



Standard Practice for Inclusion of Precision Statement Variation in Specification Limits¹

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1. Scope

1.1 This practice covers a method of determining rational specification limits by inclusion of the precision of the test method used in the specification.

1.2 The values stated in SI units are to be regarded as standard. No other units of measurement are included in this standard.

1.3 *This standard does not purport to address all of the safety concerns, if any, associated with its use. It is the responsibility of the user of this standard to establish appropriate safety and health practices and determine the applicability of regulatory limitations prior to use.*

2. Referenced Documents

2.1 *ASTM Standards:*²

C670 Practice for Preparing Precision and Bias Statements for Test Methods for Construction Materials

C802 Practice for Conducting an Interlaboratory Test Program to Determine the Precision of Test Methods for Construction Materials

D2172 Test Methods for Quantitative Extraction of Bitumen From Bituminous Paving Mixtures

D2726 Test Method for Bulk Specific Gravity and Density of Non-Absorptive Compacted Bituminous Mixtures

E177 Practice for Use of the Terms Precision and Bias in ASTM Test Methods

2.2 *Federal Highway Administration Report:*

FHWA Report HI-93-047 Materials Control and Acceptance—Quality Assurance, Federal Highway Administration, May 1993³

¹ This practice is under the jurisdiction of Committee D04 on Road and Paving Materials and is the direct responsibility of Subcommittee D04.94 on Statistical Procedures and Evaluation of Data.

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² For referenced ASTM standards, visit the ASTM website, www.astm.org, or contact ASTM Customer Service at service@astm.org. For *Annual Book of ASTM Standards* volume information, refer to the standard's Document Summary page on the ASTM website.

³ Available from National Technical Information Service (NTIS), U.S. Department of Commerce, 5285 Port Royal Rd., Springfield, VA 22161.

3. Terminology

3.1 For definitions of terms used in this practice, consult Practice E177.

4. Significance and Use

4.1 Each test method has a limited precision. Even if a test is performed as carefully and as correctly as possible on a material which is as homogeneous as can be obtained, the test will still vary from one to another. A widely used measure of the variation of the test results from a test method is the standard deviation (σ). In an ASTM standard test, the standard deviation of the test method can be found in the Precision and Bias statement for the test. The “Blue Book,” *Form and Style for ASTM Standards*, requires that all test methods include Precision and Bias statements. Practice C670 and Practice C802 provide guidance for determination of these values.

4.2 If the precision of a test method is low and the precision of the test has not been properly considered in a material specification, a uniform material with the right quality may still be rejected most of the time because of the wide variation of the test results. In order to have rational specification limits, the precision of the test used should be properly included in a specification.

4.3 This practice provides a guideline for proper inclusion of precision of the test method in a rational specification.

5. Procedure

5.1 Determine the effective standard deviation (σ_x) of the test results due to the combined effects of materials variation and test variation using Eq 1:

$$\sigma_x = (\sigma_M^2 + \sigma_T^2) \quad (1)$$

where:

σ_M = standard deviation of test property due to material variation (see Note 1), and

σ_T = standard deviation of test property due to test method (see Note 2).

NOTE 1— σ_M is the expected standard deviation of the material property when the material is produced in a properly controlled process. A standard deviation which is representative of the acceptable variation of the material can be used. It can be calculated from the data obtained from properly produced materials.

NOTE 2— σ_T is the standard deviation as given in the precision statement for the test method used to measure the test property.

5.2 Determine the standard deviation of the mean of the test results ($\sigma_{\bar{x}}$) using Eq 2:

$$\sigma_{\bar{x}} = \sigma_x / \sqrt{n} \quad (2)$$

where:

n = number of tests performed.

5.3 For a two-ended specification (with both a minimum and maximum limits), the specification limits for the average test value from n test (\bar{x}) should be the following:

$$\mu - Z_{\alpha/2} \sigma_{\bar{x}} \leq \bar{x} \leq \mu + Z_{\alpha/2} \sigma_{\bar{x}} \quad (3)$$

where:

μ = target property

$Z_{\alpha/2}$ = critical number of standard deviations for $(1-\alpha)$ confidence interval. (See Table 1 for values of $Z_{\alpha/2}$ for different specified confidence intervals.)

TABLE 1 Z Values for Different Confidence Levels

Confidence Level (1 - α):	90 %	95 %	97.5 %	99.0 %
$Z_{\alpha/2}$ (Two-End Specification)	1.645	1.960	2.243	2.575
Z_{α} (One-End Specification)	1.282	1.645	1.960	2.327

5.4 For a one-ended specification (with only a maximum or minimum limit), the specification limit for the average test value from n test (\bar{x}) should be the following:

$$\bar{x} \geq \mu - Z_{\alpha} \sigma_{\bar{x}} \quad (\text{with a minimum limit}) \quad (4)$$

or

$$\bar{x} \leq \mu + Z_{\alpha} \sigma_{\bar{x}} \quad (\text{with a maximum limit}) \quad (5)$$

APPENDIXES

X1. First Example of the Application of Precision Limits to Specification Writing

X1.1 Problem Statement

X1.1.1 A specification is to be written for the asphalt content of an asphalt mixture with aggregate water absorption capacity of less than 1.25 %. Three reflux asphalt extraction tests are to be run and the average of three test results is to be used for acceptance purpose. The target asphalt content is 6.2 %. It is assumed that the contractor can reasonably control the asphalt content with a standard deviation of 0.20 % (see Note X1.1).

NOTE X1.1—Typical standard deviations of different material properties can be found in FHWA Report HI-93-047. The typical range of standard deviation of asphalt content was given as 0.15 % – 0.30 %.

X1.2 Precision statement for Test Methods D2172 (Method B—Reflux) is given in Table X1.1.

X1.3 The combined standard deviation of the measured asphalt content:

TABLE X1.1 Mixes with Agg. of Water Absorption < 1.25 %

	Standard Deviation	Acceptable Range of Two Test Results
Single-Operator	0.19 %	.054 %
Multi-Operator	0.23 %	0.65 %

$$\sigma_x = \sqrt{(0.2^2 + 0.23^2)} = 0.305 \% \quad (X1.1)$$

X1.4 The standard deviation of the mean of three test results:

$$\sigma_{\bar{x}} = 0.305 / \sqrt{3} = 0.176 \% \quad (X1.2)$$

X1.5 Specification limits using a 95 % confidence interval:

$$= 6.2 \% \pm Z_{\alpha/2} (0.176 \%) \quad (X1.3)$$

$$= 6.2 \% \pm 1.96 (0.176 \%)$$

$$= 6.2 \% \pm 0.3 \%$$

X2. Second Example

X2.1 Problem Statement

X2.1.1 A specification is to be written for the asphalt content of the asphalt mixture as described in Example 1. However, the average of seven test results (instead of three test results) is to be used.

X2.2 The combined standard deviation of the measured asphalt content is the same as in Example 1:

$$\sigma_x = \sqrt{(0.2^2 + 0.23^2)} = 0.305 \% \quad (\text{X2.1})$$

X2.3 The standard deviation of the mean of seven test results:

$$\sigma_x^- = 0.305 / \sqrt{7} = 0.115 \% \quad (\text{X2.2})$$

X2.4 Specification limits using a 95 % confidence interval:

$$\begin{aligned} &= 6.2 \% \pm 1.96 (0.115 \%) \quad (\text{X2.3}) \\ &= 6.2 \% \pm 0.2 \% \end{aligned}$$

X3. Third Example

X3.1 Problem Statement

X3.1.1 A specification is to be written for the compacted density of an asphalt mixture with non-absorptive aggregate. The target density is 2.365 g/cm³. Five density measurements in accordance with Test Method **D2726** are to be made, and the average test result is to be used for acceptance purposes. It is assumed that the contractor can control the density of the mixture with a standard deviation of 0.02 g/cm³.

X3.2 Precision statement for Test Method **D2726** is in **Table X3.1**.

X3.3 The combined standard deviation of the measured density:

$$\begin{aligned} \sigma_x &= \sqrt{(0.200^2 + 0.0269^2)} \quad (\text{X3.1}) \\ &= 0.0335 \text{ g/cm}^3 \end{aligned}$$

X3.4 The standard deviation of the mean of five test results:

$$\begin{aligned} \sigma_x^- &= (0.0335 / \sqrt{5}) \quad (\text{X3.2}) \\ &= 0.0150 \text{ g/cm}^3 \end{aligned}$$

X3.5 Specification limit using a 95 % confidence interval:

$$\begin{aligned} &\text{Minimum average measured density} \quad (\text{X3.3}) \\ &= 2.365 - Z_\alpha (0.015) \\ &= 2.365 - 1.65 (0.015)^3 \\ &= 2.340 \text{ g/cm}^3 \end{aligned}$$

X3.6 With this specification, a contractor who compacts the asphalt mixture to an average density of 2.356 g/cm³ would meet the specification 95 % of the time.

TABLE X3.1 Precision Statement Values

	Standard Deviation	Acceptable Range of Two Test Results
Single-Operator Precision	0.0124	0.035
Multi-Operator Precision	0.0269	0.076

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