



Standard Practice for Factors and Procedures for Applying the MIL-STD-105 Plans in Life and Reliability Inspection¹

This standard is issued under the fixed designation E2555; the number immediately following the designation indicates the year of original adoption or, in the case of revision, the year of last revision. A number in parentheses indicates the year of last reapproval. A superscript epsilon (ϵ) indicates an editorial change since the last revision or reapproval.

1. Scope

1.1 This practice presents a procedure and related tables of factors for adapting Practice E2234 (equivalent to MIL-STD-105) sampling plans to acceptance sampling inspection when the item quality of interest is life length or reliability. Factors are provided for three alternative criteria for lot evaluation: mean life, hazard rate, and reliable life. Inspection of the sample is by attributes with testing truncated at the end of some prearranged period of time. The Weibull distribution, together with the exponential distribution as a special case, is used as the underlying statistical model.

1.2 A system of units is not specified by this practice.

1.3 *This standard does not purport to address all of the safety concerns, if any, associated with its use. It is the responsibility of the user of this standard to establish appropriate safety and health practices and determine the applicability of regulatory limitations prior to use.*

2. Referenced Documents

2.1 *ASTM Standards:*²

E456 Terminology Relating to Quality and Statistics

E2234 Practice for Sampling a Stream of Product by Attributes Indexed by AQL

2.2 *Other Documents:*

MIL-STD-105E Sampling Procedures and Tables for Inspection by Attributes³

3. Terminology

3.1 *Definitions:*

¹ This practice is under the jurisdiction of ASTM Committee E11 on Quality and Statistics and is the direct responsibility of Subcommittee E11.30 on Statistical Quality Control.

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² For referenced ASTM standards, visit the ASTM website, www.astm.org, or contact ASTM Customer Service at service@astm.org. For *Annual Book of ASTM Standards* volume information, refer to the standard's Document Summary page on the ASTM website.

³ MIL-STD-105E is also commonly referred to as "MIL-STD-105." It is virtually identical in content to its predecessor, MIL-STD-105D. These documents are out of print.

3.1.1 The terminology defined in Terminology E456 applies to this practice unless modified herein.

3.1.2 *acceptance quality level (AQL), n*—quality limit that is the worst tolerable process average when a continuing series of lots is submitted for acceptance sampling. E2234

3.1.2.1 *Discussion*—This term is often referred to as the "acceptance quality limit."

3.1.2.2 *Discussion*—This definition supersedes that given in MIL-STD-105E.

3.1.2.3 *Discussion*—A sampling plan and an AQL are chosen in accordance with the risk assumed. Use of a value of AQL for a certain defect or group of defects indicates that the sampling plan will accept the great majority of the lots or batches provided the process average level of percent defective (or defects per hundred units) in these lots or batches are no greater than the designated value of AQL. Thus, the AQL is a designated value of percent defective (or defects per hundred units) for which lots will be accepted most of the time by the sampling procedure being used. The sampling plans provided herein are so arranged that the probability of acceptance at the designated AQL value depends upon the sample size, being generally higher for large samples than for small ones, for a given AQL. The AQL alone does not identify the chances of accepting or rejecting individual lots or batches but more directly relates to what might be expected from a series of lots or batches, provided the steps indicated in this refer to the operating characteristic curve of the plan to determine the relative risks.

3.1.3 *consumer's risk, n*—probability that a lot having specified rejectable quality level will be accepted under a defined sampling plan.

3.1.4 *double sampling plan, n*—a multiple sampling plan in which up to two samplings can be taken and evaluated to accept or reject a lot.

3.1.5 *limiting quality level (LQL), n*—quality level having a specified consumer's risk for a given sampling plan.

3.1.6 *lot, n*—a definite quantity of a product or material accumulated under conditions that are considered uniform for sampling purposes.

3.1.6.1 *Discussion*—The lot for sampling may differ from a collection of units designated as a batch for other purposes, for example, production, shipment, and so forth.

3.1.7 *multiple sampling plan, n*—a sampling plan in which successive samples from a lot are drawn and after each sample is inspected a decision is made to accept the lot, reject the lot, or to take another sample, based on quality level of the combined samples.

3.1.7.1 *Discussion*—When the quality is much less or much more than the AQL, the decision can be made on the first sample, which is smaller than that of a single sampling plan with equivalent acceptance quality level. For samples that are close to the AQL in quality, additional samples are required and the total sample size will be larger than the corresponding single sampling plan.

3.1.8 *sample, n*—group of items, observations, test results, or portions of material taken from a large collection of items, observations, test results, or quantities of material that serves to provide information that may be used as a basis for making a decision concerning the larger collection. **E2234**

3.2 *Definitions of Terms Specific to This Standard:*

3.2.1 *acceptance number, n*—the maximum number of failed items allowed in the sample for the lot to be accepted using a single or multiple sampling plan.

3.2.2 *hazard rate, n*—differential fraction of items failing at time *t* among those surviving up to time *t*, symbolized by *h(t)*.

3.2.2.1 *Discussion*—*h(t)* is also referred to as the instantaneous failure rate at time *t*. It is related to the probability density and cumulative distribution functions by $h(t) = f(t) / (1 - F(t))$.

3.2.3 *mean life, n*—average time that items in the lot or population are expected to operate before failure.

3.2.3.1 *Discussion*—This metric is often referred to as mean time to failure (MTTF) or mean time before failure (MTBF).

3.2.4 *rejection number, n*—the minimum number of failed items in the sample that will cause the lot to be rejected under a given sampling plan.

3.2.5 *reliable life (ρ_r), n*—life beyond which some specified proportion, *r*, of the items in the lot or population will survive.

3.2.6 *test truncation time (t), n*—amount of time sampled items are allowed to be tested.

3.2.7 *Weibull distribution, n*—probability distribution having cumulative distribution:

$$\text{function } F(t) = 1 - \exp\left(-\left(\frac{t - \gamma}{\eta}\right)^\beta\right), t > \gamma \text{ and probability density}$$

$$\text{function } f(t) = \frac{\beta}{\eta} \left(\frac{t - \gamma}{\eta}\right)^{\beta-1} \exp\left(-\left(\frac{t - \gamma}{\eta}\right)^\beta\right)$$

3.2.7.1 *Discussion*—The Weibull distribution is widely used for modeling product life. It can take a wide variety of shapes and also the characteristics of other types of distributions based on the value of its parameters. γ is called the location, minimum life, or threshold parameter and defines the lower limit of the distribution (Fig. 1). η is called the scale or characteristic life parameter and is equal to the 63.2 percentile of the distribution, minus γ (Fig. 2). β is the shape parameter (Fig. 3). The exponential distribution is the special case where $\gamma = 0$ and $\beta = 1$.

4. Significance and Use

4.1 The procedure and tables presented in this practice are based on the use of the Weibull distribution in acceptance sampling inspection. Details of this work, together with tables

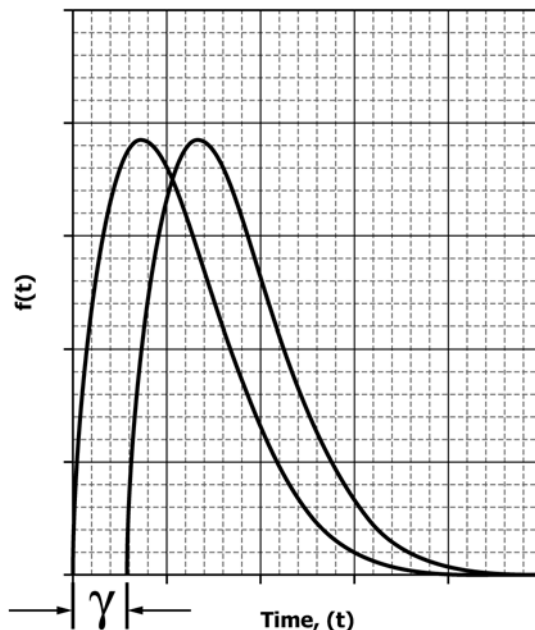


FIG. 1 Effect of the Parameter γ on the Weibull Probability Density Function, $f(t)$

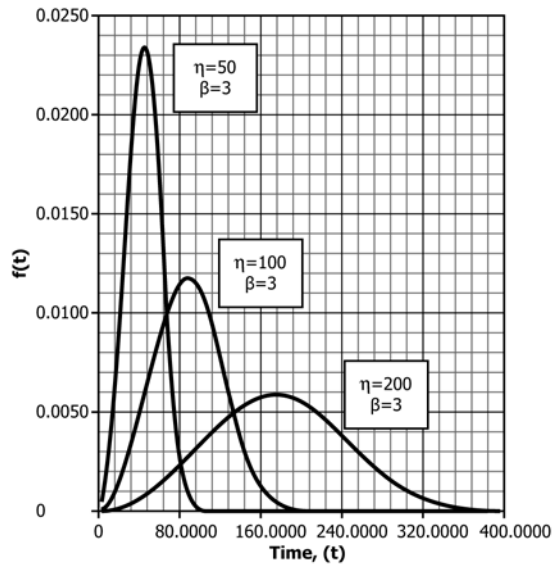


FIG. 2 Effect of the Parameter η on the Weibull Probability Density Function, $f(t)$

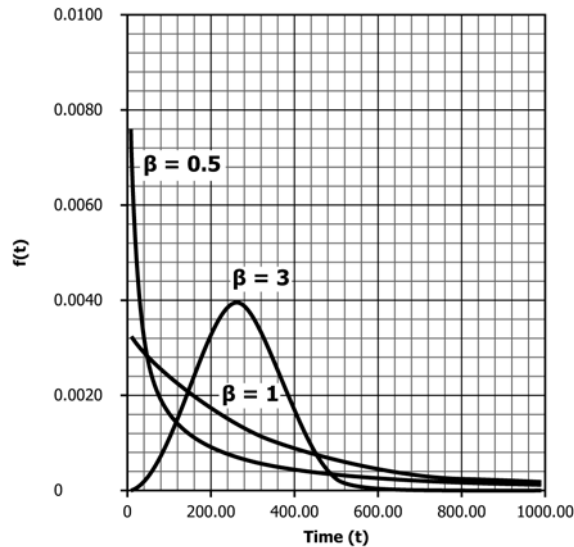


FIG. 3 Effect of the Parameter β on the Weibull Probability Density Function, $f(t)$

of sampling plans of other forms, have been published previously. See Refs (1-3).⁴ Since the basic computations required have already been made, it has been quite easy to provide these new factors. No changes in method or details of application have been made over those described in the publications referenced above. For this reason, the text portion of this report has been briefly written. Readers interested in further details are referred to these previous publications. Other sources of material on the underlying theory and approach are also available (4-7).

⁴ The boldface numbers in parentheses refer to the list of references at the end of this standard.

4.2 The procedure to be used is essentially the same as the one normally used for attribute sampling inspection. The only difference is that sample items are tested for life or survival instead of for some other property. For single sampling, the following are the required steps:

4.2.1 Using the tables of factors provided in Annex A1, select a suitable sampling inspection plan from those tabulated in Practice E2234.

4.2.2 Draw at random a sample of items of the size specified by the selected Practice E2234 plan.

4.2.3 Place the sample of items on life test for the specified period of time, t .

4.2.4 Determine the number of sample items that failed during the test period.

4.2.5 Compare the number of items that failed with the number allowed under the selected Practice E2234 plan.

4.2.6 If the number that failed is equal to or less than the acceptable number, accept the lot; if the number failing exceeds the acceptable number, reject the lot.

4.3 Both the sample sizes and the acceptance numbers used are those specified by Practice E2234 plans. It will be assumed in the section on examples that single sampling plans will be used. However, the matching double sampling and multiple sampling plans provided in MIL-STD-105 can be used if desired. The corresponding sample sizes and acceptance and rejection numbers are used in the usual way. The specified test truncation time, t , must be used for all samples.

4.4 The probability of acceptance for a lot under this procedure depends only on the probability of a sample item failing before the end of the test truncation time, t . For this reason, the actual life at failure need not be determined; only the number of items failing is of interest. Life requirements and test time specifications need not necessarily be measured in chronological terms such as minutes or hours. For example, the life measure may be cycles of operation, revolutions, or miles of travel.

4.5 The underlying life distribution assumed in this standard is the Weibull distribution (note that the exponential distribution is a special case of the Weibull). The Weibull model has three parameters. One parameter is a scale or characteristic life parameter. For these plans and procedures, the value for this parameter need not be known; the techniques used are independent of its magnitude. A second parameter is a location or “guaranteed life” parameter. In these plans and procedures, it is assumed that this parameter has a value of zero and that there is some risk of item failure right from the start of life. If this is not the case for some applications, a simple modification in procedure is available. The third parameter, and the one of importance, is the shape parameter, β .⁵ The magnitude of the conversion factors used in the procedures described in this report depends directly on the value for this parameter. For this reason, the magnitude of the parameter shall be known through experience with the product or shall be estimated from past research, engineering, or inspection data. Estimation procedures are available and are outlined in Ref (1).

4.6 For the common case of random chance failures with the failure rate constant over time, rather than failures as a result of “infant mortality” or wearout, a value of 1 for the shape parameter shall be assumed. With this parameter value, the Weibull distribution reduces to the exponential. Tables of conversion factors are provided in Annex A1 for 15 selected shape parameter values ranging from $\frac{1}{2}$ to 10, the range commonly encountered in industrial and technical practice. The value 1, used for the exponential case, is included. Factors for other required shape parameter values within this range may be obtained approximately by interpolation. A more complete discussion of the relationship between failure patterns and the Weibull parameters can be found in Refs (1-3).

⁵ In some disciplines, the Weibull shape β parameter is referred to as the “Weibull slope.”

4.7 One possible acceptance criterion is the mean life for items making up the lot (μ). Mean life conversion factors or values for the dimensionless ratio $100t/\mu$ have been determined to correspond to or replace all the p' or percent defective values associated with Practice E2234 plans. In this factor, t represents the specified test truncation time and μ the mean item life for the lot. For reliability or life-length applications, these factors are used in place of the corresponding p' values normally used in the use of Practice E2234 plans for attribute inspection of other item qualities. The use of these factors will be demonstrated by several examples (see Sections 5, 7, and 9).

4.8 Annex Table 1A lists, for each selected shape parameter value, $100t/\mu$ ratios for each of the Practice E2234 AQL [p' (%)] values. With acceptance inspection plans selected in terms of these ratios, the probability of acceptance will be high for lots whose mean life meets the specified requirement. The actual probability of acceptance will vary from plan to plan and may be read from the associated operating characteristic curves supplied in MIL-STD-105. The curves are entered by using the corresponding p' (%) value. Annex Table 1B lists $100t/\mu$ ratios at the LQL for the quality level at which the consumer’s risk is 0.10. Annex Table 1C lists corresponding $100t/\mu$ ratios for a consumer’s risk of 0.05.

4.8.1 These ratios are to be used directly for the usual case for which the value for the Weibull location or threshold parameter (γ) can be assumed as zero. If γ is not zero but has some other known value, all that shall be done is to subtract the value for γ from t to get t_0 and from m to get m_0 . These transformed values, t_0 and m_0 , are then employed in the use of the tables and for all other computations. A solution in terms of m_0 and t_0 can then be converted back to actual or absolute values by adding the value for γ to each.

5. Examples, Mean Life Ratio

5.1 A Practice E2234 acceptance sampling inspection plan is to be applied to incoming lots of product for which the mean item life is the property of interest. An acceptable mean life of 2000 h has been specified, and under the plan, used lots with a mean life of this value or greater shall have a high probability of acceptance. A testing truncation time of $t = 250$ h has been specified. From past experience it has been determined that the Weibull distribution can be used as a life-length model and a shape parameter value of 2.5 and a location or threshold parameter value of 0 can be assumed. Single sampling is to be used. A sample of as many as 300 items or so can be tested at one time. An appropriate sampling inspection plan shall be selected. Also, the consumer’s risk under use of the selected plan shall be determined.

5.1.1 Computation of the $100t/\mu$ ratio at the AQL gives $100t/\mu = 100 \times 250/2000 = 12.5$. Examination of the ratios in the column for a shape parameter of 2.5 in Annex Table 1A discloses a value of 12.4 for an AQL of 0.40 in p' (%) terms. A plan with this AQL is accordingly to be used. Reference now to Practice E2234 indicates for Sample Size Code Letter M the sample size is 315; this value will accordingly be used. Examination of the Master Table for Normal Inspection (Single Sampling) in Practice E2234 shows for Sample Size Code

Letter M and an AQL of 0.40, the acceptance number must be 3 and the rejection number 4.

5.1.2 The acceptance procedure will thus be to draw at random a sample of 315 items and submit them to life test for 250 h. At the end of that time, the number that has failed will be determined. If three items or less have failed, the lot will be accepted; if four or more have failed, it will be rejected.

5.1.3 The consumer's risk at a probability level of 0.10 can be determined by use of Annex Table 1B which gives $100t/\mu$ ratios at the LQL for the 0.10 risk value. For a shape parameter value of 2.5, a Sample Size Code Letter M, and an AQL of 0.40, the $100t/\mu$ ratio value is found to be 24. With $t = 250$, $100t/\mu = 24$ or $100 \times 250/\mu = 24$ which gives a value for μ of 1040. Thus, if the mean life for the items in the lot is 1040 h or less, the probability of acceptance will be 0.10 or less. If the lot quality for which the consumer's risk was 0.05 was desired instead, Annex Table 1C might be used which gives ratios at the LQL for this risk value.

5.2 A Practice E2234 plan with Sample Size Code Letter F and an AQL of 4.0 has been specified for a product for which life length in terms of cycles of operation is the quality of interest. Acceptance is to be in terms of a mean life evaluation. The Weibull distribution can be assumed to apply with a shape parameter value and a location parameter value of 0. Testing of sample items is to be truncated at 5000 cycles. The operating characteristics in terms of mean life for this plan are required.

5.2.1 Annex Table 1A lists ratios of $100t/\mu$ at selected AQLs and gives a $100t/\mu$ value of 0.62 for an AQL of 4.0 and a shape parameter value of $\frac{2}{3}$. With $t = 5000$, $100t/\mu = 0.62$ or $100 \times 5000/\mu = 0.62$ which gives $\mu = 810\,000$. Therefore, if the mean item life for the lot is 810 000 or more, the probability of acceptance will be high. Annex Table 1C gives ratios $100t/\mu$ at the LQL for a consumer's risk of 0.05 and provides a $100t/\mu$ value of 14 for Code Letter F, an AQL of 4.0, and a shape parameter value of $\frac{2}{3}$. Thus, $100 \times 5000/\mu = 14$ or $\mu = 36\,000$. If the mean item life for the lot is 36 000 cycles or less, the probability of acceptance will be 0.05 or less.

5.2.2 The sample size and acceptance number will be those specified by Practice E2234 for Code Letter F and an AQL of 4.0. For single sampling, the sample size will be 20 items and the acceptance number 2. For this example, as in all cases, the matched Practice E2234 double sampling and multiple sampling plans may be used instead. No additional changes in procedure are required. The specified test time, which in this case is 5000 cycles, shall be used for all samples.

5.3 Assume the Weibull distribution applies with a shape parameter value of $\beta = 3.33$ and a location or threshold parameter value, γ , of 3000 h. A Practice E2234 acceptance-inspection plan shall be selected under which the probability of acceptance will be low (0.05 or less) if mean item life is 8000 h or less. The sample size will be kept large to reduce the testing period time but it cannot exceed 250 items. To reduce further testing time, an acceptance number of 0 will be used. The required test truncation time must be determined; also, the AQL.

5.3.1 Reference to Practice E2234 indicates the Code Letter L with a sample size of 200 items shall be used. With this code letter and an acceptance number of 0, the AQL in Practice

E2234 terms must be 0.065. Subtraction of the threshold parameter value, γ , of 3000 h from the required mean value, μ , of 8000 h gives as a converted value for the mean $\mu_0 = 8000 - 3000 = 5000$ h. This converted value must now be used in working with the tables of factors. Use of Annex Table 1C for $\beta = 3\frac{1}{3}$ Code Letter L, and an AQL of 0.065 gives a $100t/\mu$ value of 31 at the LQL (for $P(A) = 0.05$). With $\mu_0 = 5000$, $100t_0/\mu_0 = 100 t_0/5000 = 31$ or $t_0 = 1550$ h. Conversion of this to absolute terms gives $t = t_0 + \gamma = 1550 + 3000 = 4550$ h as the required test truncation time.

5.3.2 From Annex Table 1A, the corresponding ratio at the AQL may be found. For an AQL of 0.065 and $b = 3\frac{1}{3}$ it is 12.3. Thus, $100 t_0/\mu_0 = 12.3$ or $100 \times 1550/\mu_0 = 12.3$ or $\mu_0 = 12\,600$. Converting this to absolute terms gives $\mu = \mu_0 + \gamma = 12\,600 + 3000 = 15\,600$. Thus, the mean item life for a lot shall be 15 600 h or more for its probability of acceptance to be high.

6. Hazard Rate Conversion Factors

6.1 Another measure of lot quality is the hazard rate or instantaneous failure rate, $h(t)$, at some specified period of time, t . Hazard rate conversion factors or values for the dimensionless product $100t\{h(t)\}$ have been determined for all of the p' values that characterize the collection of Practice E2234 plans. As for the mean life plans, these products may be used in place of the corresponding p' values when using the Practice E2234 plans for life-length and reliability applications.

6.2 Annex Table 2A lists for each selected value for the shape parameter $100t\{h(t)\}$ products for each Practice E2234 AQL value. Annex Table 2B lists corresponding $100t\{h(t)\}$ products at the LQL for a consumer's risk of 0.10. Annex Table 2C lists products at the LQL for a consumer's risk of 0.05. Use of these tables of factors is similar to the method of use for the mean life ratios including the variation in method required when some nonzero value for the location or threshold parameter shall be assumed.

6.2.1 Note one point of difference. The products are for direct application only in cases in which the time t at which the hazard rate is specified or is to be evaluated is the same as the time t at which the life testing of sample items is to be truncated. However, a table of hazard rate ratios has been prepared, Annex Table 2D, to use in a simple modification of method that allows the test truncation time to differ from the time at which the hazard rate is specified. All that shall be done is to determine the hazard rate at the test truncation time which corresponds to the hazard rate at the specification time. Annex Table 2D provides ratios for making this conversion. It gives for various values of t_2/t_1 the corresponding values for the ratio $h(t_2)/h(t_1)$ for all the shape parameter values for which conversion values have been provided. If the test truncation time is shorter than the time for hazard rate specification, t_1 is used to represent the test truncation time and $h(t_1)$ the corresponding hazard rate at that time. In this case, t_2 represents the time of hazard rate specification and $h(t_2)$ the specified hazard rate. If the test truncation is longer instead, the meanings given Subscripts 1 and 2 are simply reversed.

7. Examples, Hazard Rate

7.1 An acceptance-inspection plan shall be selected from the Practice E2234 collection for an application for which the Weibull distribution applies and for which it may be assumed the shape parameter value is 1.67 and the location parameter value is 0. A hazard rate of no more than 0.0005/h at 1000 h of life can be tolerated so a plan under which the probability of acceptance will be low (0.10) if this rate will be exceeded at this life is required. The test truncation time is likewise to be 1000 h.

7.1.1 Computation of the $100t\{h(t)\}$ product gives $100 \times 1000 \times 0.0005 = 50$. Thus, a plan shall be used for which this product is found at the LQL for which the consumer's risk is 0.10. Examination of the column for $\beta = 1.67$ in Annex Table 2B discloses several close possibilities. One is for a plan with Code Letter D and an AQL of 1.5 for which the product is 48; another is Code Letter F and an AQL of 4.0 for which the product is likewise 48; still another is Code Letter G and an AQL of 6.5 for which the product is 53. Any of these will provide fairly closely the required consumer's protection.

7.1.2 The last plan mentioned with its relatively large sample size and acceptance number will discriminate most sharply between good and bad lots and hence provide the most reasonable AQL. This will be achieved at the expense of a relatively large number of item hours of inspection, of course. With this choice (Code Letter G and an AQL of 6.5) the AQL can be easily determined. Reference to Annex Table 2A gives a value for $100t\{h(t)\}$ of 11.2 for an AQL of 6.5. Thus, $100 \times 1000 h(t) = 11.2$ or $h(t) = 0.000 112$ at $t = 1000$; the "acceptable" hazard rate is therefore 0.000 112 (per hour). If, alternatively, Code Letter D and an AQL of 1.5 had been used, the "acceptable" hazard rate would be 0.000 025 2 (per hour) instead.

7.2 Suppose the selected sampling plan must have an acceptable hazard rate (a rate for which the probability of acceptance is high) of 0.0001 per hour at 500 h of life. However, the testing of sample items shall be truncated at 200 h. A value of $\beta = 0.67$ and a location parameter of 0 can be assumed. A Practice E2234 plan shall be selected.

7.2.1 In this case, use Annex Table 2D. Letting $t_2 = 500$ and $t_1 = 200$, $t_2/t_1 = 500/200 = 2.5$. Referencing Annex Table 2D with this ratio using the value $\beta = 0.67$ column shows $h(t_2)/h(t_1)$ to be 0.734. With $h(t_2) = 0.0001$, $0.0001/h(t_1) = 0.734$ or $h(t_1) = 0.000 136$. This failure rate number shall be used in selecting the plan. Thus, $100t\{h(t)\} = 100 \times 200 \times 0.000 136 = 2.72$ (note that the testing truncation time of 200 h is used as t at this point). Referencing Annex Table 2A examining the column for $\beta = 0.67$ shows that a Practice E2234 plan with an AQL of 4.0 % precisely meets this need.

8. Reliable Life Conversion Factors

8.1 A third possible reliability and life-length measure for the items in a lot or population is reliable life (ρ). Reliable life can be defined as the life beyond which some specified proportion of the items in the lot or population will survive. The letter r represents this specified proportion.

8.1.1 Tables of conversion factors have been prepared for two different proportions, $r = 0.90$ and $r = 0.99$. As for the

mean life case, these reliable life conversion factors have been prepared in the form of values for the dimensionless ratio $100t/\rho$. Ratio values have been determined for all the p '(%) values associated with Practice E2234 plans. Annex Table 3A gives $100t/\rho$ values at each of the AQLs for $r = 0.90$; Annex Table 4A gives corresponding values for $r = 0.99$. Annex Table 3B gives ratio values at the LQL for a consumer's risk of 0.10 for $r = 0.90$; Annex Table 4B gives corresponding values for a consumer's risk of 0.10 and $r = 0.99$. Annex Table 3C gives ratio values at the LQL for a consumer's risk of 0.05 and $r = 0.90$; Annex Table 4C gives similar ratio values at a consumer's risk of 0.05 and $r = 0.99$. These conversion ratios are used in the same manner in which mean life ratios are used, including the manner for application when the location parameter is not zero. See Section 9 for an example.

9. Examples, Reliable Life

9.1 A sampling inspection plan shall be selected for a product for which item life in terms of feet of travel is the quality of interest. Experience indicates the Weibull distribution will serve well as a statistical model with a shape parameter value of approximately $1\frac{1}{3}$ and a location parameter of 0. A lot will be considered "acceptable" if the reliable life is 40 000 ft and the probability of acceptance for such lots shall be high. For lots in which reliable life is 10 000 ft or less, the probability of acceptance shall be low, namely 0.05 or less. Reliable life is defined as the life beyond which 90 % of the items will survive; that is, r is to be 0.90. Testing of sample items is to be truncated at 5000 ft.

9.1.1 At the AQL, the $100t/\rho$ factor is $100 \times 5000/40 000 = 12.5$. Examination of Annex Table 3A shows that for $\beta = 1\frac{1}{3}$ the $100t/\rho$ ratio for an AQL of 0.65 is 12.4 which is quite close to the desired ratio. Accordingly, a plan with this AQL is to be adopted. At the unacceptable or LQL, the $100t/\rho_r$ factor is $100 \times 5000/10 000 = 50$. Referencing Annex Table 3C, which gives ratios at the LQL for $P(A) = 0.05$, shows that, for Code Letter L, an AQL of 0.65 (which is required for this application, as indicated above) and $\beta = 1\frac{1}{3}$ the corresponding ratio is 48, which is close to the desired value of 50. Thus, a Practice E2234 plan with Code Letter L and an AQL of 0.65 will meet the specified operating requirements. For single sampling, Practice E2234 shows the sample size to be 200 items and the acceptance number 3.

10. Summary

10.1 This practice preserves the structure of TR-7 for use in applications in which that standard is prescribed or its use is desirable.

10.2 This practice provides tables and procedures for applying three different measures of reliability in which testing is performed without replacement.

10.2.1 *Mean Life*, μ —The expected life of the product.

10.2.2 *Hazard Rate*, $h(t)$ —The instantaneous failure rate at some specified time, t .

10.2.3 *Reliable Life*, ρ_r —The life ρ beyond which some specified proportion r of the items in the population will survive.

10.3 *Procedure for Application*:

10.3.1 Using the tables of factors provided in **Annex A1**, select a suitable sampling inspection plan from those tabulated in Practice **E2234** for normal inspection.

10.3.2 Draw at random a sample of items of the size specified by the selected Practice **E2234** plan.

10.3.3 Place the sample of items on life test for the specified period of time, t .

10.3.4 Determine the number of sample items that failed during the test period.

10.3.5 Compare the number of items that failed with the number allowed under the selected Practice **E2234** plan.

10.3.6 If the number that failed is equal to or less than the acceptance number, accept the lot; if the number failing exceeds the acceptance number, reject the lot.

10.4 Selection—Mean Life:

10.4.1 Specify:

10.4.1.1 Acceptable mean life, μ_0 .

10.4.1.2 Unacceptable mean life, μ_1 .

10.4.1.3 Test truncation time, t .

10.4.1.4 Weibull shape parameter, β .

10.4.2 Compute the dimensionless ratio $100t/\mu_0$ from the specified μ_0 and t and enter Annex Table 1A under β . Locate the nearest value of $100t/\mu_0$ to that calculated and read the corresponding AQL.

10.4.3 Compute the dimensionless ratio $100t/\mu_1$ from the specified μ_1 and t and enter Annex Table 1B under β . Locate

the nearest value of $100t/\mu_1$ corresponding to the AQL obtained in 10.4.2 and read the sample size code letter (use Annex Table 1C if a limiting quality with 5 % probability of acceptance is desired).

10.4.4 Obtain the sample size and acceptance number for the test from the Practice **E2234** normal inspection plan.

10.4.5 Mean Life Example:

10.4.5.1 Suppose $\mu_0 = 50$, $\mu_1 = 10$, $t = 5$, $\beta = 1$, then $100t/\mu_0 = 10$ giving an AQL of 10 from Annex Table 1A and $100t/\mu_1 = 50$ giving Code F from Table 1B.

10.4.5.2 Practice **E2234** gives sample size 20. Accept on 5 for Code F, AQL = 10.

10.5 Selection—Hazard Rate or Reliable Life:

10.5.1 The selection of plans for a specified hazard rate or reliable life follows the procedure for mean life described in 10.4 using appropriate dimensionless ratios and the associated tables from **Annex A1**.

10.5.2 Hazard rate uses the product $100t\{h(t)\}$ with the **Annex A1** tables of Section B.

10.5.3 Reliable life uses the dimensionless ratio $100t/\rho$ with the **Annex A1** tables of Section C.

11. Keywords

11.1 exponential distribution; hazard rate; mean life; MIL-STD-105; reliability; reliable life; Weibull distribution

ANNEX

(Mandatory Information)

A1. TABLES OF CONVERSION FACTORS

TABLE 1A

100t/μ Ratios at the Acceptable Quality Level (normal inspection)
for the ASTM **E2234** Plans

NOTE—These plans assume the characteristic being measured has a Weibull distribution.

NOTE—Where scientific notation is used (that is, E-x), the decimal point is moved to the left x places (for example, if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

AQL p' (%)	Shape Parameter, β														
	0.333	0.500	0.667	1.000	1.333	1.500	1.667	2.000	2.500	3.000	3.333	3.500	4.000	5.000	10.000
0.010	1.67E-11	5.00E-07	7.52E-05	1.00E-02	0.109	0.239	0.446	1.128	2.831	5.198	7.031	7.999	11.033	17.262	41.847
0.015	5.63E-11	1.13E-06	1.38E-04	1.50E-02	0.147	0.313	0.568	1.382	3.330	5.950	7.940	8.981	12.210	18.720	43.578
0.025	2.61E-10	3.13E-06	2.97E-04	2.50E-02	0.216	0.440	0.772	1.784	4.085	7.055	9.255	10.393	13.873	20.734	45.863
0.040	1.07E-09	8.00E-06	6.02E-04	4.00E-02	0.308	0.601	1.024	2.257	4.930	8.252	10.657	11.887	15.603	22.778	48.070
0.065	4.58E-09	2.11E-05	1.25E-03	6.50E-02	0.443	0.831	1.370	2.877	5.986	9.702	12.328	13.656	17.617	25.101	50.462
0.100	1.67E-08	5.01E-05	2.38E-03	0.100	0.612	1.108	1.774	3.569	7.113	11.200	14.030	15.445	19.622	27.360	52.684
0.150	5.64E-08	1.13E-04	4.38E-03	0.150	0.830	1.452	2.263	4.372	8.366	12.822	15.845	17.344	21.716	29.673	54.866
0.250	2.61E-07	3.13E-04	9.42E-03	0.250	1.218	2.042	3.076	5.645	10.265	15.205	18.472	20.072	24.677	32.868	57.744
0.400	1.07E-06	8.03E-04	1.91E-02	0.401	1.733	2.795	4.080	7.144	12.391	17.788	21.274	22.962	27.759	36.113	60.527
0.650	4.62E-06	2.13E-03	3.96E-02	0.652	2.497	3.867	5.464	9.112	15.055	20.922	24.619	26.388	31.352	39.806	63.547
1.000	1.69E-05	5.05E-03	7.58E-02	1.005	3.454	5.159	7.083	11.312	17.899	24.167	28.031	29.859	34.932	43.402	66.356
1.500	5.75E-05	1.14E-02	0.140	1.511	4.690	6.771	9.047	13.872	21.071	27.687	31.680	33.551	38.683	47.092	69.119
2.500	2.70E-04	3.20E-02	0.303	2.532	6.906	9.551	12.330	17.954	25.901	32.883	36.983	38.879	44.008	52.211	72.778
4.000	1.13E-03	8.33E-02	0.620	4.082	9.882	13.133	16.422	22.798	31.355	38.559	42.682	44.565	49.591	57.446	76.339
6.500	5.06E-03	0.226	1.311	6.721	14.362	18.311	22.149	29.253	38.275	45.530	49.569	51.388	56.174	63.469	80.242

TABLE 1A

100/ μ Ratios at the Acceptable Quality Level (normal inspection)
for the ASTM E2234 Plans

NOTE—These plans assume the characteristic being measured has a Weibull distribution.

NOTE—Where scientific notation is used (that is, E-x), the decimal point is moved to the left x places (for example, if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

AQL p' (%)	Shape Parameter, β														
	0.333	0.500	0.667	1.000	1.333	1.500	1.667	2.000	2.500	3.000	3.333	3.500	4.000	5.000	10.000
10.000	1.95E-02	0.555	2.573	10.536	20.122	24.711	29.007	36.626	45.816	52.891	56.726	58.431	62.856	69.441	83.932

TABLE 1B

100/ μ Ratios at the Limiting Quality Level
for the ASTM E2234 Plans, Consumer's Risk = 0.10

NOTE—These plans assume the characteristic being measured has a Weibull distribution.

NOTE—Where scientific notation is used (that is, E-x), the decimal point is moved to the left x places (for example, if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

Code Letter	AQL (p%)	Shape Parameter, β														
		0.333	0.50	0.667	1.000	1.333	1.500	1.667	2.000	2.500	3.000	3.333	3.500	4.000	5.000	10.000
A	6.500	25.433	66.274	92.927	115.129	120.933	121.682	121.789	121.073	119.240	117.369	116.235	115.707	114.281	112.025	106.605
B	4.000	7.536	29.455	50.583	76.753	89.223	92.861	95.489	98.856	101.388	102.531	102.922	103.050	103.265	103.299	102.369
C	2.500	1.628	10.604	23.509	46.052	60.826	66.059	70.282	76.573	82.650	86.478	88.298	89.056	90.885	93.267	97.271
C	10.000	11.235	38.440	61.762	87.681	98.590	101.478	103.429	105.659	106.932	107.183	107.115	107.045	106.759	106.086	103.741
D	1.500	0.397	4.142	11.616	28.782	42.756	48.289	53.012	60.537	68.485	73.938	76.686	77.865	80.809	84.899	92.805
D	6.500	2.361	13.587	28.313	52.129	66.752	71.750	75.709	81.469	86.852	90.126	91.644	92.267	93.745	95.608	98.484
D	10.000	7.688	29.850	51.091	77.265	89.669	93.274	95.871	99.185	101.658	102.759	103.128	103.247	103.437	103.437	102.437
E	1.000	9.26E-02	1.569	5.608	17.712	29.707	34.937	39.615	47.489	56.397	62.890	66.292	67.780	71.573	77.043	88.407
E	4.000	0.505	4.859	13.094	31.175	45.395	50.930	55.614	63.003	70.708	75.933	78.546	79.662	82.439	86.266	93.549
E	6.500	1.478	9.943	22.401	44.594	59.376	64.657	68.939	75.352	81.594	85.556	87.450	88.241	90.157	92.669	96.959
E	10.000	3.379	17.255	33.871	58.746	73.011	77.700	81.336	86.486	91.104	93.789	94.989	95.471	96.588	97.920	99.668
F	0.650	2.54E-02	0.663	2.939	11.513	21.505	26.215	30.592	38.287	47.470	54.478	58.255	59.930	64.265	70.683	84.679
F	2.500	0.133	1.992	6.709	19.962	32.495	37.836	42.562	50.415	59.160	65.448	68.714	70.136	73.745	78.908	89.471
F	4.000	0.369	3.940	11.189	28.073	41.963	47.492	52.224	59.786	67.805	73.325	76.114	77.312	80.306	84.476	92.574
F	6.500	0.795	6.577	16.430	36.267	50.850	56.335	60.899	67.954	75.120	79.860	82.193	83.182	85.617	88.916	94.975
F	10.000	2.566	14.362	29.516	53.596	68.156	73.089	76.980	82.608	87.821	90.964	92.410	93.001	94.938	96.140	98.758
G	0.400	6.21E-03	0.259	1.452	7.196	15.117	19.164	23.075	30.268	39.334	46.578	50.594	52.399	57.141	64.341	80.792
G	1.500	3.14E-02	0.763	3.266	12.352	22.670	27.474	31.911	39.657	48.825	55.770	59.498	61.147	65.405	71.684	85.277
G	2.500	8.46E-02	1.476	5.358	17.183	29.038	34.237	38.900	46.773	55.716	62.257	65.691	67.194	71.032	76.576	88.139
G	4.000	0.176	2.407	7.730	21.939	34.879	40.294	45.043	52.852	61.437	67.540	70.688	72.053	75.506	80.412	90.319
G	6.500	0.524	4.981	13.339	31.563	45.818	51.351	56.028	63.393	71.059	76.246	78.837	79.944	82.694	86.479	93.665
G	10.000	1.201	8.658	20.194	41.613	56.374	61.743	66.136	72.790	79.367	83.606	85.654	86.514	88.611	91.395	96.290
H	0.250	1.63E-03	0.106	0.743	4.605	10.817	14.232	17.654	24.215	32.904	40.140	44.254	46.126	51.108	58.847	77.265
H	1.000	8.09E-03	0.309	1.657	7.859	16.150	20.324	24.329	31.633	40.747	47.967	51.950	53.737	58.414	65.486	81.507
H	1.500	2.14E-02	0.590	2.694	10.865	20.592	25.223	29.548	37.194	46.384	53.437	57.252	58.947	63.342	69.869	84.191
H	2.500	4.36E-02	0.950	3.849	13.783	24.613	29.558	34.081	41.892	51.014	57.846	61.487	63.093	67.223	73.274	86.217
H	4.000	0.125	1.912	6.505	19.555	31.996	37.320	42.039	49.898	58.675	65.000	68.290	69.724	73.366	78.583	89.286
H	6.500	0.273	3.222	9.621	25.385	38.912	44.411	49.164	56.852	65.130	70.906	73.850	75.121	78.311	82.793	91.647
H	10.000	0.680	5.928	15.199	34.432	48.908	54.418	59.030	66.212	73.575	78.490	80.922	81.956	84.512	87.997	94.483
J	0.150	3.97E-04	1.4E-02	0.367	2.878	7.603	10.404	13.316	19.143	27.264	34.319	38.434	40.330	45.442	53.568	73.718
J	0.650	1.95E-03	0.120	0.814	4.893	11.320	14.819	18.308	24.960	33.711	40.959	45.066	46.932	51.889	59.565	77.735
J	1.000	5.10E-03	0.227	1.316	6.738	14.390	18.342	22.183	29.290	38.314	45.569	49.606	51.425	56.210	63.501	80.262
J	1.500	1.03E-02	0.362	1.868	8.513	17.147	21.436	25.523	32.922	42.070	49.262	53.211	54.977	59.593	66.541	82.161
J	2.500	2.86E-02	0.717	3.117	11.974	22.148	26.911	31.322	39.046	48.222	55.196	58.946	60.607	64.899	71.240	85.013
J	4.000	6.09E-02	1.186	4.547	15.403	26.752	31.830	36.430	44.285	53.332	60.029	63.571	65.128	69.116	74.920	87.180
J	6.500	0.145	2.119	7.025	20.584	33.251	38.618	43.353	51.194	59.891	66.120	69.349	70.753	74.312	79.393	89.745
J	10.000	0.354	3.832	10.956	27.682	41.525	47.051	51.787	59.369	67.426	72.984	75.795	77.003	80.026	84.240	92.444
K	0.100	1.04E-04	1.70E-02	0.188	1.842	5.440	7.726	10.188	15.315	22.807	29.575	33.618	35.502	40.645	48.994	70.500
K	0.400	5.08E-04	8.8E-02	0.415	3.124	8.086	10.989	13.988	19.945	28.174	35.270	39.392	41.287	46.384	54.454	74.325
K	0.650	1.32E-03	9.21E-02	0.669	4.292	10.261	13.580	16.925	23.378	31.991	39.210	43.330	45.209	50.217	58.025	76.724
K	1.000	2.64E-03	0.146	0.947	5.410	12.206	15.845	19.445	26.246	35.094	42.354	46.445	48.299	53.208	60.774	78.520
K	1.500	7.24E-03	0.287	1.568	7.573	15.707	19.828	23.793	31.052	40.147	47.378	51.376	53.170	57.875	65.002	81.205
K	2.500	1.52E-02	0.470	2.270	9.692	18.900	23.373	27.590	35.129	44.311	51.439	55.323	57.054	61.558	68.290	83.234
K	4.000	3.54E-02	0.825	3.465	12.849	23.351	28.206	32.675	40.447	49.602	56.509	60.206	61.840	66.054	72.252	85.614
K	6.500	8.31E-02	1.459	5.312	17.084	28.913	34.105	38.765	46.638	55.588	62.137	65.577	67.084	70.929	76.488	88.088
K	10.000	2.51E-01	3.050	9.234	24.700	38.122	43.608	48.363	56.079	64.420	70.262	73.247	74.535	77.111	82.341	91.396
L	0.065	2.54E-05	6.3E-03	9.29E-02	1.151	3.824	5.648	7.684	12.107	18.898	25.286	29.197	31.041	36.139	44.598	67.263
L	0.250	1.24E-04	1.90E-02	0.205	1.950	5.677	8.025	10.541	15.756	23.331	30.141	34.196	36.083	41.226	49.553	70.902
L	0.400	3.19E-04	3.58E-02	0.329	2.675	7.196	9.907	12.742	18.454	26.476	33.490	37.597	39.493	44.616	52.787	73.179
L	0.650	6.35E-04	6.6E-02	0.465	3.366	8.550	11.548	14.627	20.701	29.026	36.156	40.281	42.174	47.255	55.271	74.880
L	1.000	1.73E-03	0.110	0.766	4.696	10.977	14.419	17.863	24.453	33.163	40.403	44.515	46.386	51.360	59.079	77.417

TABLE 1B

100t/μ Ratios at the Limiting Quality Level
for the ASTM E2234 Plans, Consumer's Risk = 0.10

NOTE—These plans assume the characteristic being measured has a Weibull distribution.

NOTE—Where scientific notation is used (that is, E-x), the decimal point is moved to the left x places (for example, if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

Code Letter	AQL (p%)	Shape Parameter, β														
		0.333	0.50	0.667	1.000	1.333	1.500	1.667	2.000	2.500	3.000	3.333	3.500	4.000	5.000	10.000
L	1.500	3.58E-03	0.179	1.103	5.991	13.176	16.961	20.673	27.619	36.556	43.819	47.889	49.728	54.583	62.027	79.325
L	2.500	8.23E-03	0.312	1.671	7.903	16.218	20.400	24.411	31.722	40.838	48.057	52.038	53.823	58.497	65.560	81.553
L	4.000	1.89E-02	0.544	2.536	10.435	19.977	24.552	28.840	36.450	45.640	52.722	56.562	58.270	62.705	69.307	83.851
L	6.500	5.50E-02	1.109	4.323	14.892	26.083	31.122	35.699	43.544	52.617	59.357	62.931	64.503	68.535	74.416	86.887
M	0.040	6.51E-062.67E-034.70E-02	0.731	2.720	4.172	5.851	9.647	15.758	21.733	25.477	27.263	32.259	40.725	64.276		
M	0.150	3.15E-057.65E-03	0.103	1.237	4.035	5.924	8.022	12.549	19.448	25.897	29.831	31.683	36.792	45.242	67.747	
M	0.250	8.12E-051.44E-02	0.166	1.695	5.111	7.309	9.692	14.691	22.061	28.766	32.789	34.668	39.808	48.185	69.916	
M	0.400	1.61E-042.27E-02	0.234	2.131	6.069	8.515	11.119	16.472	24.176	31.047	35.120	37.011	42.153	50.443	71.535	
M	0.650	4.36E-044.40E-02	0.385	2.968	7.780	10.619	13.564	19.440	27.601	34.672	38.790	40.686	45.793	53.898	73.944	
M	1.000	8.99E-047.14E-02	0.553	3.779	9.326	12.474	15.679	21.935	30.402	37.580	41.706	43.593	48.643	56.566	75.753	
M	1.500	2.05E-03	0.124	0.834	4.970	11.454	14.975	18.481	25.157	33.924	41.174	45.279	47.143	52.093	77.857	
M	2.500	4.65E-03	0.214	1.257	6.537	14.066	17.975	21.782	28.849	37.852	45.110	49.157	50.981	55.785	80.019	
M	4.000	1.32E-02	0.429	2.120	9.260	18.265	22.674	26.846	34.338	43.511	50.664	54.572	56.316	60.861	67.671	82.856
N	0.025	1.63E-061.06E-032.35E-02	0.461	1.923	3.066	4.435	7.657	13.099	18.631	22.180	23.891	28.740	37.130	61.374		
N	0.100	7.87E-063.03E-035.17E-02	0.779	2.852	4.352	6.078	9.957	16.162	22.197	25.965	27.760	32.774	41.243	64.684		
N	0.150	2.02E-055.69E-038.29E-02	1.067	3.611	5.367	7.340	11.654	18.329	24.651	28.535	30.370	35.455	43.922	66.751		
N	0.250	4.01E-058.98E-03	0.117	1.340	4.286	6.250	8.418	13.063	20.082	26.600	30.558	32.418	37.538	45.974	68.293	
N	0.400	1.08E-041.74E-02	0.191	1.864	5.490	7.788	10.261	15.407	22.917	29.694	33.739	35.624	40.767	49.111	70.585	
N	0.650	2.22E-042.81E-02	0.275	2.371	6.574	9.142	11.853	17.374	25.229	32.171	36.262	38.156	43.292	51.530	72.302	
N	1.000	5.03E-044.84E-02	0.413	3.113	8.063	10.961	13.956	19.908	28.132	35.226	39.347	41.242	46.340	54.413	74.297	
N	1.500	1.13E-038.34E-02	0.621	4.083	9.883	13.135	16.425	22.801	31.358	38.562	42.685	44.568	49.594	57.448	76.341	
N	2.500	3.18E-03	0.166	1.040	5.759	12.791	16.519	20.188	27.078	35.982	43.245	47.324	49.169	54.046	61.538	79.012
P	0.015	3.97E-074.14E-041.16E-02	0.288	1.352	2.241	3.345	6.054	10.854	15.929	19.263	20.889	25.554	33.799	58.556		
P	0.065	1.92E-061.18E-032.55E-02	0.487	2.004	3.181	4.583	7.871	13.390	18.975	22.548	24.269	29.138	37.540	61.712		
P	0.100	4.93E-062.22E-034.09E-02	0.666	2.537	3.922	5.534	9.209	15.183	21.071	26.777	28.548	31.519	39.975	63.682		
P	0.150	9.76E-063.50E-035.76E-02	0.837	3.010	4.565	6.345	10.321	16.633	22.734	26.530	28.335	33.367	41.840	65.150		
P	0.250	2.62E-056.76E-039.43E-02	1.163	3.853	5.686	7.731	12.169	18.975	25.372	29.285	31.130	36.230	44.688	67.331		
P	0.400	5.38E-051.09E-02	0.135	1.478	4.612	6.671	8.926	13.717	20.883	27.481	31.468	33.336	38.467	46.882	68.964	
P	0.650	1.21E-041.88E-02	0.203	1.938	5.652	7.992	10.503	15.708	23.275	30.080	34.134	36.021	41.164	49.493	70.859	
P	1.000	2.73E-043.22E-02	0.304	2.538	6.919	9.567	12.349	17.977	25.928	32.911	37.012	38.908	44.037	52.238	72.797	
P	1.500	7.58E-046.37E-02	0.507	3.570	8.937	12.010	15.153	21.321	29.718	36.874	41.000	42.891	47.957	55.926	75.323	
Q	0.010	1.04E-071.70E-045.95E-03	0.184	0.967	1.665	2.559	4.843	9.080	13.728	16.849	18.388	22.856	30.913	56.000		
Q	0.040	5.03E-074.85E-041.31E-02	0.311	1.434	2.362	3.506	6.296	11.200	16.351	19.721	21.362	26.060	34.333	59.017		
Q	0.065	1.29E-069.08E-042.09E-02	0.426	1.815	2.912	4.233	7.366	12.699	18.155	21.669	23.367	28.188	36.558	60.899		
Q	0.100	2.55E-061.43E-032.94E-02	0.535	2.153	3.389	4.852	8.254	13.910	19.587	23.201	24.938	29.839	38.262	62.302		
Q	0.150	6.85E-062.76E-034.82E-02	0.743	2.755	4.220	5.911	9.729	15.865	21.856	25.607	27.395	32.396	40.863	64.385		
Q	0.250	1.40E-054.46E-036.90E-02	0.944	3.296	4.949	6.823	10.965	17.458	23.670	27.512	29.332	34.392	42.865	65.943		
Q	0.400	3.16E-057.66E-03	0.104	1.237	4.037	5.926	8.025	12.552	19.452	25.902	29.836	31.688	36.797	45.247	67.751	
Q	0.650	7.08E-051.31E-02	0.155	1.619	4.939	7.090	9.430	14.359	21.661	28.332	32.343	34.219	39.356	47.747	69.597	
Q	1.000	1.96E-042.59E-02	0.258	2.274	6.371	8.891	11.560	17.015	24.812	31.726	35.811	37.704	42.842	51.101	72.001	
R	0.025	1.23E-071.89E-046.45E-03	0.195	1.008	1.726	2.644	4.977	9.280	13.979	17.127	18.677	23.170	31.252	56.307		
R	0.040	3.15E-073.54E-041.03E-02	0.266	1.275	2.128	3.192	5.822	10.521	15.521	18.818	20.429	25.061	33.276	58.102		
R	0.065	6.23E-075.59E-041.45E-02	0.334	1.513	2.477	3.659	6.524	11.524	16.744	20.147	21.801	26.528	34.826	59.439		
R	0.100	1.67E-061.08E-032.38E-02	0.464	1.935	3.083	4.456	7.689	13.142	18.682	22.234	23.947	28.799	37.191	61.424		
R	0.150	3.42E-061.74E-033.41E-02	0.590	2.315	3.615	5.143	8.664	14.460	20.230	23.886	25.638	30.571	39.011	62.909		
R	0.250	7.68E-062.98E-035.11E-02	0.772	2.835	4.328	6.047	9.916	16.108	22.135	25.901	27.694	32.705	41.175	64.630		
R	0.400	1.72E-055.10E-037.63E-02	1.010	3.466	5.176	7.104	11.340	17.934	24.206	28.072	29.901	34.975	43.445	66.388		
R	0.650	4.74E-051.00E-02	0.127	1.417	4.468	6.486	8.703	13.430	20.533	27.097	31.071	32.936	38.062	46.487	68.673	

TABLE 1C

100t/μ Ratios at the Limiting Quality Level
for the MIL-STD-105D Plans, Consumer's Risk = 0.05

NOTE—These plans assume the characteristic being measured has a Weibull distribution.

NOTE—Where scientific notation is used (that is, E-x), the decimal point is moved to the left x places (for example, if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

Code Letter	AQL (p%)	Shape Parameter, β														
		0.333	0.50	0.667	1.000	1.333	1.500	1.667	2.000	2.500	3.000	3.333	3.500	4.000	5.000	10.000
A	6.500	56.010	112.180	137.903	149.787	147.319	145.016	142.620	138.099	132.476	128.130	125.783	124.743	122.053	118.079	109.448
B	4.000	16.596	49.858	75.065	99.858	108.690	110.668	111.822	112.758	112.642	111.932	111.377	111.097	110.287	108.881	105.099
C	2.500	3.585	17.949	34.887	59.915	74.098	78.727	82.303	87.342	91.825	94.407	95.552	96.010	97.065	98.307	99.865
C	10.000	20.487	57.375	83.403	107.122	114.568	115.972	116.634	116.787	115.851	114.582	113.748	113.349	112.240	110.421	105.839



TABLE 1C

100t/μ Ratios at the Limiting Quality Level for the MIL-STD-105D Plans, Consumer's Risk = 0.05

NOTE—These plans assume the characteristic being measured has a Weibull distribution.

NOTE—Where scientific notation is used (that is, E-x), the decimal point is moved to the left x places (for example, if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

Table with columns: Code Letter, AQL (p%), and Shape Parameter, β (0.333, 0.50, 0.667, 1.000, 1.333, 1.500, 1.667, 2.000, 2.500, 3.000, 3.333, 3.500, 4.000, 5.000, 10.000). Rows list various code letters (D, E, F, G, H, J, K, L, M, N) and their corresponding AQL values and ratios.

TABLE 1C

100t/μ Ratios at the Limiting Quality Level
for the MIL-STD-105D Plans, Consumer's Risk = 0.05

NOTE—These plans assume the characteristic being measured has a Weibull distribution.

NOTE—Where scientific notation is used (that is, E-x), the decimal point is moved to the left x places (for example, if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

Code Letter	AQL (p%)	Shape Parameter, β														
		0.333	0.50	0.667	1.000	1.333	1.500	1.667	2.000	2.500	3.000	3.333	3.500	4.000	5.000	10.000
N	0.650	3.10E-04	3.51E-02	0.324	2.648	7.143	9.842	12.667	18.363	26.371	33.379	37.486	39.382	44.506	52.683	73.106
N	1.000	6.71E-04	5.87E-02	0.477	3.427	8.666	11.687	14.786	20.888	29.235	36.374	40.499	42.392	47.468	55.470	75.015
N	1.500	1.46E-03	9.86E-02	0.704	4.440	10.524	13.889	17.271	23.776	32.426	39.653	43.771	45.647	50.643	58.419	76.983
N	2.500	3.93E-03	0.191	1.155	6.179	13.485	17.313	21.060	28.049	37.010	44.272	48.334	50.168	55.006	62.411	79.570
P	0.015	8.75E-07	7.01E-04	1.72E-02	0.374	1.647	2.671	3.917	6.905	12.059	17.390	20.845	22.520	27.292	35.625	60.117
P	0.065	3.48E-06	1.76E-03	3.44E-02	0.593	2.326	3.631	5.163	8.692	14.497	20.274	23.932	25.685	30.620	39.061	62.949
P	0.100	8.15E-06	3.10E-03	5.26E-02	0.788	2.878	4.386	6.121	10.016	16.239	22.284	26.057	27.854	32.870	41.341	64.760
P	0.150	1.53E-05	4.71E-03	7.20E-02	0.971	3.366	5.042	6.938	11.119	17.654	23.891	27.743	29.567	34.633	43.105	66.128
P	0.250	3.82E-05	8.69E-03	0.114	1.318	4.233	6.182	8.335	12.956	19.950	26.454	30.407	32.265	37.383	45.822	68.180
P	0.400	7.50E-05	1.36E-02	0.160	1.651	5.011	7.182	9.539	14.498	21.828	28.514	32.530	34.407	39.546	47.931	69.731
P	0.650	1.62E-04	2.28E-02	0.234	2.134	6.074	8.522	11.127	16.482	24.188	31.060	35.133	37.024	42.166	50.455	71.544
P	1.000	3.50E-04	3.81E-02	0.345	2.760	7.368	10.117	12.985	18.746	26.811	33.843	37.954	39.850	44.968	53.120	73.409
P	1.500	9.37E-04	7.34E-02	0.564	3.831	9.421	12.588	15.807	22.085	30.567	37.750	41.876	43.762	48.809	56.719	75.855
Q	0.010	2.29E-07	2.87E-04	8.83E-03	0.240	1.179	1.984	2.997	5.524	10.088	14.986	18.233	19.824	24.411	32.583	57.493
Q	0.040	9.12E-07	7.21E-04	1.76E-02	0.380	1.664	2.696	3.949	6.953	12.126	17.470	20.931	22.609	27.386	35.724	60.200
Q	0.065	2.13E-06	1.27E-03	2.69E-02	0.504	2.058	3.257	4.682	8.011	13.581	19.201	22.789	24.516	29.397	37.807	61.931
Q	0.100	3.99E-06	1.93E-03	3.68E-02	0.621	2.407	3.743	5.306	8.892	14.764	20.584	24.261	26.022	30.971	39.419	63.237
Q	0.150	9.98E-06	3.55E-03	5.82E-02	0.843	3.026	4.587	6.373	10.359	16.681	22.789	26.588	28.394	33.427	41.900	65.197
Q	0.250	1.96E-05	5.56E-03	8.15E-02	1.055	3.581	5.328	7.291	11.589	18.248	24.559	28.440	30.274	35.357	43.824	66.677
Q	0.400	4.22E-05	9.28E-03	0.120	1.362	4.339	6.319	8.501	13.171	20.215	26.746	30.710	32.571	37.693	46.125	68.406
Q	0.650	9.10E-05	1.55E-02	0.176	1.761	5.259	7.497	9.916	14.973	22.399	29.134	33.166	35.047	40.189	48.553	70.183
Q	1.000	2.42E-04	2.98E-02	0.287	2.440	6.717	9.318	12.059	17.625	25.520	32.480	36.575	38.470	43.603	51.826	72.509
R	0.025	2.23E-07	2.81E-04	8.69E-03	0.237	1.170	1.970	2.979	5.496	10.047	14.936	18.178	19.767	24.349	32.518	57.435
R	0.040	5.21E-07	4.96E-04	1.33E-02	0.315	1.447	2.380	3.531	6.332	11.252	16.415	19.790	21.433	26.136	34.413	59.086
R	0.065	9.73E-07	7.53E-04	1.82E-02	0.388	1.691	2.735	4.001	7.028	12.231	17.596	21.068	22.749	27.535	35.879	60.331
R	0.100	2.43E-06	1.39E-03	2.87E-02	0.526	2.126	3.352	4.804	8.186	13.818	19.479	23.086	24.820	29.716	38.135	62.199
R	0.150	4.76E-06	2.17E-03	4.02E-02	0.659	2.515	3.892	5.496	9.157	15.114	20.991	24.692	26.462	31.429	39.884	63.609
R	0.250	1.02E-05	3.61E-03	5.90E-02	0.850	3.047	4.615	6.407	10.405	16.740	22.856	26.659	28.466	33.502	41.975	65.255
R	0.400	2.21E-05	6.03E-03	8.66E-02	1.098	3.691	5.473	7.470	11.825	18.545	24.891	28.786	30.625	35.715	44.179	66.946
R	0.650	5.85E-05	1.16E-02	0.141	1.520	4.710	6.797	9.078	13.912	21.120	27.740	31.735	33.605	38.738	47.146	69.158

TABLE 2A

100h/(t) Products at the Acceptable Quality Level (normal inspection)
for the MIL-STD-105D Plans

NOTE—These plans assume the characteristic being measured has a Weibull distribution.

NOTE—Where scientific notation is used (that is, E-x), the decimal point is moved to the left x places (for example, if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

AQL p' (%)	Shape Parameter, β															
	0.333	0.500	0.667	1.000	1.333	1.500	1.667	2.000	2.500	3.000	3.333	3.500	4.000	5.000	10.000	
0.010	3.33E-03	5.00E-03	6.67E-03	1.00E-02	1.33E-02	1.50E-02	1.67E-02	2.00E-02	2.50E-02	3.00E-02	3.33E-02	3.50E-02	4.00E-02	5.00E-02	0.100	
0.015	5.00E-03	7.50E-03	1.00E-02	1.50E-02	2.00E-02	2.25E-02	2.50E-02	3.00E-02	3.75E-02	4.50E-02	5.00E-02	5.25E-02	6.00E-02	7.50E-02	0.150	
0.025	8.33E-03	1.25E-02	1.67E-02	2.50E-02	3.33E-02	3.75E-02	4.17E-02	5.00E-02	6.25E-02	7.50E-02	8.33E-02	8.75E-02	0.100	0.125	0.250	
0.040	1.33E-02	2.00E-02	2.67E-02	4.00E-02	5.33E-02	6.00E-02	6.67E-02	8.00E-02	0.100	0.120	0.133	0.140	0.160	0.200	0.400	
0.065	2.17E-02	3.25E-02	4.33E-02	6.50E-02	0.087	9.75E-02	0.108	0.130	0.163	0.195	0.217	0.228	0.260	0.325	0.650	
0.100	3.34E-02	5.00E-02	6.67E-02	0.100	0.133	0.150	0.167	0.200	0.250	0.300	0.334	0.350	0.400	0.500	1.001	
0.150	5.00E-02	7.51E-02	0.100	0.150	0.200	0.225	0.250	0.300	0.375	0.450	0.500	0.525	0.600	0.751	1.501	
0.250	8.34E-02	0.125	0.167	0.250	0.334	0.375	0.417	0.501	0.626	0.751	0.834	0.876	1.001	1.252	2.503	
0.400	0.134	0.200	0.267	0.401	0.534	0.601	0.668	0.802	1.002	1.202	1.336	1.403	1.603	2.004	4.008	
0.650	0.217	0.326	0.435	0.652	0.869	0.978	1.087	1.304	1.630	1.956	2.174	2.282	2.608	3.261	6.521	
1.000	0.335	0.503	0.670	1.005	1.340	1.508	1.675	2.010	2.513	3.015	3.350	3.518	4.020	5.025	10.050	
1.500	0.504	0.756	1.008	1.511	2.015	2.267	2.519	3.023	3.778	4.534	5.038	5.290	6.045	7.557	15.114	
2.500	0.844	1.266	1.688	2.532	3.376	3.798	4.220	5.064	6.329	7.595	8.439	8.861	10.127	12.659	25.318	
4.000	1.361	2.041	2.721	4.082	5.443	6.123	6.804	8.164	10.205	12.247	13.607	14.288	16.329	20.411	40.822	
6.500	2.240	3.360	4.481	6.721	8.961	10.081	11.201	13.442	16.802	20.163	22.403	23.523	26.883	33.604	67.209	
10.000	3.512	5.268	7.024	10.536	14.048	15.804	17.560	21.072	26.340	31.608	35.120	36.876	42.144	52.680	105.361	



TABLE 2B

100h(t) Products at the Limiting Quality Level for the MIL-STD-105D Plans, Consumer's Risk = 0.10

NOTE—These plans assume the characteristic being measured has a Weibull distribution.

NOTE—Where scientific notation is used (that is, E-x), the decimal point is moved to the left x places (for example, if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

Table with columns: Code Letter, AQL (p%), and Shape Parameter β (0.333, 0.50, 0.667, 1.000, 1.333, 1.500, 1.667, 2.000, 2.500, 3.000, 3.333, 3.500, 4.000, 5.000, 10.000). Rows list various code letters (A-N) and AQL values.

TABLE 2B

100h(t) Products at the Limiting Quality Level
for the MIL-STD-105D Plans, Consumer's Risk = 0.10

NOTE—These plans assume the characteristic being measured has a Weibull distribution.

NOTE—Where scientific notation is used (that is, E-x), the decimal point is moved to the left x places (for example, if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

Code Letter	AQL (p%)	Shape Parameter, β														
		0.333	0.50	0.667	1.000	1.333	1.500	1.667	2.000	2.500	3.000	3.333	3.500	4.000	5.000	10.000
N	0.100	0.260	0.389	0.519	0.779	1.038	1.168	1.298	1.557	1.947	2.336	2.596	2.726	3.115	3.894	7.787
N	0.150	0.356	0.533	0.711	1.067	1.422	1.600	1.778	2.133	2.667	3.200	3.555	3.733	4.266	5.333	10.666
N	0.250	0.447	0.670	0.893	1.340	1.787	2.010	2.234	2.680	3.350	4.021	4.467	4.691	5.361	6.701	13.402
N	0.400	0.621	0.932	1.243	1.864	2.486	2.796	3.107	3.729	4.661	5.593	6.214	6.525	7.457	9.321	18.643
N	0.650	0.790	1.185	1.581	2.371	3.161	3.556	3.951	4.742	5.927	7.113	7.903	8.298	9.483	11.854	23.708
N	1.000	1.038	1.556	2.075	3.113	4.150	4.669	5.188	6.225	7.782	9.338	10.375	10.894	12.450	15.563	31.126
N	1.500	1.361	2.042	2.722	4.083	5.444	6.125	6.805	8.166	10.208	12.249	13.610	14.291	16.332	20.416	40.831
N	2.500	1.920	2.879	3.839	5.759	7.678	8.638	9.598	11.518	14.397	17.277	19.196	20.156	23.035	28.794	57.588
P	0.015	9.59E-02	0.144	0.192	0.288	0.384	0.432	0.480	0.576	0.720	0.863	0.959	1.007	1.151	1.439	2.878
P	0.065	0.162	0.243	0.324	0.487	0.649	0.730	0.811	0.973	1.216	1.460	1.622	1.703	1.946	2.433	4.865
P	0.100	0.222	0.333	0.444	0.666	0.888	0.999	1.110	1.332	1.665	1.998	2.220	2.331	2.664	3.331	6.661
P	0.150	0.279	0.418	0.558	0.837	1.116	1.255	1.394	1.673	2.092	2.510	2.789	2.928	3.347	4.183	8.367
P	0.250	0.388	0.581	0.775	1.163	1.551	1.744	1.938	2.326	2.907	3.489	3.877	4.070	4.652	5.815	11.630
P	0.400	0.493	0.739	0.985	1.478	1.970	2.217	2.463	2.956	3.695	4.434	4.926	5.172	5.911	7.389	14.778
P	0.650	0.646	0.969	1.292	1.938	2.584	2.907	3.230	3.876	4.845	5.814	6.460	6.783	7.752	9.690	19.380
P	1.000	0.846	1.269	1.692	2.538	3.384	3.807	4.230	5.077	6.346	7.615	8.461	8.884	10.153	12.691	25.383
P	1.500	1.190	1.785	2.380	3.570	4.760	5.355	5.950	7.140	8.925	10.710	11.900	12.496	14.281	17.851	35.701
Q	0.010	6.14E-02	9.21E-02	0.123	0.184	0.246	0.276	0.307	0.368	0.461	0.553	0.614	0.645	0.737	0.921	1.842
Q	0.040	0.104	0.156	0.208	0.311	0.415	0.467	0.519	0.623	0.778	0.934	1.038	1.090	1.245	1.557	3.113
Q	0.065	0.142	0.213	0.284	0.426	0.568	0.639	0.710	0.852	1.065	1.278	1.420	1.491	1.704	2.131	4.261
Q	0.100	0.178	0.268	0.357	0.535	0.713	0.803	0.892	1.070	1.338	1.605	1.784	1.873	2.140	2.676	5.351
Q	0.150	0.248	0.372	0.496	0.743	0.991	1.115	1.239	1.487	1.859	2.230	2.478	2.602	2.974	3.717	7.435
Q	0.250	0.315	0.472	0.630	0.944	1.259	1.416	1.574	1.889	2.361	2.833	3.148	3.305	3.777	4.722	9.443
Q	0.400	0.412	0.619	0.825	1.237	1.650	1.856	2.062	2.475	3.094	3.712	4.125	4.331	4.950	6.187	12.375
Q	0.650	0.540	0.810	1.080	1.619	2.159	2.429	2.699	3.239	4.048	4.858	5.398	5.668	6.477	8.097	16.193
Q	1.000	0.758	1.137	1.516	2.274	3.032	3.411	3.790	4.548	5.685	6.822	7.580	7.959	9.096	11.370	22.739
R	0.025	6.48E-02	9.73E-02	0.130	0.195	0.259	0.292	0.324	0.389	0.486	0.584	0.648	0.681	0.778	0.973	1.945
R	0.040	8.87E-02	0.133	0.177	0.266	0.355	0.399	0.444	0.532	0.666	0.799	0.887	0.932	1.065	1.331	2.662
R	0.065	0.111	0.167	0.223	0.334	0.446	0.501	0.557	0.669	0.836	1.003	1.114	1.170	1.337	1.671	3.343
R	0.100	0.155	0.232	0.310	0.464	0.619	0.696	0.774	0.929	1.161	1.393	1.548	1.625	1.857	2.322	4.643
R	0.150	0.197	0.295	0.393	0.590	0.786	0.884	0.983	1.179	1.474	1.769	1.965	2.064	2.358	2.948	5.896
R	0.250	0.257	0.386	0.515	0.772	1.030	1.158	1.287	1.545	1.931	2.317	2.574	2.703	3.089	3.861	7.723
R	0.400	0.337	0.505	0.673	1.010	1.347	1.515	1.683	2.020	2.525	3.030	3.366	3.535	4.040	5.050	10.099
R	0.650	0.472	0.708	0.944	1.417	1.889	2.125	2.361	2.833	3.542	4.250	4.722	4.958	5.667	7.083	14.167

TABLE 2C

100t/ μ Ratios at the Limiting Quality Level
for the MIL-STD-105D Plans, Consumer's Risk = 0.05

NOTE—These plans assume the characteristic being measured has a Weibull distribution.

NOTE—Where scientific notation is used (that is, E-x), the decimal point is moved to the left x places (for example, if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

Code Letter	AQL (p%)	Shape Parameter, β														
		0.333	0.50	0.667	1.000	1.333	1.500	1.667	2.000	2.500	3.000	3.333	3.500	4.000	5.000	10.000
A	6.500	49.929	74.893	99.858	149.787	199.715	224.680	249.644	299.573	374.467	449.360	499.289	524.253	599.146	748.933	1497.866
B	4.000	33.286	49.929	66.572	99.858	133.144	149.787	166.430	199.715	249.644	299.573	332.859	349.502	399.431	499.289	998.577
C	2.500	19.972	29.957	39.943	59.915	79.886	89.872	99.858	119.829	149.787	179.744	199.715	209.701	239.659	299.573	599.146
C	10.000	35.707	53.561	71.414	107.122	142.829	160.682	178.536	214.243	267.804	321.365	357.072	374.926	428.486	535.608	1071.216
D	1.500	12.482	18.723	24.964	37.447	49.929	56.170	62.411	74.893	93.617	112.340	124.822	131.063	149.787	187.233	374.467
D	6.500	21.205	31.808	42.411	63.616	84.821	95.424	106.027	127.232	159.040	190.848	212.054	222.656	254.464	318.080	636.161
D	10.000	30.517	45.776	61.034	91.551	122.068	137.327	152.585	183.102	228.878	274.653	305.171	320.429	366.205	457.756	915.512
E	1.000	7.681	11.522	15.363	23.044	30.725	34.566	38.407	46.088	57.610	69.132	76.814	80.654	92.176	115.220	230.441
E	4.000	12.676	19.015	25.353	38.029	50.706	57.044	63.382	76.059	95.073	114.088	126.764	133.102	152.117	190.146	380.293
E	6.500	17.593	26.390	35.187	52.780	70.373	79.170	87.966	105.560	131.950	158.340	175.933	184.730	211.120	263.899	527.799
E	10.000	22.750	34.125	45.500	68.250	91.000	102.375	113.750	136.500	170.626	204.751	227.501	238.876	273.001	341.251	682.502
F	0.650	4.993	7.489	9.986	14.979	19.972	22.468	24.964	29.957	37.447	44.936	49.929	52.425	59.915	74.893	149.787
F	2.500	8.116	12.174	16.232	24.348	32.464	36.522	40.580	48.696	60.870	73.045	81.161	85.219	97.393	121.741	243.482
F	4.000	11.072	16.607	22.143	33.215	44.286	49.822	55.358	66.430	83.037	99.644	110.716	116.252	132.859	166.074	332.148
F	6.500	14.036	21.054	28.072	42.108	56.144	63.162	70.180	84.216	105.271	126.325	140.361	147.379	168.433	210.541	421.082
F	10.000	20.268	30.402	40.536	60.804	81.072	91.206	101.340	121.608	152.010	182.412	202.680	212.814	243.216	304.020	608.039
G	0.400	3.121	4.681	6.241	9.362	12.482	14.042	15.603	18.723	23.404	28.085	31.206	32.766	37.447	46.808	93.617
G	1.500	5.022	7.532	10.043	15.065	20.086	22.597	25.108	30.130	37.662	45.195	50.216	52.727	60.259	75.324	150.648

TABLE 2C

100t/μ Ratios at the Limiting Quality Level
for the MIL-STD-105D Plans, Consumer's Risk = 0.05

NOTE—These plans assume the characteristic being measured has a Weibull distribution.

NOTE—Where scientific notation is used (that is, E-x), the decimal point is moved to the left x places (for example, if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

Code Letter	AQL (p%)	Shape Parameter, β														
		0.333	0.50	0.667	1.000	1.333	1.500	1.667	2.000	2.500	3.000	3.333	3.500	4.000	5.000	10.000
Q	0.040	0.127	0.190	0.253	0.380	0.506	0.569	0.633	0.759	0.949	1.139	1.266	1.329	1.519	1.898	3.797
Q	0.065	0.168	0.252	0.336	0.504	0.672	0.756	0.840	1.008	1.260	1.512	1.680	1.764	2.016	2.520	5.041
Q	0.100	0.207	0.311	0.414	0.621	0.828	0.932	1.035	1.242	1.553	1.863	2.070	2.174	2.484	3.105	6.210
Q	0.150	0.281	0.421	0.562	0.843	1.124	1.264	1.405	1.685	2.107	2.528	2.809	2.950	3.371	4.214	8.427
Q	0.250	0.352	0.527	0.703	1.055	1.406	1.582	1.758	2.110	2.637	3.164	3.516	3.692	4.219	5.274	10.548
Q	0.400	0.454	0.681	0.908	1.362	1.817	2.044	2.271	2.725	3.406	4.087	4.541	4.769	5.450	6.812	13.624
Q	0.650	0.587	0.880	1.174	1.761	2.348	2.641	2.935	3.522	4.402	5.282	5.869	6.163	7.043	8.804	17.608
Q	1.000	0.813	1.220	1.627	2.440	3.253	3.660	4.066	4.880	6.099	7.319	8.133	8.539	9.759	12.199	24.398
R	0.025	0.079	0.119	0.158	0.237	0.316	0.356	0.395	0.475	0.593	0.712	0.791	0.830	0.949	1.186	2.373
R	0.040	0.105	0.157	0.210	0.315	0.420	0.472	0.525	0.630	0.787	0.945	1.050	1.102	1.260	1.575	3.149
R	0.065	0.129	0.194	0.259	0.388	0.517	0.582	0.647	0.776	0.970	1.164	1.293	1.358	1.552	1.940	3.880
R	0.100	0.175	0.263	0.351	0.526	0.702	0.789	0.877	1.053	1.316	1.579	1.754	1.842	2.105	2.632	5.263
R	0.150	0.220	0.329	0.439	0.659	0.878	0.988	1.098	1.317	1.646	1.976	2.195	2.305	2.634	3.293	6.586
R	0.250	0.283	0.425	0.567	0.850	1.134	1.275	1.417	1.700	2.126	2.551	2.834	2.976	3.401	4.251	8.502
R	0.400	0.366	0.549	0.732	1.098	1.464	1.647	1.830	2.196	2.745	3.295	3.661	3.844	4.393	5.491	10.982
R	0.650	0.507	0.760	1.013	1.520	2.027	2.280	2.533	3.040	3.800	4.560	5.067	5.320	6.080	7.600	15.200

TABLE 2D

Table of Hazard Rate Ratios for t_2/t_1
 $h(t_2)/h(t_1)$

NOTE—These plans assume the characteristic being measured has a Weibull distribution.

NOTE—Where scientific notation is used (that is, E-x), the decimal point is moved to the left x places (for example, if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

t_2/t_1	Shape Parameter, β														
	0.333	0.500	0.667	1.000	1.333	1.500	1.667	2.000	2.500	3.000	3.333	3.500	4.000	5.000	10.000
1.25	0.862	0.894	0.928	1.000	1.077	1.118	1.160	1.250	1.398	1.563	1.683	1.747	1.953	2.441	7.451
1.50	0.763	0.816	0.874	1.000	1.145	1.225	1.310	1.500	1.837	2.250	2.576	2.756	3.375	5.063	38.443
1.75	0.689	0.756	0.830	1.000	1.205	1.323	1.452	1.750	2.315	3.063	3.691	4.051	5.359	9.379	153.937
2.00	0.630	0.707	0.794	1.000	1.260	1.414	1.587	2.000	2.828	4.000	5.040	5.657	8.000	16.000	512.000
2.25	0.582	0.667	0.763	1.000	1.310	1.500	1.717	2.250	3.375	5.063	6.634	7.594	11.391	25.629	1,477.892
2.50	0.543	0.632	0.737	1.000	1.357	1.581	1.842	2.500	3.953	6.250	8.483	9.882	15.625	39.063	3,814.697
2.75	0.509	0.603	0.714	1.000	1.401	1.658	1.963	2.750	4.560	7.563	10.595	12.541	20.797	57.191	8,994.857
3.00	0.481	0.577	0.693	1.000	1.442	1.732	2.080	3.000	5.196	9.000	12.980	15.588	27.000	81.000	19,683.000
3.25	0.456	0.555	0.675	1.000	1.481	1.803	2.194	3.250	5.859	10.563	15.646	19.042	34.328	111.566	40,452.955
3.50	0.434	0.535	0.659	1.000	1.518	1.871	2.305	3.500	6.548	12.250	18.599	22.918	42.875	150.063	78,815.639
3.75	0.414	0.516	0.644	1.000	1.554	1.936	2.414	3.750	7.262	14.063	21.848	27.232	52.734	197.754	146,649.778
4.00	0.397	0.500	0.630	1.000	1.587	2.000	2.520	4.000	8.000	16.000	25.398	32.000	64.000	256.000	262,144.000
4.25	0.381	0.485	0.617	1.000	1.620	2.062	2.624	4.250	8.762	18.063	29.258	37.237	76.766	326.254	452,376.848
4.50	0.367	0.471	0.606	1.000	1.651	2.121	2.726	4.500	9.546	20.250	33.432	42.957	91.125	410.063	756,680.643
4.75	0.354	0.459	0.595	1.000	1.681	2.179	2.826	4.750	10.352	22.563	37.927	49.174	107.172	509.066	1,230,955.878
5.00	0.342	0.447	0.585	1.000	1.710	2.236	2.924	5.000	11.180	25.000	42.749	55.902	125.000	625.000	1,953,125.000



TABLE 3B

100t/p Ratios at the Limiting Quality Level for the MIL-STD-105D Plans, r = 0.90, Consumer's Risk = 0.10

NOTE—These plans assume the characteristic being measured has a Weibull distribution.

NOTE—Where scientific notation is used (that is, E-x), the decimal point is moved to the left x places (for example, if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

Table with 16 columns: Code Letter, AQL (p%), and Shape Parameter β (0.333, 0.50, 0.667, 1.000, 1.333, 1.500, 1.667, 2.000, 2.500, 3.000, 3.333, 3.500, 4.000, 5.000, 10.000). Rows include various code letters (J, K, L, M, N, P, Q, R) and their corresponding AQL values and β ratios.

TABLE 3C

100/p Ratios at the Limiting Quality Level
for the MIL-STD-105D Plans, r = 0.90, Consumer's Risk = 0.05

NOTE—These plans assume the characteristic being measured has a Weibull distribution.

NOTE—Where scientific notation is used (that is, E-x), the decimal point is moved to the left x places (for example, if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

Code Letter	AQL (p%)	Shape Parameter, β														
		0.333	0.50	0.667	1.000	1.333	1.500	1.667	2.000	2.500	3.000	3.333	3.500	4.000	5.000	10.000
N	0.100	7.32E-02	0.813	2.706	9.014	16.451	20.104	23.602	30.023	38.192	44.837	48.582	50.281	54.794	61.799	78.613
N	0.150	0.172	1.434	4.144	11.975	20.357	24.295	27.987	34.605	42.787	49.290	52.903	54.532	58.826	65.412	80.877
N	0.250	0.322	2.179	5.672	14.763	23.816	27.933	31.732	38.422	46.523	52.851	56.331	57.892	61.986	68.208	82.588
N	0.400	0.807	4.023	8.982	20.057	29.971	34.264	38.138	44.785	52.590	58.536	61.756	63.190	66.922	72.519	85.158
N	0.650	1.588	6.318	12.601	25.135	35.498	39.828	43.668	50.135	57.559	63.109	66.082	67.399	70.806	75.867	87.102
N	1.000	3.441	10.579	18.549	32.525	43.069	47.295	50.972	57.031	63.810	68.771	71.395	72.549	75.519	79.881	89.376
N	1.500	7.483	17.757	27.355	42.140	52.302	56.207	59.541	64.915	70.774	74.972	77.163	78.121	80.570	84.128	91.721
N	2.500	20.171	34.394	44.912	58.646	67.016	70.664	72.601	76.581	80.779	83.704	85.206	85.858	87.511	89.877	94.803
P	0.015	4.49E-03	0.126	0.670	3.554	8.186	10.810	13.503	18.852	26.320	32.878	36.747	38.541	43.419	51.304	71.626
P	0.065	1.79E-02	0.317	1.336	5.632	11.561	14.692	17.798	23.731	31.641	38.331	42.188	43.958	48.715	56.251	75.000
P	0.100	4.18E-02	0.559	2.045	7.479	14.301	17.751	21.101	27.347	35.443	42.132	45.935	47.669	52.295	59.534	77.158
P	0.150	7.83E-02	0.849	2.798	9.216	16.727	20.403	23.918	30.358	38.532	45.170	48.907	50.601	55.098	62.074	78.787
P	0.250	0.196	1.565	4.426	12.512	21.037	25.016	28.734	35.372	43.544	50.016	53.604	55.219	59.474	65.988	81.233
P	0.400	0.385	2.455	6.202	15.668	24.903	29.063	32.885	39.582	47.643	53.910	57.346	58.885	62.915	69.024	83.081
P	0.650	0.830	4.101	9.113	20.251	30.188	34.485	38.359	45.001	52.793	58.724	61.935	63.364	67.083	72.659	85.240
P	1.000	1.798	6.862	13.408	26.196	36.617	40.941	44.766	51.182	58.519	63.985	66.907	68.200	71.542	76.498	87.463
P	1.500	4.806	13.218	21.922	36.357	46.821	50.940	54.495	60.297	66.717	71.372	73.821	74.895	77.651	81.680	90.377
Q	0.010	1.18E-03	5.17E-02	0.343	2.275	5.857	8.028	10.331	15.082	22.017	28.334	32.142	33.927	38.835	46.923	68.500
Q	0.040	4.68E-03	0.130	0.684	3.603	8.271	10.910	13.615	18.983	26.466	33.030	36.899	38.693	43.569	51.445	71.725
Q	0.065	1.10E-02	0.229	1.046	4.784	10.230	13.179	16.139	21.873	29.643	36.302	40.174	41.957	46.768	54.445	73.787
Q	0.100	2.05E-02	0.347	1.431	5.894	11.963	15.146	18.292	24.278	32.224	38.918	42.769	44.535	49.273	56.766	75.343
Q	0.150	5.12E-02	0.640	2.262	7.999	15.040	18.564	21.969	28.282	36.409	43.086	46.871	48.593	53.181	60.340	77.679
Q	0.250	0.100	1.002	3.168	10.011	17.798	21.561	25.136	31.641	39.829	46.433	50.136	51.812	56.250	63.110	79.442
Q	0.400	0.216	1.672	4.650	12.931	21.564	25.572	29.308	35.960	44.122	50.568	54.137	55.742	59.967	66.424	81.501
Q	0.650	0.467	2.793	6.832	16.712	26.138	30.340	34.184	40.881	48.889	55.082	58.467	59.980	63.938	69.921	83.619
Q	1.000	1.242	5.362	11.143	23.157	33.382	37.709	41.572	48.121	55.702	61.408	64.477	65.838	69.370	74.634	86.391
R	0.025	1.14E-03	0.051	0.338	2.252	5.813	7.974	10.269	15.006	21.929	28.239	32.045	33.829	38.738	46.828	68.431
R	0.040	2.67E-03	8.94E-02	0.517	2.989	7.189	9.632	12.171	17.289	24.560	31.035	34.887	36.681	41.581	49.558	70.397
R	0.065	4.99E-03	0.136	0.707	3.682	8.406	11.068	13.794	19.189	26.696	33.269	37.140	38.933	43.806	51.668	71.881
R	0.100	1.25E-02	0.250	1.116	4.995	10.566	13.564	16.563	22.350	30.160	36.829	40.698	42.478	47.276	54.918	74.106
R	0.150	2.44E-02	0.391	1.563	6.251	12.501	15.750	18.947	25.001	32.989	39.686	43.529	45.287	50.001	57.436	75.786
R	0.250	5.26E-02	0.651	2.292	8.070	15.141	18.674	22.086	28.407	36.538	43.214	46.996	48.716	53.299	60.447	77.747
R	0.400	0.113	1.086	3.365	10.423	18.344	22.148	25.751	32.285	40.476	47.061	50.746	52.412	56.820	63.621	79.763
R	0.650	0.300	2.081	5.480	14.427	23.409	27.507	31.297	37.983	46.097	52.447	55.944	57.513	61.630	67.894	82.398

TABLE 4A

100/p Ratios at the Acceptable Quality Level (normal inspection)
for the MIL-STD-105D Plans, r = 0.99

NOTE—These plans assume the characteristic being measured has a Weibull distribution.

NOTE—Where scientific notation is used (that is, E-x), the decimal point is moved to the left x places (for example, if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

AQL p(%)	Shape Parameter, β														
	0.333	0.500	0.667	1.000	1.333	1.500	1.667	2.000	2.500	3.000	3.333	3.500	4.000	5.000	10.000
0.010	9.85E-05	9.90E-03	9.93E-02	0.995	3.151	4.626	6.291	9.975	15.817	21.509	25.081	26.789	31.584	39.771	63.064
0.015	3.33E-04	2.23E-02	0.182	1.493	4.270	6.062	8.024	12.217	18.603	24.621	28.326	30.079	34.953	43.131	65.674
0.025	1.54E-03	6.19E-02	0.392	2.488	6.264	8.522	10.902	15.773	22.821	29.192	33.017	34.807	39.715	47.771	69.116
0.040	6.31E-03	0.158	0.794	3.981	8.912	11.659	14.454	19.952	27.541	34.145	38.018	39.810	44.667	52.480	72.443
0.065	2.71E-02	0.419	1.646	6.470	12.828	16.116	19.343	25.435	33.446	40.144	43.981	45.735	50.433	57.833	76.048
0.100	9.87E-02	0.991	3.141	9.955	17.723	21.480	25.051	31.551	39.739	46.346	50.051	51.728	56.171	63.039	79.397
0.150	0.333	2.231	5.772	14.936	24.026	28.151	31.955	38.647	46.741	53.057	56.529	58.085	62.167	68.367	82.684
0.250	1.545	6.203	12.430	24.906	35.256	39.585	43.429	49.906	57.348	62.917	65.901	67.223	70.644	75.729	87.022
0.400	6.342	15.904	25.184	39.879	50.184	54.179	57.604	63.150	69.231	73.607	75.897	76.900	79.467	83.205	91.217
0.650	27.318	42.101	52.266	64.886	72.295	74.949	77.142	80.552	84.112	86.573	87.830	88.375	89.751	91.713	95.767
1.000	100.000	100.000	100.000	100.000	100.000	100.000	100.000	100.000	100.000	100.000	100.000	100.000	100.000	100.000	100.000
1.500	340.068	226.140	184.409	150.379	135.797	131.258	127.736	122.629	117.727	114.568	113.020	112.364	110.738	108.502	104.164
2.500	1,598.588	634.587	399.823	251.910	199.956	185.139	174.079	158.717	144.710	136.066	131.939	130.209	125.983	120.295	109.679
4.000	6,701.020	1,649.785	818.598	406.175	286.111	254.571	231.861	201.538	175.180	159.553	152.270	149.251	141.964	132.356	115.046
6.500	29,904.443	4,471.884	1,729.290	668.721	415.847	354.947	312.714	258.596	213.845	188.400	176.837	172.101	160.809	146.234	120.927
10.000	#####	10,989.922	3,394.2671	1,048.328	582.603	478.996	409.542	323.779	255.976	218.860	202.371	195.691	179.939	159.992	126.488



TABLE 4B

100t/p Ratios at the Limiting Quality Level for the MIL-STD-105D Plans, r = 0.99, Consumer's Risk = 0.10

NOTE—These plans assume the characteristic being measured has a Weibull distribution.

NOTE—Where scientific notation is used (that is, E-x), the decimal point is moved to the left x places (for example, if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

Table with columns: Code Letter, AQL (p%), and Shape Parameter beta (0.333, 0.50, 0.667, 1.000, 1.333, 1.500, 1.667, 2.000, 2.500, 3.000, 3.333, 3.500, 4.000, 5.000, 10.000). Rows include codes A through N with various AQL values.

TABLE 4B

100t/p Ratios at the Limiting Quality Level
for the MIL-STD-105D Plans, r = 0.99, Consumer's Risk = 0.10

NOTE—These plans assume the characteristic being measured has a Weibull distribution.

NOTE—Where scientific notation is used (that is, E-x), the decimal point is moved to the left x places (for example, if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

Code Letter	AQL (p%)	Shape Parameter, β														
		0.333	0.50	0.667	1.000	1.333	1.500	1.667	2.000	2.500	3.000	3.333	3.500	4.000	5.000	10.000
N	0.100	46.517	60.035	68.203	77.482	82.585	84.360	85.807	88.024	90.299	91.848	92.632	92.970	93.821	95.026	97.481
N	0.150	119.527	112.627	109.328	106.126	104.560	104.043	103.632	103.018	102.407	102.002	101.800	101.713	101.498	101.196	100.596
N	0.250	237.110	177.814	153.984	133.347	124.090	121.150	118.847	115.476	112.200	110.068	109.017	108.570	107.460	105.925	102.920
N	0.400	638.255	344.083	252.637	185.495	158.946	150.969	144.877	136.196	128.036	122.869	120.365	119.307	116.703	113.153	106.373
N	0.650	1,312.698	556.472	362.312	235.897	190.345	177.207	167.353	153.589	140.958	133.119	129.365	127.789	123.931	118.726	108.961
N	1.000	2,970.497	959.149	545.023	309.701	233.457	212.469	197.045	175.983	157.173	145.763	140.373	138.124	132.659	125.369	111.968
N	1.500	6,705.535	1,650.526	818.873	406.267	286.160	254.609	231.892	201.561	175.196	159.565	152.280	149.261	141.972	132.362	115.049
N	2.500	18,813.286	3,283.294	1,371.615	573.000	370.353	320.211	285.032	239.374	201.031	178.944	168.829	164.670	154.717	141.785	119.074
P	0.015	2.349	8.201	15.326	28.638	39.148	43.447	47.224	53.515	60.643	65.915	68.720	69.959	73.154	77.873	88.246
P	0.065	11.344	23.434	33.681	48.408	58.035	61.652	64.707	69.576	74.811	78.519	80.441	81.279	83.412	86.494	93.002
P	0.100	29.115	43.929	53.959	66.279	73.456	76.018	78.131	81.412	84.830	87.188	88.392	88.913	90.228	92.103	95.970
P	0.150	57.692	69.301	75.955	83.247	87.152	88.494	89.582	91.240	92.928	94.071	94.648	94.896	95.520	96.399	98.183
P	0.250	154.942	133.900	124.476	115.715	111.569	110.220	109.153	107.571	106.012	104.986	104.476	104.258	103.716	102.962	101.470
P	0.400	317.939	216.220	178.308	147.044	133.532	129.310	126.028	121.262	116.675	113.715	112.262	111.646	110.119	108.016	103.931
P	0.650	716.976	371.823	267.764	192.827	163.635	154.922	148.286	138.862	130.037	124.468	121.773	120.636	117.840	114.034	106.787
P	1.000	1,610.956	637.856	401.367	252.558	200.342	185.456	174.348	158.921	144.859	136.182	132.041	130.305	126.064	120.357	109.707
P	1.500	4,482.455	1,261.858	669.511	355.226	258.749	232.811	213.946	188.475	166.036	152.581	146.269	143.644	137.286	128.855	113.514
Q	0.010	0.616	3.359	7.847	18.328	28.012	32.266	36.131	42.812	50.728	56.803	60.109	61.583	65.431	71.224	84.394
Q	0.040	2.972	9.594	17.239	30.974	41.519	45.779	49.499	55.654	62.575	67.660	70.356	71.544	74.602	79.104	88.941
Q	0.065	7.622	17.977	27.608	42.399	52.543	56.438	59.760	65.114	70.948	75.125	77.305	78.258	80.693	84.231	91.777
Q	0.100	15.093	28.348	38.850	53.242	62.329	65.691	68.510	72.967	77.715	81.050	82.771	83.520	85.421	88.156	93.891
Q	0.150	40.479	54.721	63.623	73.974	79.764	81.793	83.454	86.008	88.640	90.440	91.353	91.747	92.740	94.149	97.030
Q	0.250	82.949	88.282	91.076	93.959	95.434	95.931	96.330	96.932	97.538	97.944	98.148	98.235	98.454	98.761	99.379
Q	0.400	186.673	151.608	136.628	123.129	116.888	114.879	113.296	110.964	108.679	107.182	106.441	106.125	105.339	104.249	102.102
Q	0.650	418.279	259.604	204.519	161.122	143.010	137.437	133.135	126.934	121.021	117.234	115.384	114.601	112.665	110.010	104.886
Q	1.000	1,158.179	511.898	340.320	226.252	184.478	172.343	163.213	150.417	138.623	131.280	127.755	126.273	122.644	117.738	108.507
R	0.025	0.725	3.747	8.516	19.356	29.182	33.461	37.333	43.995	51.847	57.846	61.100	62.551	66.329	72.005	84.856
R	0.040	1.859	7.018	13.635	26.491	36.926	41.248	45.067	51.470	58.782	64.225	67.132	68.418	71.742	76.669	87.561
R	0.065	3.680	11.063	19.183	33.262	43.798	48.006	51.661	57.673	64.384	69.285	71.876	73.015	75.943	80.240	89.577
R	0.100	9.860	21.343	31.401	46.198	56.036	59.761	62.918	67.969	73.426	77.305	79.321	80.201	82.444	85.689	92.568
R	0.150	20.187	34.412	44.930	58.662	67.030	70.076	72.613	76.591	80.787	83.712	85.213	85.865	87.516	89.882	94.806
R	0.250	45.368	59.043	67.356	76.839	82.071	83.892	85.379	87.658	89.998	91.593	92.401	92.749	93.626	94.867	97.400
R	0.400	101.472	100.979	100.733	100.488	100.366	100.325	100.293	100.244	100.195	100.163	100.146	100.139	100.122	100.097	100.049
R	0.650	280.066	198.689	167.352	140.957	129.365	125.716	122.872	118.725	114.719	112.123	110.848	110.305	108.961	107.107	103.492

TABLE 4C

100t/p Ratios at the Limiting Quality Level
for the MIL-STD-105D Plans, r = 0.99, Consumer's Risk = 0.05

NOTE—These plans assume the characteristic being measured has a Weibull distribution.

NOTE—Where scientific notation is used (that is, E-x), the decimal point is moved to the left x places (for example, if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

Code Letter	AQL (p%)	Shape Parameter, β														
		0.333	0.50	0.667	1.000	1.333	1.500	1.667	2.000	2.500	3.000	3.333	3.500	4.000	5.000	10.000
A	6.500	331,037,568.113	2,221,185.631	181,944.378	14,903.643	4265.494	2811.005	2013.610	1220.805	740.145	530.189	448.733	417.773	349.400	272.056	164.941
B	4.000	98,085,205.367	987,193.614	99,037.975	9,935.762	3147.030	2145.198	1578.777	996.783	629.333	463.163	397.338	372.074	315.719	250.865	158.387
C	2.500	21,186,404.359	355,389.701	46,028.691	5,961.457	2145.430	1526.048	1162.014	772.105	513.028	390.647	340.883	321.546	277.868	226.501	150.500
C	10.000	121,084,759.250	1,136,038.340	110,038.520	10,658.510	3317.205	2248.007	1646.713	1032.401	647.260	474.132	405.797	379.614	321.310	254.413	159.503
D	1.500	5,172,462.002	138,824.102	22,743.047	3,725.911	1508.080	1115.548	876.475	610.402	425.102	333.998	296.053	281.141	247.063	206.180	143.590
D	6.500	25,360,556.828	400,656.805	50,359.266	6,329.746	2244.087	1588.269	1204.569	795.597	525.478	398.531	347.069	327.101	282.063	229.233	151.404
D	10.000	75,587,482.973	829,786.929	86,941.062	9,109.264	2948.577	2024.521	1498.615	954.425	607.846	449.947	387.119	362.955	308.938	246.545	157.018
E	1.000	1,205,416.725	52,572.441	10,979.147	2,292.868	1047.814	807.085	654.979	478.839	350.067	284.092	255.926	244.726	218.824	187.101	136.785
E	4.000	5,417,662.996	143,177.461	23,275.874	3,783.880	1525.643	1127.089	884.631	615.132	427.735	335.721	297.428	282.383	248.019	206.818	143.812
E	6.500	14,483,173.782	275,788.294	38,056.765	5,251.555	1950.814	1402.357	1076.893	724.676	487.658	374.481	328.161	310.106	269.198	220.830	148.603
E	10.000	31,316,328.959	461,155.328	55,960.994	6,790.842	2365.608	1664.495	1256.476	824.066	540.467	407.982	354.468	333.739	287.065	232.480	152.473
F	0.650	331,037.568	22,211.856	5,753.586	1,490.364	758.524	605.613	505.796	386.052	294.657	246.092	224.899	216.385	196.482	171.656	131.017
F	2.500	1,421,864.978	58,691.099	11,924.198	2,422.625	1091.980	837.254	676.974	492.202	357.861	289.353	260.187	248.605	221.856	189.172	137.540
F	4.000	3,609,535.582	109,219.676	18,998.778	3,304.840	1378.361	1029.833	815.625	574.877	405.191	320.910	285.591	271.671	239.766	201.294	141.878
F	6.500	7,354,597.617	175,538.592	27,119.361	4,189.733	1646.796	1206.306	940.398	647.281	445.528	347.319	306.659	290.725	254.417	211.075	145.284
F	10.000	22,143,822.623	366,017.398	47,057.223	6,049.937	2169.268	1541.111	1172.332	777.813	516.060	392.570	342.393	322.903	278.893	227.170	150.721
G	0.400	80,819.719	8,676.506	2,842.881	931.478	533.187	442.706	381.508	305.201	244.157	210.406	195.322	189.194	174.700	156.255	125.002
G	1.500	336,784.430	22,468.186	5,803.313	1,498.939	761.795	607.933	507.540	387.161	295.334	246.563	225.287	216.740	196.764	171.853	131.093



TABLE 4C

100t/p Ratios at the Limiting Quality Level for the MIL-STD-105D Plans, r = 0.99, Consumer's Risk = 0.05

NOTE—These plans assume the characteristic being measured has a Weibull distribution.

NOTE—Where scientific notation is used (that is, E-x), the decimal point is moved to the left x places (for example, if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

Table with columns: Code Letter, AQL (p%), and Shape Parameter, beta (0.333, 0.50, 0.667, 1.000, 1.333, 1.500, 1.667, 2.000, 2.500, 3.000, 3.333, 3.500, 4.000, 5.000, 10.000). Rows include codes G, H, J, K, L, M, N, P, Q with various AQL values.

TABLE 4C

100t/μ Ratios at the Limiting Quality Level
for the MIL-STD-105D Plans, r = 0.99, Consumer's Risk = 0.05

NOTE—These plans assume the characteristic being measured has a Weibull distribution.

NOTE—Where scientific notation is used (that is, E-x), the decimal point is moved to the left x places (for example, if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

Code Letter	AQL (p%)	Shape Parameter, β														
		0.333	0.50	0.667	1.000	1.333	1.500	1.667	2.000	2.500	3.000	3.333	3.500	4.000	5.000	10.000
Q	0.040	5.391	14.270	23.218	37.776	48.185	52.257	55.761	61.462	67.746	72.289	74.673	75.719	78.398	82.308	90.724
Q	0.065	12.616	25.154	35.519	50.154	59.597	63.125	66.097	70.819	75.879	79.451	81.300	82.106	84.154	87.109	93.332
Q	0.100	23.595	38.183	48.574	61.793	69.695	72.548	74.914	78.608	82.485	85.175	86.553	87.150	88.661	90.821	95.300
Q	0.150	58.955	70.310	76.782	83.851	87.626	88.921	89.971	91.570	93.197	94.298	94.853	95.092	95.692	96.539	98.254
Q	0.250	115.604	110.149	107.519	104.952	103.691	103.275	102.942	102.446	101.952	101.624	101.461	101.391	101.216	100.971	100.484
Q	0.400	249.121	183.770	157.836	135.562	125.633	122.487	120.028	116.431	112.942	110.674	109.557	109.082	107.903	106.274	103.089
Q	0.650	537.763	306.945	231.897	175.198	152.282	145.329	139.997	132.363	125.145	120.553	118.320	117.376	115.049	111.868	105.768
Q	1.000	1,430.607	589.314	378.234	242.758	194.482	180.627	170.257	155.807	142.584	134.397	130.482	128.840	124.823	119.408	109.274
R	0.025	1.315	5.573	11.469	23.606	33.867	38.196	42.055	48.586	56.132	61.803	64.850	66.201	69.704	74.921	86.557
R	0.040	3.077	9.820	17.542	31.337	41.883	46.136	49.846	55.979	62.867	67.923	70.602	71.782	74.819	79.289	89.044
R	0.065	5.753	14.902	23.985	38.603	48.974	53.017	56.490	62.131	68.336	72.813	75.160	76.189	78.823	82.666	90.921
R	0.100	14.361	27.423	37.896	52.367	61.560	64.969	67.832	72.365	77.201	80.603	82.360	83.125	85.068	87.864	93.736
R	0.150	28.135	42.937	53.042	65.526	72.830	75.441	77.598	80.948	84.443	86.857	88.090	88.623	89.971	91.893	95.861
R	0.250	60.546	71.569	77.811	84.598	88.211	89.449	90.452	91.977	93.529	94.577	95.106	95.334	95.905	96.710	98.341
R	0.400	130.459	119.394	114.219	109.268	106.873	106.087	105.462	104.531	103.609	102.998	102.695	102.565	102.240	101.788	100.890
R	0.650	345.942	228.737	185.995	151.240	136.380	131.758	128.174	122.980	117.996	114.786	113.214	112.547	110.896	108.626	104.224

APPENDIX

(Nonmandatory Information)

X1. MATHEMATICAL MATERIAL

X1.1 *Computation of the Conversion Factors*—For the attribute acceptance procedure used with these plans, the probability of acceptance for a lot depends only on the probability, p', of item life being less than (or equal to) the test truncation time, t. With the magnitude of the shape parameter known, the magnitude of the location parameter taken as zero, and the value of test truncation time, t, preassigned, p' becomes a function only of the lot quality under evaluation (mean life, hazard rate, or reliable life). The means for the mathematical determination of the specific relationships are outlined below.

X1.2 *Evaluation in Terms of Mean Life (μ):*

X1.2.1 As noted, p' is a function of the test truncation time, t, and the mean item life, μ, for the lot. To make use of Practice E2234 plans for mean life evaluation, it is necessary to find t and μ combinations equivalent to the p' (percent defective) values associated with each of the Practice E2234 plans. To make the conversion factors available for general use rather than preparing them in terms of specific values of t and μ, the dimensionless ratio t/μ has been used (for ease in tabulation and use, 100t/μ factors are provided). The probability, p', of an item failing before time, t, is the value of the cumulative density function at time t. For the Weibull distribution (with the location parameter equal to zero), this is given by:

$$p' = F(t) = 1 - e^{-\left(\frac{t}{\eta}\right)^\beta} \tag{X1.1}$$

X1.2.2 Here, η is the scale or characteristic life parameter. The formula for the mean of the Weibull distribution is:

$$\mu = \eta\Gamma(1/\beta + 1) \tag{X1.2}$$

X1.2.3 Solving Eq X1.1 for t gives:

$$t = \eta\{-\ln(1 - p')\}^{1/\beta} \tag{X1.3}$$

X1.2.4 Then the ratio of (Eq X1.3) to (Eq X1.2) × 100 gives the appropriate 100t/μ ratio. This equation is:

$$100t/\mu = \frac{100\{-\ln(1 - p')\}^{1/\beta}}{\Gamma(1/\beta + 1)} \tag{X1.4}$$

X1.2.5 Further details will be found in Refs (1) and (4).

X1.3 *Evaluation in Terms of Hazard Rate, h(t):*

X1.3.1 The instantaneous failure rate or the hazard rate at any specified time, t, which is symbolized by h(t), is given by relationship (Eq X1.5):

$$h(t) = \frac{f(t)}{1 - F(t)} \tag{X1.5}$$

X1.3.2 The value f(t) is the population probability density function and F(t) is the cumulative distribution function of the population. For the Weibull distribution (with the location parameter equal to zero), the expression for the population density function is:

$$f(t) = \frac{\beta}{\eta} \left(\frac{t}{\eta}\right)^{\beta-1} e^{-(t/\eta)^\beta} \tag{X1.6}$$

X1.3.3 The expression for the cumulative density function is:

$$F(t) = 1 - e^{-(t/\eta)^\beta} \tag{X1.7}$$

X1.3.4 From Eq X1.6 and X1.7, the following expression for hazard rate may be obtained:

$$h(t) = \frac{\beta}{\eta} \left(\frac{t}{\eta} \right)^{\beta-1} \quad (\text{X1.8})$$

X1.3.5 A more useful form for the steps to follow is given if both sides of this equation are multiplied by (t/b) which gives:

$$\frac{t h(t)}{\beta} = \left(\frac{t}{\eta} \right)^{\beta} \quad (\text{X1.9})$$

X1.3.6 The probability, p' of an item failing before the end of the testing time, t , is given by the cumulative density function, $F(t)$, as shown in Eq X1.7. By combining Eq X1.9 and Eq X1.7, p' in terms of $h(t)$ becomes:

$$p' = 1 - e^{-\frac{t h(t)}{\beta}} \quad (\text{X1.10})$$

X1.3.7 By transposing and taking the natural logarithm, the following required expression is found:

$$t h(t) = -\beta \ln(1 - p') \quad (\text{X1.11})$$

X1.3.8 Values for this dimensionless product, $t h(t)$, may thus be found by use of this expression for all p' (percent defective) values associated with Practice E2234 plans. Note that the time t at which the hazard rate is to be evaluated is the same as the test truncation time. Further details may be found in Refs (2) and (5).

X1.4 *Evaluation in Terms of Reliable Life* (ρ_r):

X1.4.1 With the location parameter equal to zero, the value for reliable life, ρ_r , where r is the proportion of items surviving beyond a life of ρ , is given by the expression:

$$\rho_r = \eta(-\ln(r))^{1/\beta} \quad (\text{X1.12})$$

X1.4.2 The probability, p' of an item failing before time t is given by:

$$p' = F(t) = 1 - e^{-(t/\eta)^\beta} \quad (\text{X1.13})$$

X1.4.3 Substitution of the value for η given by Eq X1.12 for η in Eq X1.13 and simplifying gives:

$$p' = 1 - r \left(\frac{t}{\rho_r} \right)^\beta \quad (\text{X1.14})$$

X1.4.4 This can be simplified to the following required form:

$$\frac{t}{\rho_r} = \left(\frac{\ln(1 - p')}{\ln(r)} \right)^{1/\beta} \quad (\text{X1.15})$$

X1.4.5 Values for the dimensionless ratio $100t/\rho_r$, have been determined for all the p' (percent defective) values associated with Practice E2234 plans. Further details may be found in Refs (3) and (6).

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