} \frac{1 - a(\lambda) R(\lambda)^* - R(\lambda)_0^* + R(\lambda)^* R(\lambda)_0^*}{b(\lambda) R(\lambda)^* - R(\lambda)_0^*}$$
(10)

$$K(\lambda) = S(\lambda)[a(\lambda) - 1] \tag{11}$$

Method 2 This method applies two layers of equal thickness (h) on black and white substances. After the determination of the auxiliary variables $a(\lambda)$, $b(\lambda)$ according to Formulae (12) and (13), either Formula (14) or (15) may be used to calculate the scattering coefficient $S(\lambda)$. The possibility with the least experimental uncertainty should be chosen.

$$a(\lambda) = \frac{\mathbb{1} + R(\lambda)_{w}^{*} R(\lambda)_{ow}^{*} \mathbb{R}(\lambda)_{b}^{*} - R(\lambda)_{ob}^{*} + \mathbb{1} + R(\lambda)_{b}^{*} R(\lambda)_{ob}^{*} \mathbb{R}(\lambda)_{ob}^{*} \mathbb{R}(\lambda)_{ow}^{*} - R(\lambda)_{w}^{*}}{2 \mathbb{R}(\lambda)_{b}^{*} R(\lambda)_{ow}^{*} - R(\lambda)_{w}^{*} R(\lambda)_{ob}^{*}}$$

$$(12)$$

$$b(\lambda) = \sqrt{a(\lambda)^2 - 1} \tag{13}$$

$$S(\lambda) = \frac{1}{b(\lambda) h} \operatorname{Arcoth} \frac{1 - a(\lambda)[R(\lambda)_{b}^{*} - R(\lambda)_{ob}^{*}] + R(\lambda)_{b}^{*} R(\lambda)_{ob}^{*}}{b(\lambda)[R(\lambda)_{b}^{*} - R(\lambda)_{ob}^{*}]}$$
(14)

$$S(\lambda) = \frac{1}{b(\lambda) h} \operatorname{Arcoth} \frac{1 - a(\lambda) [R(\lambda)_{w}^{*} - R(\lambda)_{ow}^{*}] + R(\lambda)_{w}^{*} R(\lambda)_{ow}^{*}}{b(\lambda) [R(\lambda)_{w}^{*} - R(\lambda)_{ow}^{*}]}$$
(15)

$$R(\lambda)^* = \frac{1 - R(\lambda)_o^* [a(\lambda) - b(\lambda) \coth\{b(\lambda) S(\lambda) h\}]}{a(\lambda) - R(\lambda)_o^* + b(\lambda) \coth\{b(\lambda) S(\lambda) h\}}$$
(16)

NOTE The formulation of the Kubelka-Munk theory leads to a system of differential equations. The solution can be stated in different ways either by the use of the trigonometric functions used here or by the use of logarithmic functions. They are mathematically equivalent.

5 Determination of relative tinting strength and residual colour difference of coloured pigments

5.1 General

All the methods specified here presuppose, at least approximately, a linear relationship between the concentration of the colorant and the Kubelka-Munk function.

It is assumed that the scattering by the draw-downs being measured is dominated by the white pigment and the absorption by the coloured pigment. All these conditions shall be met to ascertain correct results of the methods described here. The Kubelka-Munk function for the white paste can be neglected in most cases.

5.2 Principle

The reference and test samples are incorporated into white pastes. The corresponding reflectance spectra are measured on opaque draw-downs of the resulting coloured pastes. The appropriate tinting strength criterion is calculated from the measured values.

If the tinting strength criterion values for the reference and test samples differ, the mass fraction of the sample is increased or decreased until the values become equal. This adjustment may be performed either experimentally or mathematically.

If the tinting strength criterion values for the reference and test samples are the same, or after they have been equalized, the residual colour difference between the white reductions of the reference and test samples is calculated from the corresponding reflectance spectra.

A spectrophotometer with d:8° or 8°:d measuring geometry with or without gloss trap, or instruments with $45^{\circ}:0^{\circ}$ or $0^{\circ}:45^{\circ}$ measuring geometry are recommended.

5.3 Procedure

5.3.1 General

The reflectance of an opaque draw-down of the white reduction of the reference sample and the corresponding reflectance of the test sample are measured in the visible spectral range.

5.3.2 Evaluation of absorption at the absorption maximum

The tinting strength criterion is the maximum Kubelka-Munk value. Prerequisite for this method are equal concentrations of reference and test pigments in the white pastes.

Determine the wavelength in the reflectance spectra of the white reductions at which the reflectance is a minimum. From the minimum Saunderson-corrected reflectance R_r^* and R_t^* , calculate the Kubelka-Munk values $(K/S)_r$ and $(K/S)_t$ for this wavelength by means of Formula (6). The relative tinting strength C_{rel} is then obtained from:

$$C_{\text{rel}} = \left[\frac{\left(\frac{K}{S} \right)_{\text{t}}}{\left(\frac{K}{S} \right)_{\text{r}}} \right] \cdot 100 \tag{17}$$

NOTE This method does not involve any explicit equalization of the tinting strength criterion. Because of the assumption of linearity between the Kubelka-Munk function and the concentration, equalization is implicit in the formalism of

$$\frac{\left(\frac{K}{S}\right)_{\mathsf{t}}}{\left(\frac{K}{S}\right)_{\mathsf{r}}} = \frac{m_{\mathsf{r}}}{m_{\mathsf{t}}} \tag{18}$$

Consequently, Formula (17) can be transformed into the defining Formula (19).

$$C_{\rm rel} = \frac{m_{\rm r}}{m_{\rm t}} \cdot 100 \tag{19}$$

5.3.3 Evaluation of the weighted K/S sum

The tinting strength criterion is the weighted K/S sum. From the spectra of the Saunderson-corrected reflectance $R(\lambda)^*$ for the test and reference samples, calculate the corresponding Kubelka-Munk values $F(\lambda) = (K/S)(\lambda)$ and in each case generate the following weighted sum:

$$T = \sum_{(400-700\text{nm})} g(\lambda) \cdot F(\lambda) \tag{20}$$

The function $g(\lambda)$ is a weighting function, defined as the sum of the colour matching functions $\overline{x}(\lambda)$, $\overline{y}(\lambda)$, and $\overline{z}(\lambda)$ for a 10° standard observer (see Reference [4]). This weighting function is an empirical function, but without any theoretical foundation.

The relative tinting strength is calculated from the weighted sums and the mass fractions of the test and reference samples:

$$C_{\text{rel}} = \left[\frac{\left(T_{\text{t}} \cdot m_{\text{r}} \right)}{\left(T_{\text{r}} \cdot m_{\text{t}} \right)} \right] \cdot 100 \tag{21}$$

$$=\frac{\left(\frac{m_{\rm r}}{T_{\rm r}}\right)}{\left(\frac{m_{\rm t}}{T_{\rm f}}\right)}\cdot 100$$

NOTE This method does not involve any explicit equalization of the tinting strength criterion. Because of the assumption of linearity between the Kubelka-Munk function and the concentration, and hence also between the Kubelka-Munk function and the tinting strength criterion *T*, equalization is implicit in the formalism of Formula (21).

If the difference between the tinting strength criterion of the reference sample T_r and that of the test sample T_t is greater than 15 %, the mass fraction of the test sample should be varied accordingly.

To obtain the residual colour difference, the Kubelka-Munk function of the test sample is modified as follows:

$$F_{t}'(\lambda) = F_{t}(\lambda) \cdot \frac{T_{r}}{T_{t}} \tag{22}$$

Solving Formula (6) for R [as done in Formula (7)], calculate a modified reflectance spectrum $R_r^{*'}(\lambda)$ for the test sample from its modified Kubelka-Munk function $F_t'(\lambda)$ and then subject it to an inverse Saunderson correction (see Clause 3) to obtain a modified $R_t'(\lambda)$ that includes surface effects. This spectrum yields the colour coordinates of the white reduction of the test sample after equalizing the tinting strength. Calculate the residual colour difference from the reflectance spectrum $R_r(\lambda)$ of the white reduction of the reference sample and the modified reflectance spectrum $R_t'(\lambda)$.

5.3.4 Evaluation by equalizing the tristimulus value, *Y*

The tinting strength criterion is the tristimulus value, Y. From the reflectance spectra, $R(\lambda)$, for the white reductions of the test and reference samples, calculate the tristimulus value Y_r for the reference sample and Y_t for the test sample (see Reference [5]). The contracting parties agree on the standard illuminant and standard observer used.

From Formula (6) and the Saunderson-corrected reflectance $R_t^*(\lambda)$ for the white reduction of the test sample, calculate the corresponding Kubelka-Munk function $F_t(\lambda)$ for the test sample. Adjust Y_t to the value for the reference sample by varying m_t and then use the resulting value of m_t to determine a modified Kubelka-Munk function $F_t'(\lambda)$ for the test sample:

$$F_{\mathsf{t}}'(\lambda) = F_{\mathsf{t}}(\lambda) \cdot \frac{m_{\mathsf{t}}'}{m_{\mathsf{t}}} \tag{23}$$

Solving Formula (6) for R, calculate a modified reflectance spectrum $R_t^{*'}(\lambda)$ for the test sample from its modified Kubelka-Munk function $F_t'(\lambda)$ and subject it to an inverse Saunderson correction to obtain a modified $R_t'(\lambda)$ that includes surface effects. From this spectrum determine Y_t' .

Vary the mass fraction of the test sample until the tinting strength criterion has been equalized, i.e.:

$$Y_r = Y_t' \tag{24}$$

This variation of m_t is best carried out by an iterative mathematical procedure, but may also be done experimentally.

Calculate the relative tinting strength from the mass fraction m_t of the test sample that results in equalization of the tinting strength:

$$C_{\text{rel}} = \left\lceil \frac{m_{\text{r}}}{m_{\text{t}}} \right\rceil \cdot 100 \tag{25}$$

Calculate the residual colour difference from the reflectance spectrum $R_r(\lambda)$ of the white reduction of the reference sample and the modified reflectance spectrum $R_t'(\lambda)$ of the white reduction of the test sample.

5.3.5 Evaluation by equalizing the smallest of the tristimulus values X, Y, and Z

The tinting strength criterion is the smallest of the tristimulus values X, Y, and Z. From the reflectance spectra $R(\lambda)$ for the white reductions of the test and reference samples, calculate the corresponding tristimulus values X_r , Y_r , and Z_r for the reference sample and X_t , Y_t , and Z_t for the test sample (see Reference [5]). The contracting parties agree on the standard illuminant and standard observer used.

The tinting strength criterion is defined to be the tristimulus value that has the smallest numerical value for the test and reference samples.

The subsequent procedure is as described in 5.3.4, but replacing the tristimulus value Y by the smallest of the calculated tristimulus values (X, Y, or Z).

5.3.6 Evaluation by equalizing the shade depth

The tinting strength criterion is the shade depth parameter B. From the reflectance spectra $R(\lambda)$ for the white reductions of the test and reference samples, calculate the tristimulus values Y and the chromaticity coordinates x and y (see Reference [5]). This may be carried out with standard illuminant D65 and a 10° standard observer or with standard illuminant C and a 2° standard observer. The contracting parties agree on the parameters used.

From the values of Y, x, and y for the test and reference samples, calculate the shade depth parameter B of the white reductions for a standard shade depth of 1/1, 1/3, 1/9, 1/25, or 1/200. The standard shade depth used should preferably be that which yields the smallest value of B. However, it may also be a shade depth agreed on by the contracting parties. The standard shade depth used is quoted together with the result for the relative tinting strength.

The shade depth parameters for the various standard shade depths are calculated as follows:

$$B_{1/1} = \sqrt{Y} \cdot (s \cdot a \, (\varphi)_{1/1} - 10) + 19 \tag{26}$$

$$B_{1/3} = \sqrt{Y} \cdot (s \cdot a \, (\varphi)_{1/3} - 10) + 29 \tag{27}$$

$$B_{1/9} = \sqrt{Y} \cdot (s \cdot a (\varphi)_{1/9} - 10) + 41$$
 (28)

$$B_{1/25} = \sqrt{Y} \cdot (s \cdot a \, (\varphi)_{1/25} - 10) + 56 \tag{29}$$

$$B_{1/200} = \sqrt{Y} \cdot (s \cdot a \, (\varphi)_{1/200} - 10) + 73 \tag{30}$$

where

s is the saturation: 10 times the linear distance between the chromaticity coordinates x, y and the achromatic point, i.e.:

$$s = 10 \cdot \sqrt{(x - x_0)^2 + (y - y_0)^2}$$
(31)

with $x_0 = 0.3138$ and $y_0 = 0.3310$ for standard illuminant D65 and a 10° standard observer and $x_0 = 0.3101$ and $y_0 = 0.3162$ for standard illuminant C and a 2° standard observer

 φ is the hue angle (in degrees):

$$\varphi = \frac{180^{\circ}}{\pi} \cdot \arctan \frac{y - y_0}{x - x_0} \tag{32}$$

with

$$0^{\circ} < \varphi < 90^{\circ}$$
 for $y - y_0 > 0$ and $x - x_0 > 0$

$$90^{\circ} < \varphi < 180^{\circ}$$
 for $y - y_0 > 0$ and $x - x_0 < 0$

$$180^{\circ} < \varphi < 270^{\circ}$$
 for $y - y_0 < 0$ and $x - x_0 < 0$

$$270^{\circ} < \varphi < 360^{\circ}$$
 for $y - y_0 < 0$ and $x - x_0 > 0$

 $a(\varphi)$ are factors:

$$a(\varphi) = a(\varphi_0) + K_1 \cdot W + K_2 \cdot W^2 + K_3 \cdot W^3$$
(33)

Tables of coefficients K_1 , K_2 , and K_3 for standard shade depths 1/1, 1/3, 1/9, 1/25, and 1/200 are given in Annex A for standard illuminant D65 and a 10° standard observer and in Annex B for standard illuminant C and a 2° standard observer.

$$W = \frac{\varphi - \varphi_0}{100^{\circ}} \tag{34}$$

 φ_0 is the closest angle in the table below the hue angle φ (in degrees). The coefficients K_1 , K_2 , and K_3 of φ_0 are used in Formula (33).

From Formula (6) and the Saunderson-corrected reflectance $R(\lambda)^*$ for the test sample, calculate the corresponding Kubelka-Munk functions $F(\lambda)$ for the test and reference samples. Adjust the B values for the white reductions of the test and reference samples to the specified standard shade depth by varying the mass fractions $m_{\rm t}$ and $m_{\rm r}$, and use the resulting values of $m_{\rm t}$ and $m_{\rm r}$ to determine modified Kubelka-Munk functions $F'(\lambda)$ as follows:

$$F_{\mathsf{t}}'(\lambda) = F_{\mathsf{t}}(\lambda) \cdot \frac{m_{\mathsf{t}}'}{m_{\mathsf{t}}} \tag{35}$$

$$F_{\mathbf{r}'}(\lambda) = F_{\mathbf{r}}(\lambda) \cdot \frac{m_{\mathbf{r}'}}{m_{\mathbf{r}}} \tag{36}$$

Solving Formula (6) for R, calculate modified reflectance spectra $R'(\lambda)^*$ from these modified Kubelka-Munk functions $F'(\lambda)$ and subject the spectra to an inverse Saunderson correction (see <u>Clause 3</u>) to obtain modified $R(\lambda)$ that include surface effects. From these spectra calculate the B values for the white reductions of the test and reference samples.

Vary the mass fractions $m_{\rm t}$ and $m_{\rm r}$ independently of one another, preferably by an iterative mathematical procedure, until the shade depth of the white reductions of the test and reference samples equals that of the specified standard shade depth, i.e. until:

 $B_t = 0$ for m_t and

 $B_r = 0$ for m_r

Then calculate the relative tinting strength from:

$$C_{\text{rel}} = \left[\frac{m_{\text{r}}'}{m_{\text{t}}'} \right] \cdot 100 \tag{37}$$

Calculate the residual colour difference (see Reference [6]) from those reflectance spectra $R_t'(\lambda)$ and $R_r'(\lambda)$ for the test and reference samples that result in equalization of the shade depth.

6 Determination of hiding power of pigmented media

6.1 General

The hiding power value indicates what area, in square metres, of a given contrast substrate can be coated with the unit of quantity of the sample in such a manner that a specified hiding criterion is achieved. The hiding criterion shall be an agreed colour difference between the two contrasting areas of the coated contrast substrate. A $\Delta E_{ab}^* = 1$ is commonly applied. For achromatic coatings, a contrast ratio of 0,98 is used to take into account the 2 % threshold value for brightness perception by the human eye.

The substrates have of course to be standardized for an exact method of determination. Values of reflectance close to zero for black and 0,8 for white substrates are employed.

The parameter determined by all methods is the minimal film thickness h_D necessary to fulfill the criteria used. The reciprocal of this parameter is equivalent to hiding power value $D = 1/h_D$. The hiding power value can be determined and specified in the following ways:

- hiding power value D_v in square metres per litre;
- hiding power value $D_{\rm m}$, in square metres per kilogram.

 $D_{\rm v}$ and $D_{\rm m}$ each indicate the area of the contrast substrate concerned, in square metres, which can be coated with $1 \, \rm l \, or \, 1 \, kg$ of the pigmented medium so as to ensure hiding (in the sense of the hiding criterion).

Colourimetric methods for the determination of the hiding power use the general solutions for the Kubelka-Munk equation in combination with an iterative program to determine the necessary film thickness to fulfill the hiding power criteria chosen. This is the most straightforward way leading to the best results.

It is possible to work with two non hiding layers on white and black substances or with a hiding layer in combination with a non hiding one on a black or white substrate. The method should preferably be determined by reviewing the data available.

6.2 Example for white or light coloured paints with a contrast ratio of 0,98 as hiding power criterion

The following equations specify a method applicable for white and light-coloured paints where the colour differences between black and white substrates is determined by the lightness differences. In such cases $R(\lambda)$ can be replaced by R(Y) with R(Y) being the tristimulus value Y divided by 100.

The following equations give the reflectance over a black $R(Y)_B^*$ and white $R(Y)^*$ substrate:

$$R(Y)_{B}^{*} = \frac{1}{a(Y) - R(Y)_{0}^{*} + b(Y) \coth\{b(Y) S(Y)h\}}$$
(38)

$$R(Y)^* = \frac{1 - R(Y)_0^* [a(Y) - b(Y) \coth\{b(Y)S(Y)h\}]}{a(Y) - R(Y)_0^* + b(Y) \coth\{b(Y)S(Y)h\}}$$
(39)

A reflectance of 0,8 is assumed as $R(Y)_0^*$. So $R(Y)_B^* / R(Y)^*$ is with a contrast ratio of 0,98:

$$\frac{R(Y)_{B}^{*}}{R(Y)^{*}} = \frac{a(Y) - 0.8 + b(Y) \coth\{b(Y)S(Y)h_{0.98}\}}{[a(Y) + b(Y) \coth\{b(Y)S(Y)h_{0.98}\}][1 - 0.8 (a(Y) + b(Y) \coth\{b(Y)S(Y)h_{0.98}\})]} = 0.98 \quad (40)$$

this can be solved to

$$h_{0,98} = \frac{1}{b(Y)S(Y)} \operatorname{arccoth} \left(\frac{0,02 + \sqrt{V(Y)}}{1,568 \, b(Y)} \right)$$
 (41)

with

$$V(Y) = 3,136 \ a(Y) \left[1 - 0,98 \left\{ 1 - 0,8a(Y) \right\} \right] - 2,5084 \tag{42}$$

The equations above give a result of

$$D(Y) = \frac{b(Y)S(Y)}{\operatorname{arccoth}\left(\frac{0.02 + \sqrt{V(Y)}}{1.568 \ b(Y)}\right)}$$
(43)

a(Y), b(Y), and S(Y) have the same meaning as defined in Formulae 12 to 15.

7 Repeatability and reproducibility

Typically the choice of the correct sampling and the preparation of the test specimen have influences on the result of the measurement far superior to those of the calculation applied. It shall be ascertained by suitable measurements and checked by mathematical analysis (error propagation) that the parameter determined are valid.

8 Test report

The equations outlined in the text above shall be properly cited in the national and international standards in which they are used so that the influence on the test results can be investigated in case of interest.

Annex A

(normative)

Tables of coefficients for calculating a(ϕ) values (standard illuminant D65 and 10° standard observer)

The coefficients for different standard colour depths (SD) are given in $\underline{\text{Tables A.1}}$ to $\underline{\text{A.5}}$ for standard illuminant D65 and 10° standard observer.

Table A.1 — 1/1 SD

Range	φ_0	$a(\varphi_{\theta})$	К1	K ₂	К3
1	0,0	2,250	1,850 34	8,681 15	-11,632 8
2	60,0	3,973	1,512 13	-6,235 96	3,898 74
3	156,0	3,127	-1,218 51	5,390 38	-8,918 09
4	224,0	1,987	-4,006 96	-47,812 5	284,023
5	240,0	1,285	7,426 88	-17,554 7	8,955 08
6	268,0	2,185	0,822 426	0,741 241	-2,732 09
7	340,0	2,142	-1,032 000	8,056 27	-0,828 125

Table A.2 — 1/3 SD

Range	φ_0	$a(\varphi_{\theta})$	К1	K ₂	К3
1	0,0	2,040	1,801 64	9,156 25	-12,686 5
2	52,0	3,669	1,445 9	-3,590 46	2,000 06
3	140,0	3,524	1,218 93	-8,803 59	7,202 39
4	196,0	2,710	-0,562 195	-9,452 64	1,992 19
5	236,0	1,101	-4,187 35	16,971 7	118,672
6	252,0	1,351	7,984 62	-9,832 03	-14,277 3
7	276,0	2,504	1,549 35	-3,910 61	1,621 25
8	340,0	2,319	-2,578 89	-4,038 09	50,031 2

Table A.3 — 1/9 SD

Range	φ_0	$a(\varphi_{\theta})$	К1	K ₂	К3
1	0,0	2,345	-0,634 155	11,219 2	-7,883 79
2	52,0	3,94	2,405 70	-4,966 34	2,477 12
3	148,0	3,864	-1,289 06	1,005 37	-3,893 8
4	224,0	1,756	-4,939 51	-20,88 96	188,117
5	244,0	1,438	5,801 15	-1,049 80	-12,962 9
6	280,0	2,785	1,678 51	-3,350 52	1,463 81
7	336,0	2,932	-1,5271	-15,6045	49,1836

Table A.4 — 1/25 SD

Range	φ_0	$a(\varphi_{\theta})$	К1	K ₂	К3
1	0,0	2,36	-3,051 67	11,086 4	30,080 1
2	28,0	3,035	8,938 35	-15,294 9	-9,648 44
3	56,0	4,126 8	-0,280 82	5,083 5	-1,574 2
4	96,0	4,727 1	2,575 28	-6,646 51	2,610 05
5	148,0	4,636	-2,087 2	0,127 93	-3,271 97
6	224,0	1,687 3	-5,801	28,726 2	27,294 1
7	244,0	1,894 5	6,096 1	-8,308 59	2,313 48
8	292,0	3,162 2	0,668 99	-3,245 85	0,796 387

Table A.5 — 1/200 SD

Range	φ_0	$a(\varphi_{\theta})$	K ₁	K ₂	К3
1	0,0	5,68	-9,194 58	-19,978 5	95,984 4
2	28,0	3,646	-0,990 845	12,063	-1,349 61
3	80,0	6,203	14,131 8	-49,884 3	56,098 1
4	120,0	7,464	-1,578 55	1,258 79	-4,226 56
5	208,0	4,17	-8,990 36	23,008 8	15,734 4
6	232,0	3,555	4,269 04	215,078	-723,844
7	248,0	6,779	10,693 2	-40,940 4	58,806 6
8	280,0	7,935	-0,109 528	0,637 939	-5,004 52

Annex B

(normative)

Tables of coefficients for calculating $a(\phi)$ values (standard illuminant C and 2° standard observer)

The coefficients for different standard colour depths (SD) are given in $\underline{\text{Tables B.1}}$ to $\underline{\text{B.5}}$ for standard illuminant C and 2° standard observer.

Table B.1 — 1/1 SD

Range	$arphi_0$	$a(\varphi_0)$	К1	K ₂	К3
1	0,0	2,162 0	2,114 6	5,668 5	-7,691 4
2	56,000	3,773 0	2,298 2	-11,750	17,685
3	88,000	3,885 0	-1,404 7	0,860 05	-0,547 97
4	200,00	2,620 5	-0,712 65	-7,251 0	-6,423 8
5	228,00	1,711 0	-2,5648	-57,746	316,03
6	244,00	1,117 0	3,679 6	-4,184 4	1,542 6
7	328,00	2,170 0	-1,019 0	4,703 6	-18,645
8	344,00	2,051 0	-1,461 7	15,468	-12,263

Table B.2 — 1/3 SD

Range	φ_0	$a(\varphi_0)$	К1	K ₂	К3
1	0,0	1,971 0	1,885 4	7,213 9	-9,808 1
2	52,000	3,523 0	0,569 64	-0,973 66	0,380 87
3	156,00	3,491 0	-0,369 32	-5,514 2	1,481 5
4	188,00	2,856 0	-2,812 6	-2,376 0	11,254
5	216,00	2,130 0	-2,744 4	-25,405	62,615
6	252,00	0,771 00	-0,421 14	70,062	-182,87
7	276,00	2,177 0	2,798 3	-12,018	17,020
8	308,00	2,400 0	-0,492 71	3,156 1	-8,722 0
9	344,00	2,224 0	-2,955 8	-5,128 9	85,152

Table B.3 — 1/9 SD

Range	φ_0	$a(\varphi_{\theta})$	К1	K ₂	К3
1	0,0	2,338 0	-0,899 72	11,961	-10,490
2	48,000	3,502 0	5,248 4	-17,432	19,165
3	92,000	4,069 0	-0,364 96	0,647 10	-1,417 4
4	188,00	3,061 0	-1,781 9	-3,783 2	-4,893 6
5	224,00	1,701 0	-5,831 1	14,461	-12,941
6	244,00	1,010 0	4,6563	-0,212 40	-5,784 2
7	288,00	2,525 0	1,516 80	-1,577 2	-0,630 62
8	344,00	2,769 0	-0,853 58	-31,714	125,77

Table B.4 — 1/25 SD

Range	$arphi_0$	$a(\varphi_{\theta})$	К1	K ₂	К3
1	0,0	2,399 0	-3,0667	16,380	-10,999
2	24,000	2,454 0	6,050 7	19,039	-87,763
3	44,000	3,725 0	6,834 7	-38,741	69,481
4	72,000	4,126 0	-0,303 89	5,607 9	5,655 3
5	104,00	4,788 0	3,503 0	-17,579	20,218
6	144,00	4,671 0	-1,600 6	-3,757 8	2,903 8
7	196,00	3,231 0	-3,991 8	-3,584 0	-7,414 1
8	220,00	1,964 0	-8,679 8	27,377	-17,633
9	236,00	1,204 0	3,007 1	4,016 6	-7,156 2
10	296,00	2,908 0	0,416 89	-1,062 9	-1,298 5

 ${\rm Table~B.5-1/200~SD}$

Range	φ_0	$a(\varphi_0)$	К1	K ₂	К3
1	0,0	5,781 0	-8,228 8	-7,562 5	32,188
2	20,000	4,090 0	-6,295 0	27,716	-28,732
3	56,000	4,075 0	3,927 4	13,590	-14,148
4	88,000	6,260 0	6,753 7	-11,422	-22,258
5	104,00	6,957 0	2,353 2	-12,454	14,924
6	140,00	6,887 0	-2,557 2	4,140 1	-9,962 4
7	196,00	5,003 0	-4,135 0	-31,582	78,570
8	216,00	3,542 0	-4,123 0	16,913	24,602
9	232,00	3,416 0	0,285 16	121,20	-299,69
10	248,00	5,336 0	19,078	-110,38	311,44
11	264,00	6,839 0	4,345 8	-12,814	15,352
12	304,00	7,510 0	-1,007 3	1,254 4	-4,744 6
13	344,00	7,004 0	-5,101 1	-17,707	10,250

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